

Phonon Confinement Model to Measure the Average Sizes of Anatase Nanoparticles Synthesized by a Solvothermal Method Using H₂O₂

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Neste trabalho, nanopartículas de dióxido de titânio (TiO₂) cristalino, com um tamanho de cristalito médio (e.g., 8 nm) e área de superfície (e.g., 192 m² g⁻¹) variáveis, foram sintetizadas em fase anatase pura, utilizando H₂O₂ como agente de redução da taxa de hidrólise dos íons de titânio, em solução de isopropanol (IP) como meio de reação. As nanopartículas de TiO₂ foram caracterizadas por meio das técnicas de difratometria de raios X de pó (XRD), espectroscopia Raman e microscopia eletrônica de transmissão (TEM). A alteração dos parâmetros de síntese permitiu o controle do tamanho das nanopartículas e evitou o processo de coalescência. Foi determinada uma dependência entre o número de onda Raman e o tamanho dos nanocristais, o que é bastante útil para uma rápida verificação do tamanho de nanocristais de TiO₂.

In this work, crystalline titanium dioxide (TiO₂) nanoparticles with variable average crystallite sizes (e.g., 8 nm) and surface areas (e.g., 192 m² g⁻¹) were synthesized in pure anatase phase using H₂O₂ to reduce the hydrolysis rate of the titanium ions. An isopropanol (IP) solution was employed as the reaction medium. The TiO₂ nanoparticles were characterized by powder X-ray diffraction analysis (XRD), Raman spectroscopy and transmission electron microscopy (TEM). By changing the synthesis parameters it was possible to control nanoparticle size and avoid the coalescence process. A dependence of the Raman wavenumber on the nanocrystal sizes was determined, which is quite useful for a quick check of the size of TiO₂ nanocrystals.

Keywords: anatase, nanoparticles, solvothermal method, H₂O₂, Raman spectroscopy.

Introduction

Titanium dioxide (titania, TiO₂) is used in different environmental-related applications, such as photocatalytic degradation for purification of polluted air and wastewater treatment.^{1,2} Other technological applications of TiO₂ are in pigments, wet-type solar cells,³ sensors,⁴ photocatalysts⁵ and electronic material.⁶

There are three main crystallographic forms of TiO₂: rutile (tetragonal), anatase (tetragonal), and brookite (orthorhombic).^{7,8} Rutile is thermodynamically stable and

the other two forms are metastable.⁹ The anatase form is very important because it has been used in photocatalysis and various other applications with good efficiency.¹⁰

Various methods for synthesizing anatase TiO₂ have been extensively described in the scientific literature including sol-gel, precipitation, aerosol synthesis and solvothermal techniques, among others.^{9,11,12,13} In some of these processes, preparation costs are high, the reaction is time consuming and the overall process is complex with many steps. In order to obtain ultrafine particles, milling and thermal treatment are also needed. In the solvothermal method, the reaction conditions, such as solution concentration, temperature and pH, have a strong

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influence on the reaction process but they are relatively easy to control, and the cost is low. Some of the advantages of the solvothermal method over other preparation techniques include the purity, homogeneity and stoichiometry control of the obtained particles.

The synthesis of TiO₂ nanocrystals also allows the investigation of size-induced effects such as the softening and broadening of Raman modes, lattice expansion and shift in the optical absorption band edge.¹⁴ The softening and broadening of the Raman allowed modes are directly correlated with the nanocrystal size, so that Raman spectroscopy can be used to readily estimate the average size of TiO₂ nanocrystals.^{14,15}

In this study, the synthesis of anatase titanium dioxide nanoparticles employing different reaction parameters is reported. Hydrogen peroxide (H₂O₂) was used for slowing the hydrolysis rate of the titanium ions in solution. Hydrogen peroxide is an ideal environmentally friendly solvent and oxidant, and has been widely used in the synthesis of nanostructured inorganic materials.¹⁶ Considering that the synthesis of TiO₂ nanocrystals is based on a nucleation and growth process, the presence of H₂O₂ modifies crystallization by increasing the nucleation rate. The presence of peroxides can inhibit the hydrolysis of the titanium ions in solution (in fact a titanium oxyanion). As a result, a colloidal dispersion with a crystallite size smaller than that obtained in the absence of H₂O₂ was obtained.

