

Supplementary Information

Bursting in the Belousov-Zhabotinsky Reaction Added with Phenol in a Batch Reactor

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Table S1. Species nomenclature and initial concentrations used for the simulation of the BZ reaction added with phenol

Specie representation	Initial concentration used for simulations / (mol L ⁻¹)	Specie name	Mechanism
c(1)	0	Br ⁻	MBM and GVKFR
c(2)	0	HOBr	MBM and GVKFR
c(3)	1.29	H ⁺	MBM and GVKFR
c(4)	0	Br ₂	MBM and GVKFR
c(5)	0	HBrO ₂	MBM and GVKFR
c(6)	2.8896 × 10 ⁻²	BrO ₃ ⁻	MBM and GVKFR
c(7)	0	H ₂ BrO ₂ ⁺	MBM and GVKFR
c(8)	0	Br ₂ O ₄	MBM and GVKFR
c(9)	0	BrO ₂ [*]	MBM and GVKFR
c(10)	0	Ce ⁺³	MBM
c(11)	5.606 × 10 ⁻⁴	Ce ⁺⁴	MBM
c(12)	0	O ₂	MBM
c(13)	0	BrMA ^b	MBM
c(14)	0	BrMA ^{*b}	MBM
c(15)	0	BrEETRA ^b	MBM
c(16)	0	CO ₂	MBM
c(17)	0	BrMA(enol) ^b	MBM
c(18)	0	Br ₂ MA ^b	MBM
c(19)	0	BrMABrO ₂ ^b	MBM
c(20)	0	OA ^b	MBM
c(21)	0	BrTA ^b	MBM
c(22)	0	MOA ^b	MBM
c(23)	0	COOH ^{*b}	MBM
c(24)	0	MA ^{*b}	MBM
c(25)	2.6056 × 10 ⁻²	MA ^b	MBM
c(26)	0	ETA ^b	MBM

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Table S1. continuation

Specie representation	Initial concentration used for simulations / (mol L ⁻¹)	Specie name	Mechanism
c(27)	0	MA(enol) ^b	MBM
c(28)	0	MABrO ₂ ^b	MBM
c(29)	0	TA ^b	MBM
c(30)	0	EETA ^b	MBM
c(31)	0	TA* ^b	MBM
c(32)	0	EEHTRA ^b	MBM
c(33)	0	TA(enol) ^b	MBM
c(34)	0	TABrO ₂ ^b	MBM
c(35)	variable ^a	Fenol	GVKFR
c(36)	0	Fenol*	GVKFR
c(37)	0	Rox1 ^c	GVKFR
c(38)	0	RBr ^c	GVKFR
c(39)	0	RBr ₂ ^c	GVKFR
c(40)	0	RBr* ^c	GVKFR
c(41)	0	R(BrOH) ^c	GVKFR
c(42)	0	Rox2 ^c	GVKFR
c(43)	0	OQN ^c	GVKFR
c(44)	0	RBr ₂ * ^c	GVKFR
c(45)	0	RBr(BrOH) ^c	GVKFR
c(46)	0	Rox3 ^c	GVKFR
c(47)	0	BrOQN ^c	GVKFR
c(48)	0	Rox4 ^c	GVKFR
c(49)	0	<i>p</i> -hydroxyphenol	proposed in this work
c(50)	0	<i>p</i> -hydroxyphenol radical	proposed in this work
c(51)	0	<i>p</i> -quinone	proposed in this work

^aEveryone of the 18 experimental concentrations of phenol was used here. ^bThe nomenclature use in references 32 of the paper was used. ^cThe nomenclature use in references 33 of the paper was used.

Table S2. The complete set of reaction rates used for the simulation of the bursting phenomena in the BZ reaction added with phenol. The numerical values are the respective kinetic constants. The negative sign precedes the reverse reaction when the reverse kinetic constant is different to zero

Reaction	Reaction rate	Mechanism
V(1)	$8 \times 10^9 c(1) c(2) c(3) - 110 c(4)$	MBM and GVKFR
V(2)	$2.9 \times 10^6 c(1) c(5) c(3) - 2 \times 10^5 c(2) c(2)$	MBM and GVKFR
V(3)	$0.6 c(1) c(6) c(3) c(3) - 3.2 c(2) c(5)$	MBM and GVKFR
V(4)	$2 \times 10^6 c(5) c(3) - 1.0 \times 10^8 c(7)$	MBM and GVKFR
V(5)	$1.7 \times 10^5 c(5) c(7)$	MBM and GVKFR
V(6)	$48 c(5) c(6) c(3) - 3.2 \times 10^3 c(8)$	MBM and GVKFR
V(7)	$7.5 \times 10^4 c(8) - 1.4 \times 10^9 c(9) c(9)$	MBM
V(8)	$6 \times 10^4 c(10) c(9) c(3) - 1.3 \times 10^4 c(11) c(5)$	MBM
V(9)	$6 \times 10^{-10} c(6) c(6) c(3) c(3)$	MBM
V(10)	$0.06 c(9)$	MBM
V(11)	$0.1 c(13) c(11) - 400 c(14) c(10) c(3)$	MBM
V(12)	$1 \times 10^9 c(14) c(14)$	MBM
V(13)	$1.2 \times 10^{-2} c(13) - 800 c(17)$	MBM
V(14)	$3.5 \times 10^6 c(17) c(4)$	MBM
V(15)	$1.1 \times 10^6 c(17) c(2)$	MBM
V(16)	$2 \times 10^9 c(14) c(9)$	MBM
V(17)	$0.62 c(19)$	MBM
V(18)	$0.46 c(19)$	MBM
V(19)	$1.5 c(21)$	MBM
V(20)	$7 \times 10^3 c(22) c(11)$	MBM
V(21)	$28 c(20) c(11)$	MBM
V(22)	$5 \times 10^9 c(23) c(23)$	MBM
V(23)	$1 \times 10^{97} c(23) c(11)$	MBM
V(24)	$0.6 \times 10^6 c(23) c(13)$	MBM
V(25)	$3 \times 10^9 c(23) c(14)$	MBM
V(26)	$5 \times 10^9 c(23) c(9)$	MBM
V(27)	$0.23 c(25) c(11) - 2.2 \times 10^4 c(24) c(10) c(3)$	MBM
V(28)	$3.2 \times 10^9 c(24) c(24)$	MBM
V(29)	$2.6 \times 10^{-3} c(25) - 180 c(27)$	MBM
V(30)	$2 \times 10^6 c(27) c(4)$	MBM
V(31)	$6.7 \times 10^5 c(27) c(2)$	MBM
V(32)	$5 \times 10^9 c(24) c(9)$	MBM
V(33)	$0.55 c(28)$	MBM
V(34)	$1.0 c(28)$	MBM
V(35)	$2 \times 10^9 c(24) c(14)$	MBM
V(36)	$4 \times 10^9 c(24) c(23)$	MBM
V(37)	$0.66 c(29) c(11) - 1.7 \times 10^4 c(31) c(10) c(3)$	MBM
V(38)	$1 \times 10^9 c(31) c(31)$	MBM
V(39)	$2.3 \times 10^{-5} c(29) - 1.5 c(33)$	MBM
V(40)	$3 \times 10^5 c(33) c(4)$	MBM
V(41)	$2 \times 10^5 c(33) c(2)$	MBM
V(42)	$1 \times 10^9 c(31) c(24)$	MBM
V(43)	$1 \times 10^9 c(31) c(14)$	MBM