Moreover, by analyzing the Raman data we determined an empirical relationship that correlates the Raman frequency with the anatase nanocrystal diameter. The Raman scattering data is analyzed based on the phonon confinement model.¹⁷ This is of practical interest for using Raman spectroscopy as a quick check of TiO₂ nanocrystal sizes. This evaluation is readily available, non-destructive, does not require any special preparation of the sample and can be applied to different kinds of TiO₂-based samples.

Experimental

All chemicals (reagent grade) were used as received, without further purification processes.

Titania Nanoparticle Synthesis

Synthesis with variation of time and temperature

Titania nanoparticles were produced by mixing 2.5 mL of titanium isopropoxide (TIP, Ti[OCH(CH₃)₂]₄, > 99%, Acros Organics (Pittsburg, USA)) and 8.0 mL of hydrogen peroxide solution (H₂O₂ 10% v/v, > 99%, Acros Organics) diluted in 50 mL of isopropanol (IP, 99.5%, Vetec (Duque de Caxias, Brazil)). The solution was poured into an

autoclavable bottle and was then placed in a regular furnace. The TiO₂ nanocrystals were prepared using different times (6.0, 12, 24 and 72h at 100 °C) and temperatures (80, 90 and 100 °C for 72h of reaction).

Synthesis with variation of pH

Titania nanoparticles were produced by mixing 2.5 mL of titanium isopropoxide and 8.0 mL hydrogen peroxide solution diluted in a mixture of H₂O (25 mL)/isopropanol (25 mL). The solution was poured into an autoclavable bottle and was then placed in a regular furnace at 100 °C for 72h. The TiO₂ nanocrystals were prepared using different pHs (2.0, 7.0 and 12) controlled by addition of HCl or NaOH.

Sample Calcination

In the study of grain size as a function of calcination temperature, the sample powders produced by solvothermal reaction for 72h at 100 °C were heated in the temperature range from 100 to 900 °C. The calcination was performed in a muffle furnace in which the heating rate was equal to 10 °C min⁻¹. Samples were kept at the selected temperatures for 3h.

Characterization

X-Ray diffraction (XRD) patterns were recorded with a Rigaku diffractometer (D-Max 2500PC, Japan), employing Cu-K_α radiation in the 2θ range from 5° to 75° and a scan rate of 0.2 degree min⁻¹. The surface area was determined by the BET multi-point method using a Micromeritics ASAP 2000 equipment (Norcross, USA) for analysis of adsorption/desorption. The pH of the solutions was measured with a digital pH meter (Sentron Model 1001 pH System (Roden, Netherlands)). For the transmission electron microscopy (TEM) measurements, a Philips microscope model CM200 (Eindhoven, Netherlands) was used with 200 kV of voltage acceleration. A drop of the aqueous suspension was deposited on a carbon-covered copper grid. Raman spectra were obtained using a Bruker RFS-100/S FT-Raman spectrometer (Ettlingen, Germany). All measurements in this work were made at room temperature.

Results and Discussion

In this solvothermal synthesis, crystalline powders were produced. Neither rutile nor brookite phases were observed in the XRD patterns shown in Figure 1a and 1b, thus indicating that the obtained TiO₂ nanoparticles are a single anatase phase (JCPDS No.78-1285). The crystal

structure of the TiO₂ nanoparticles was not affected by changing the reaction temperature and time. Thus, pure anatase nanoparticles were obtained without annealing.

Figure 1c shows that the sample produced in alkaline pH 12 has an XRD pattern of a not well crystallized rutile phase. By increasing the reaction temperature and time, the obtained anatase samples presented a much better crystallization. The line width of the diffraction peaks suggests that the obtained anatase TiO₂ is nanometric because the peaks are very large.

An estimation of the average crystalline size (*D*) of anatase phase TiO₂ particles can be made by using the well-known Scherrer equation, $D = k\lambda/B \cos\theta$, where *k* is the constant related to the shape of the crystallites and the indices of the reflecting plane (anatase 101 diffraction peak). Based on Scherrer's equation, we calculated, as shown in Figure 1a, 1b and 1c, the average sizes of the anatase nanoparticles, thus obtaining 7.0, 7.5 and 6.1 nm for samples prepared at 80, 90 and 100 °C, respectively. The average sizes of the particles synthesized by varying the reaction time and pH were also calculated, thus giving 7.8, 7.4, 9.3 and 13.1 nm for samples heated during 6, 12, 24 and 74h and 35, 10 and 22 nm for samples prepared at pH equal to 2, 7 and 12, respectively.

Figure 2 shows that TiO₂ nanoparticles remained in the anatase phase up to about 700 °C; after this temperature, a transition phase to rutile was initialized. The anatase nanoparticle average sizes were calculated, based on Scherrer's equation, for each calcination temperature (see Table 1).

The morphology and average size of some synthesized pure nanocrystalline anatase TiO₂ were investigated in detail by transmission electron microscopy (TEM) as a function of the reaction parameter. Figure 3 shows the TEM micrograph of the anatase TiO₂ samples prepared at 100 °C by solvothermal treatment for 72h. The TEM images of the samples show an irregular spherical shape. The average diameter of the nanocrystals was estimated by inspection to be about 8.8 nm, as shown in the inset of Figure 3 below.

In order to further characterize the crystalline phase and sizes of the TiO₂ samples, Raman measurements were performed. Before discussing the Raman spectra of the TiO₂ nanocrystals, we briefly recall the vibrational properties of bulk anatase and rutile TiO₂. The anatase (rutile) phase is tetragonal with two formulas per unit cell, belonging to the space group *D*_{4h}¹⁹ (*D*_{4h}¹⁴). Standard group theory analysis suggests that the Raman active modes are distributed into the irreducible representations as *A*_{1g}+2*B*_{1g}+3*E*_g and *A*_{1g}+*B*_{1g}+*B*_{2g}+*E*_g for anatase and rutile, respectively.¹⁸ The spectral signatures of anatase and rutile are distinct and Raman spectroscopy can be used for