Table S2. continuation

Reaction	Reaction rate	Mechanism
V(44)	$3 \times 10^9 c(31) c(23)$	MBM
V(45)	$2 \times 10^9 c(31) c(9)$	MBM
V(46)	$0.1 c(34)$	MBM
V(47)	$5 \times 10^{-5} c(29) c(6)$	MBM
V(48)	$160 c(24) c(6) c(3)$	MBM
V(49)	$1 \times 10^{-2} c(35) c(6) c(3)$	GVKFR
V(50)	$1 \times 10^4 c(35) c(9)$	GVKFR
V(51)	$1 \times 10^4 c(36) c(6) c(3)$	GVKFR
V(52)	$6 \times 10^5 c(35) c(4)$	GVKFR
V(53)	$2 \times 10^3 c(38) c(4)$	GVKFR
V(54)	$1 \times 10^4 c(38) c(9)$	GVKFR
V(55)	$1 \times 10^4 c(40) c(6) c(3)$	GVKFR
V(56)	$1 \times 10^4 c(40) c(6) c(3)$	GVKFR
V(57)	$2 \times 10^{-1} c(41)$	GVKFR
V(58)	$1 \times 10^4 c(39) c(9)$	GVKFR
V(59)	$1 \times 10^4 c(44) c(6) c(3)$	GVKFR
V(60)	$2.5 \times 10^3 c(44) c(6) c(3)$	GVKFR
V(61)	$2 \times 10^{-1} c(45)$	GVKFR
V(62)	$1 \times 10^2 c(4) c(37)$	GVKFR
V(63)	$1 \times 10^3 c(11) c(35) - 4 \times 10^4 c(10) c(36) c(3)$	our proposal
V(64)	$1 \times 10^4 c(36) c(11)$	our proposal
V(65)	$1 \times 10^3 c(49) c(11) - 4 \times 10^4 c(50) c(10) c(3)$	our proposal
V(66)	$1 \times 10^4 c(50) c(11)$	our proposal
V(67)	$1 \times 10^6 c(51) c(23)$	our proposal
V(68)	$1 \times 10^8 c(50) c(23)$	our proposal
V(69)	$1 \times 10^6 c(51) c(31)$	our proposal
V(70)	$1 \times 10^7 c(50) c(31)$	our proposal
V(71)	$1 \times 10^0 c(28)$	MBM, called NR5
V(72)	$1 \times 10^5 c(51)$	our proposal

All variables used in the computer program were double precision, and the tolerance for the convergence of the algorithm was set to 1×10^{-10} . Others tolerances were tested

but few changes were found and no more detailed studies were try respect to this parameter.

Source code

```

!Revisado septiembre 17 de 2013.
  Program BarridoFenol
  Implicit none
  DOUBLE PRECISION CFenol
  Integer contador
! Do contador=1,18,1
!   If (contador .EQ. 1) then; CFenol=0D0; end if
!   If (contador .EQ. 2) then; CFenol=5.347D-5; end if
!   If (contador .EQ. 3) then; CFenol=1.337D-4; end if
!   If (contador .EQ. 4) then; CFenol=2.673D-4; end if
!   If (contador .EQ. 5) then; CFenol=5.347D-4; end if
!   If (contador .EQ. 6) then; CFenol=1.069D-3; end if
!   If (contador .EQ. 7) then; CFenol=1.337D-3; end if
!   If (contador .EQ. 8) then; CFenol=1.604D-3; end if
!   If (contador .EQ. 9) then; CFenol=1.871D-2; end if
!   If (contador .EQ. 10) then; CFenol=2.272D-2; end if
!   If (contador .EQ. 11) then; CFenol=2.673D-2; end if
!   If (contador .EQ. 12) then; CFenol=3.074D-2; end if
!   If (contador .EQ. 13) then; CFenol=3.476D-2; end if
!   If (contador .EQ. 14) then; CFenol=3.877D-2; end if
!   If (contador .EQ. 15) then; CFenol=4.278D-2; end if
!   If (contador .EQ. 16) then; CFenol=4.679D-2; end if
!   If (contador .EQ. 17) then; CFenol=5.347D-2; end if
!   If (contador .EQ. 18) then; CFenol=1.069D-1; end if
  contador=18 ! The variable "contador" must be change from 1 to 18 to choose one of the experimental
concentrations of phenol used.
  If (contador .EQ. 1) then; CFenol=0D0; end if
  If (contador .EQ. 2) then; CFenol=5.347D-5; end if
  If (contador .EQ. 3) then; CFenol=1.337D-4; end if
  If (contador .EQ. 4) then; CFenol=2.673D-4; end if
  If (contador .EQ. 5) then; CFenol=5.347D-4; end if
  If (contador .EQ. 6) then; CFenol=1.069D-3; end if
  If (contador .EQ. 7) then; CFenol=1.337D-3; end if
  If (contador .EQ. 8) then; CFenol=1.604D-3; end if
  If (contador .EQ. 9) then; CFenol=1.871D-2; end if
  If (contador .EQ. 10) then; CFenol=2.272D-2; end if
  If (contador .EQ. 11) then; CFenol=2.673D-2; end if
  If (contador .EQ. 12) then; CFenol=3.074D-2; end if
  If (contador .EQ. 13) then; CFenol=3.476D-2; end if
  If (contador .EQ. 14) then; CFenol=3.877D-2; end if
  If (contador .EQ. 15) then; CFenol=4.278D-2; end if
  If (contador .EQ. 16) then; CFenol=4.679D-2; end if
  If (contador .EQ. 17) then; CFenol=5.347D-2; end if
  If (contador .EQ. 18) then; CFenol=1.069D-1; end if
  write(*,*) "Contador = ",contador,"CFenol = ", CFenol
!   call sleep(1)
  call MBMReGVKFR(contador,CFenol)
!   write(*,*) "CFenol = ", CFenol
!   call sleep(1)
! End Do
end Program BarridoFenol

Subroutine MBMReGVKFR(contador,CFenol)
  Implicit none
  EXTERNAL F, Jac
  DOUBLE PRECISION ATOL, RWORK, RTOL, T, Tmax, TOUT, c, Delta, Hmax,
+Max_step, CFenol
  Integer neq, ITOL, ITASK, ISTATE, IOPT, LRW, LIW, MF, LPR, IWORK, I, contador
  DIMENSION c(51), RWORK(3100), IWORK(100)
  character*19 grafife
  Character*1 ContadorArchivo1
  Character*2 ContadorArchivo2

c 15 format(A70)