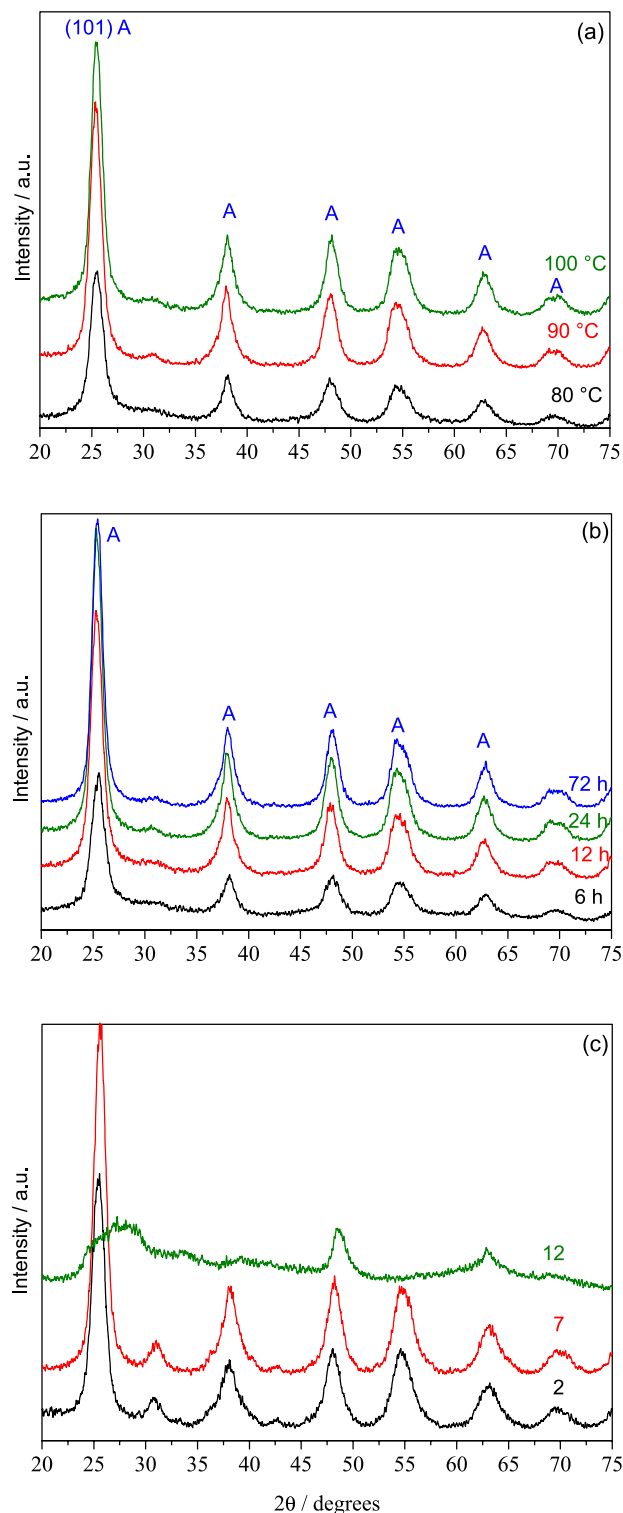


Figure 1. X-ray diffraction patterns recorded for TiO₂ samples prepared with different reaction (a) temperatures (80, 90 and 100 °C for 72h), (b) times (6, 12, 24 and 72h at 100 °C) and (c) pHs (2.0, 7.0 and 12 at 100 °C for 72h)

unambiguously identifying them. The Raman spectrum recorded for TiO₂ samples obtained with variable parameters (Figure 4a and 4b) clearly shows a strong band at about

Table 1. Average crystallite sizes (d_{XRD}) of calcined TiO₂ nanocrystals determined by the use of Scherrer's equation applied to the anatase (101) diffraction peak. The sample powders were produced by solvothermal reaction for 72h at 100 °C

T / °C	100	200	300	400	450	500	600	700
d_{XRD} / nm	6.1	6.6	–	8.5	9.4	11.4	bulk	bulk

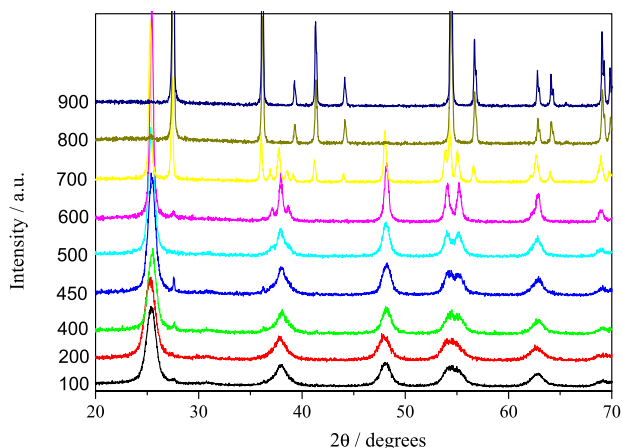


Figure 2. XRD patterns of TiO₂ samples submitted to calcination. The sample powders were produced by solvothermal reaction for 72h at 100 °C.

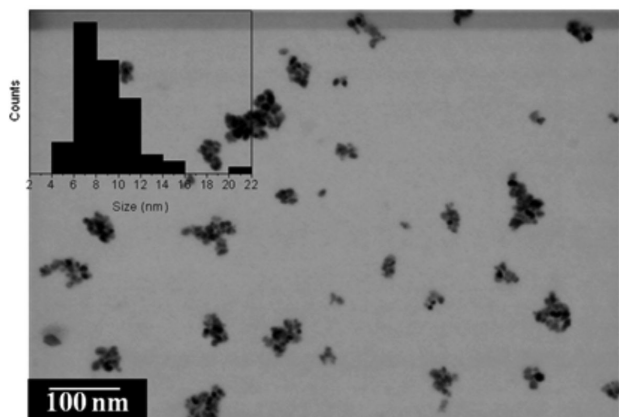


Figure 3. TEM image of TiO₂ nanocrystals obtained by solvothermal method at 100 °C and 72h of reaction. The inset shows the size dispersion curve.

143 cm⁻¹ and four other bands at 197, 399, 513 and 639 cm⁻¹, which are from the optical vibration modes belonging to the E_g(ν₆), E_g(ν₅), B_{1g}(ν₄), A_{1g}+B_{1g}(ν₃+ν₂) and Eg(ν₁) irreducible representations.¹⁵ These spectra can be assigned to the anatase phase without the presence of the rutile or brookite phases,¹⁶ in agreement with the XRD analysis. The two most intense peaks located at about 143 and 639 cm⁻¹ are the spectral signatures of anatase. However, the TiO₂ sample produced in alkaline pH 12 shows (see Figure 4c) that the predominant phase is rutile, since the most intense modes are located at 451 and 615 cm⁻¹.¹⁵

It is clear that the vibrational mode features (wavenumber, peak width and relative intensity) associated

with the modes assigned to TiO₂ nanocrystals do change as a function of reaction parameters. The lowest frequency E_g mode experiences an upshift and becomes broader as the reaction time, temperature and pH decrease (see the inset to Figures 4a, 4b and 4c), for example as the nanocrystal size decreases. This is a size-induced phenomena observed in nanocrystals and it has been described based on a phonon confinement model.¹⁷ The lack of long-range order in nanocrystals breaks down the q=0 selection rule valid for a first-order Raman scattering. Broad and asymmetric modes are observed because phonons with q ≠ 0 are also allowed to contribute to the Raman profile.

The Raman profile is not a Lorentzian curve and it depends on the nanocrystal size. The model used for fitting the Raman profile yields the following Equation 1:

$$I(\omega) \propto \int_{BZ} \frac{|C(0,q)|^2 d^3q}{[\omega - \omega(q)]^2 + \left(\frac{\Gamma_0}{2}\right)^2} \quad (1)$$

where Γ_0 is the linewidth of the Raman peak and $\omega(q)$ is the phonon dispersion curve. For spherical nanocrystals, the equation is: $|C(0,q)|^2 = \exp\left(-\frac{q^2 d^2}{16\pi^2}\right)$, where d stands for the nanocrystal diameter.¹⁷ The integration in Equation 1 is performed over the Brillouin zone of bulk TiO₂. The phonon confinement is evident for the lowest frequency E_g mode located at about $\omega_0 = 143$ cm⁻¹ for bulk anatase TiO₂ in this work. For simplicity, we approximated the phonon dispersion of this mode using a linear chain model, e.g., (18) $\omega(q) = \omega_0 + 28[1 - \cos(0.3768q)]$.¹⁹ As the nanocrystal size gets smaller the phonon confinement involves large q values and the maximum of the Raman peak follows the same trend for $\omega(q)$ that is positive in the case of the E_g mode for bulk anatase TiO₂.

In Figure 5 we plot the Raman profile of the E_g mode according to Equation 1 for 12 (dashed line), 8.3 (solid line) and 5 nm (dotted line) diameters and considering $\Gamma_0 = 16$ cm⁻¹. The experimental data (solid circles) for the sample obtained at 100 °C for 72h were best described by the solid line in which the nanocrystal size was estimated to be 8.3 nm. We can see that the size estimated by the Raman measurement is in better agreement with the TEM image than with that estimated by XRD (not shown here). By adjusting the experimental data for the other samples we have obtained the nanocrystal diameter as a function of