```

```

C write(*,20)
C 20 format(2x,'Archivo para los datos de integracion: `)
C read(*,15) grafifle

If (contador .LT. 10) then
write(ContadorArchivo1,'(I1)') contador !convierte entero a caracter
! ContadorArchivo=trim(ContadorArchivo) !Quita los espacios en blanco
grafifle="Ago-26-2013-"/trim(ContadorArchivo)///.txt"
else
write(ContadorArchivo2,'(I2)') contador
grafifle="Ago-26-2013-"/trim(ContadorArchivo2)///.txt"
End if

C Aqui se especifica el número de ecuaciones diferenciales ODES
neq=51
C *** !Estos datos son los que debe leer la subrutina, o se le deben dar

C WRITE(*,*) `Entre el tiempo total de la simulación: `
C READ(*,*) Tmax
C WRITE(*,*) `Entre el intervalo del tiempo: `
C READ(*,*) Delta

Tmax=2D6 !4D4 !4D5 !2D6
Delta=40D0

C Concentraciones Iniciales de cada especie
C WRITE(*,*) `Entre la concentración inicial 1: `
C read(*,*) c(1)
C WRITE(*,*) `Entre la concentración inicial 2: `
C read(*,*) c(2)

c(1)=0.00000001 ! c(1)= Br-
c(2)=0.0 ! c(2)= HOBr
c(3)=1.29 ! c(3)= H+
c(4)=0.0 ! c(4)= Br2
c(5)=0.0 ! c(5)= HBrO2
c(6)=2.8896D-2 ! Concentraci≤n Ariel !MBM articulo concentraci≤n 0.15D0 ! c(6)= BrO3-
c(7)=0.0 ! c(7)= H2BrO2+
c(8)=0.0 ! c(8)= Br2O4
c(9)=0.0 ! c(9)= BrO2*
c(10)=0.0 ! c(10)= Ce+3
c(11)=5.606D-4 ! Concentraci≤n Ariel !MBM articulo concentracion 3.56D-4 ! c(11)=
Ce+4
c(12)=0.0 ! c(12)= O2
c(13)=0.0 ! c(13)= BrMA
c(14)=0.0 ! c(14)= BrMA*
c(15)=0.0 ! c(15)= BrEETRA
c(16)=0.0 ! c(16)= CO2
c(17)=0.0 ! c(17)= BrMA(enol)
c(18)=0.0 ! c(18)= Br2MA
c(19)=0.0 ! c(19)= BrMABrO2
c(20)=0.0 ! c(20)= OA
c(21)=0.0 ! c(21)= BrTA
c(22)=0.0 ! c(22)= MOA
c(23)=0.0 ! c(23)= COOH*
c(24)=0.0 ! c(24)= MA*
c(25)=2.6056D-2 ! Concentraci≤n Ariel !MBM articulo concentraci≤n 5D-2 ! c(25)=
MA
c(26)=0.0 ! c(26)= ETA
c(27)=0.0 ! c(27)= MA(enol)
c(28)=0.0 ! c(28)= MABrO2
c(29)=0.0 ! c(29)= TA
c(30)=0.0 ! c(30)= EETA
c(31)=0.0 ! c(31)= TA*
c(32)=0.0 ! c(32)= EEHTRA
c(33)=0.0 ! c(33)= TA(enol)
c(34)=0.0 ! c(34)= TABrO2