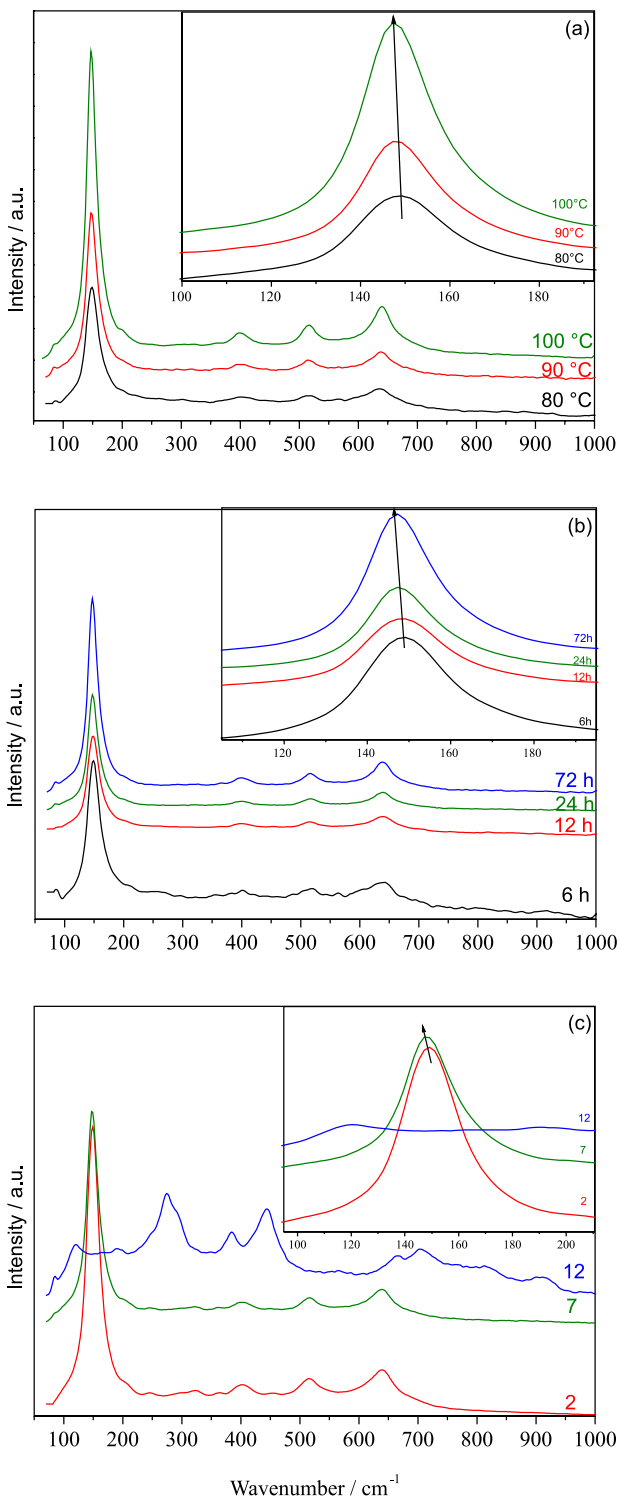


Figure 4. Raman spectra of TiO_2 samples recorded with different reaction (a) temperature (b) time and (c) pH. The inset shows the shift of the E_g mode at 145 cm^{-1} as a function of nanocrystal sizes, which in turn depend on the reaction parameters.

the reaction time, temperature and pH. The obtained results are shown in Figure 6. It can be seen in Figure 6a that the decreasing reaction temperature promotes the reduction

of the TiO_2 nanoparticles average sizes. Moreover, in Figure 6b, the decreasing reaction time also promotes the TiO_2 nanoparticle size decrease. Regarding the reaction pH, which is controlled by addition of either HCl or NaOH, we produced anatase nanoparticles in pH 2 and 7 with 7.5 and 7.9 nm grain sizes, respectively. The estimate of the TiO_2 nanocrystal diameter through Raman spectroscopy is important because this method is fast and it is not necessary to prepare the TiO_2 nanocrystals for analysis. Based on the average sizes obtained by the Raman measurements, we can state that the mechanisms of crystal growth are influenced by the reaction parameters and presence of hydrogen peroxide. In the presence of H_2O_2 , the starting material is titanium peroxide, the OH^- concentration around Ti^{4+} decreases, and the nucleation rate of $\text{Ti}(\text{OH})_x$ slows down.

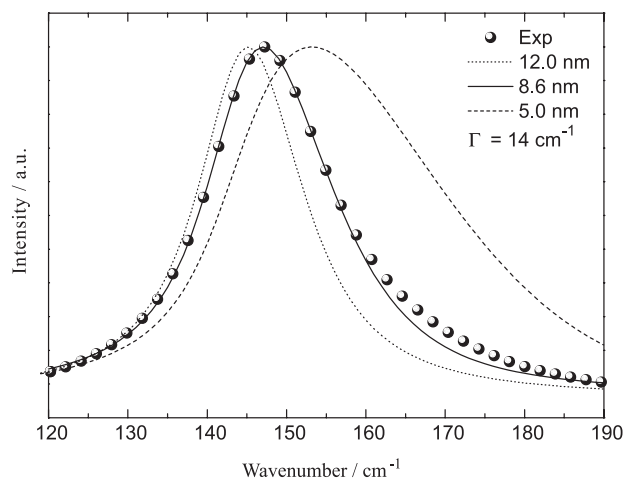


Figure 5. Size dependent Raman scattering profile of the lowest frequency E_g mode. The solid points stand for the experimental data resulting from the sample obtained after treatment at $100 \text{ }^\circ\text{C}$ for 72h. The dashed, solid and dotted lines were obtained by plotting Equation 1 for nanocrystal diameters of 12.0, 8.3 and 5.0 nm, respectively. The line width used was 14 cm^{-1} .

Figure 7 shows the Raman spectra of calcined samples. We can observe that TiO_2 nanoparticles remained in the anatase phase up to about $700 \text{ }^\circ\text{C}$. After this temperature, a transition phase to rutile occurred, confirmed by XRD measurements (as shown above). The narrowing and red shift of the E_g peak with rising calcination temperatures may show that the increasing size of the anatase nanoparticles is promoted by calcination. Based on the phonon confinement model, the anatase nanoparticle average sizes were calculated for each calcination temperature (see Table 2) up to the anatase-rutile transition phase. Sample calcination promoted the coalescence of the anatase nanoparticles that led to increasing grain sizes.

The discrepancies between the nanocrystal sizes obtained by TEM, Raman, and X-ray diffractometry are inherent to the different phenomena involved in these techniques (Table S1).

Table 2. Calcined TiO₂ nanocrystal average sizes (d_{Raman}) calculated from the phonon confinement model by fitting the E_g Raman mode. Sample powders were produced by solvothermal reaction for 72h at 100 °C

T / °C	100	200	300	400	450	500	600	700
d_{Raman} / nm	8.6	8.8	9.8	12.2	13.4	15.3	bulk	bulk

The changes in lattice parameters and different strain levels along the nanoparticle induce small changes in position and