```

```

! *** Desde aquí se suman las reacciones del mecanismo GVKFR ***
c(35)=CFenol          ! GVKFR: c(7)= R          Fenol          H2BrO2+
c(36)=0.0D0          ! GVKFR: c(8)= R*          Fenol* = H-*Fenol=0 Br2O4
c(37)=0.0D0          ! GVKFR: c(10)= Rox1       HO-HFenol=0          Ce+3
c(38)=0.0D0          ! GVKFR: c(11)= RBr        Br*                   Ce+4
c(39)=0.0D0          ! GVKFR: c(12)= RBr2 O=Fenol*-OH = *O-Fenol-OH O2
c(40)=0.0D0          ! GVKFR: c(13)= RBr*       O=Fenol=0            BrMA
c(41)=0.0D0          ! GVKFR: c(14)= R(BrOH)    HO-Fenol-OH          BrMA*
c(42)=0.0D0          ! GVKFR: c(15)= Rox2       HO-Fenol-Br          BrEETRA
c(43)=0.0D0          ! GVKFR: c(16)= OQN        (Fenol-O)2           CO2
c(44)=0.0D0          ! GVKFR: c(17)= RBr2*                                BrMA(enol)
c(45)=0.0D0          ! GVKFR: c(18)= RBr(BrOH)                                Br2MA
c(46)=0.0D0          ! GVKFR: c(19)= Rox3                                BrMABrO2
c(47)=0.0D0          ! GVKFR: c(20)= BrOQN                                OA
c(48)=0.0D0          ! GVKFR: c(21)= Rox4                                BrTA

! *** Las especies de las interreacciones
c(49)=0.0D0          ! Ariel: p-Hidroxyphenol
c(50)=0.0D0          ! Ariel: p-Hidroxyphenol radical
c(51)=0.0D0          ! Ariel: p-Quinone

!      write(*,*) "cs = ", (c(I), I=1, neq)

open(9, file = grafile, status='replace')

Hmax= 10D0           ! Maximun step size
Max_step= 1000000D0

TOUT = 0D0
ITOL = 1
RTOL = 1.D-10      !tol      : Error tolerance
ATOL = 1.D-10      !wlimit : Error control limit
ITASK = 1
ISTATE = 1
IOPT = 1
LRW = 3100
LIW = 100
MF = 22 !, por LSODE suministra el jacobiano full
C Input options
Do lpr=5,10
  rwork(lpr)=0
iwork(lpr)=0
End Do
C rwork(5)=H !h0
rwork(6)=Hmax
iwork(6)=Max_step
Do While (Tout .LE. Tmax) !Del ciclo de integracion DLSODE
  CALL DLSODE(F,NEQ,c,T,TOUT,ITOL,RTOL,ATOL,ITASK,ISTATE,
+ IOPT,RWORK,LRW,IWORK,LIW,Jac,MF)
! WRITE(6,32) T,c(1),c(2)
! 32 FORMAT(7H En T =,E12.4,7H c(1) =,E14.6,7H c(2) =,E14.6)

  WRITE(9,34) T,((c(I)), I=1, neq)
34 FORMAT(52(1PE13.5))
  IF (ISTATE .LT. 0) Then
  WRITE(6,90) ISTATE
90 FORMAT(///22H ERROR HALT.. ISTATE =,I3)
  close(9)
  STOP
  End If

  TOUT = TOUT + delta
End Do !fin Del ciclo de integracion DLSODE *****
WRITE(6,60) IWORK(11),IWORK(12),IWORK(13)
60 FORMAT(/12H NO. STEPS =,I4,11H NO. F-S =,I4,11H NO. J-S =,I4)
close(9)