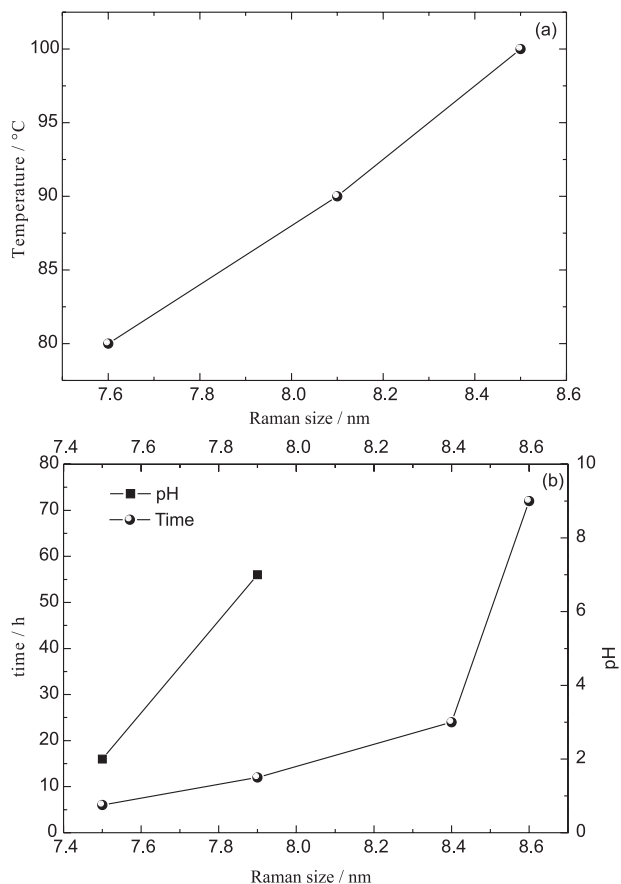


Figure 6. TiO₂ nanocrystal sizes as a function of the reaction parameters as obtained from Raman data.

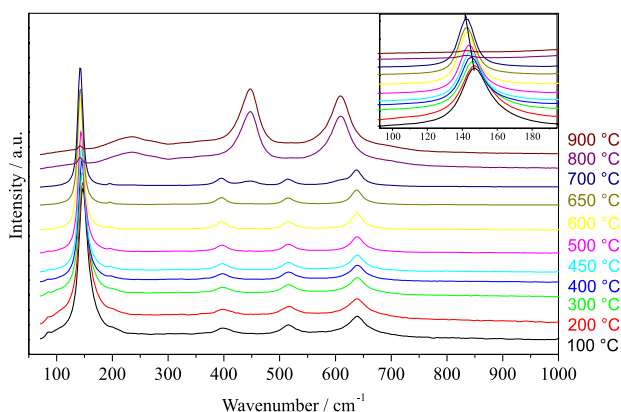


Figure 7. Raman spectra of TiO₂ samples submitted to calcination. Sample powders were produced by solvothermal reaction for 72h at 100 °C. The inset shows the wavenumber red shift as a function of calcination temperature.

also broaden the peak, which in turn affects the estimation of the nanocrystal size decrease. The direct observation of the nanoparticle by TEM is the most effective method for determining the average nanoparticle size, but the cost and availability of the TEM equipment and the agglomeration of particles can prevent its appropriate use and causes contrast at the interfaces, preventing their direct observation and a precise analysis of their size. Thus, estimates of anatase nanocrystal size using Raman spectroscopy are useful and the results obtained regarding the nanocrystal sizes should be interpreted as being values close to the true average diameter size of the particle distribution. Also, the differences in the values are much smaller than the width of the TEM particle size distribution.

Conclusions

Summarizing, this study reports on the structural and vibrational properties of TiO₂ nanocrystals synthesized by a solvothermal method with different reaction parameters and using H₂O₂ in the solution. X-ray diffraction and transmission electron microscopy analyses were employed as structural characterization tools and revealed that TiO₂ nanocrystals were grown in the anatase phase. The nanocrystal sizes exhibited a linear behavior as a function of the increasing values of the reaction parameters. Both softening and broadening of the Raman modes confirmed the very small size of the TiO₂ nanocrystals. A dependence of the Raman peak wavenumber on the TiO₂ nanocrystal diameter was observed, which can be used as a prompt characterization tool for estimating average nanocrystal sizes. This observation is also supported by TEM micrograph evidence. The presence of the H₂O₂ in the solvothermal reaction mixture produces anatase TiO₂ nanoparticles with uniform and smaller size due to its role as a retardant of grain size increase at a low cost. During the crystallization process, the nucleation rate of TiO₂ is increased because the presence of peroxides can inhibit the hydrolysis of the titanium ions in solution. As a result, uniformly shaped anatase particles with nanometric grain sizes smaller than those obtained in the absence of H₂O₂ were produced.

Supplementary Information

Supplementary information (Table S1) is available free of charge at <http://jbcs.sbg.org.br> as a PDF file.

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