```

```

END Subroutine MBMReGVKFR
C*****
SUBROUTINE F (NEQ, T, c, YDOT)
  DOUBLE PRECISION T, c, YDOT, V
  DIMENSION c(51), YDOT(51), V(72)
  Integer especie
! *** Para controlar los posibles valores negativos de GVKFR R=c(7) y R*=c(8)
Do especie=1, 51, 1
  IF ( c(especie) < 1D-14 ) Then
    c(especie)=0D0 !; write (*,*), 'Se acabo el reactivo. c(7) =', c(7)
  END IF
End Do
  V(1)= 8d+9*c(1)*c(2)*c(3)-110*c(4)
  V(2)= 2.9d+6*c(1)*c(5)*c(3)-2d-5*c(2)*c(2)
  V(3)= 0.6*c(1)*c(6)*c(3)*c(3)-3.2*c(2)*c(5)
  V(4)= 2d+6*c(5)*c(3)-1.0d+8*c(7)
  V(5)= 1.7d+5*c(5)*c(7)
  V(6)= 48*c(5)*c(6)*c(3)-3.2d+3*c(8)
  V(7)= 7.5d+4*c(8)-1.4d+9*c(9)*c(9)
  V(8)= 6d+4*c(10)*c(9)*c(3)-1.3d+4*c(11)*c(5)
  V(9)= 6d-10*c(6)*c(6)*c(3)*c(3)
  V(10)= 0.06*c(9)
  V(11)= 0.1*c(13)*c(11)-400*c(14)*c(10)*c(3)
  V(12)= 1d+9*c(14)*c(14)
  V(13)= 1.2d-2*c(13)-800*c(17)
  V(14)= 3.5d+6*c(17)*c(4)
  V(15)= 1.1d+6*c(17)*c(2)
  V(16)= 2d+9*c(14)*c(9)
  V(17)= 0.62*c(19)
  V(18)= 0.46*c(19)
  V(19)= 1.5*c(21)
  V(20)= 7d+3*c(22)*c(11)
  V(21)= 28*c(20)*c(11)
  V(22)= 5d+9*c(23)*c(23)
  V(23)= 1d+7*c(23)*c(11)
  V(24)= 0.6d+6*c(23)*c(13)
  V(25)= 3d+9*c(23)*c(14)
  V(26)= 5d+9*c(23)*c(9)
  V(27)= 0.23*c(25)*c(11)-2.2d+4*c(24)*c(10)*c(3)
  V(28)= 3.2d+9*c(24)*c(24)
  V(29)= 2.6d-3*c(25)-180*c(27)
  V(30)= 2d+6*c(27)*c(4)
  V(31)= 6.7d+5*c(27)*c(2)
  V(32)= 5d+9*c(24)*c(9)
  V(33)= 0.55*c(28)
  V(34)= 1.0*c(28)
  V(35)= 2d+9*c(24)*c(14)
  V(36)= 4d+9*c(24)*c(23)
  V(37)= 0.66*c(29)*c(11)-1.7d+4*c(31)*c(10)*c(3)
  V(38)= 1d+9*c(31)*c(31)
  V(39)= 2.3d-5*c(29)-1.5*c(33)
  V(40)= 3d+5*c(33)*c(4)
  V(41)= 2d+5*c(33)*c(2)
  V(42)= 1d+9*c(31)*c(24)
  V(43)= 1d+9*c(31)*c(14)
  V(44)= 3d+9*c(31)*c(23)
  V(45)= 2d+9*c(31)*c(9)
  V(46)= 0.1*c(34)
  V(47)= 5d-5*c(29)*c(6)
  V(48)= 160*c(24)*c(6)*c(3)
! *** Desde aquí se suman las velocidades del mecanismo GVKFR ***
  V(49)= 1D-2*c(35)*c(6)*c(3)
  V(50)= 1D4*c(35)*c(9)
  V(51)= 1D4*c(36)*c(6)*c(3)
  V(52)= 6D5*c(35)*c(4)
  V(53)= 2D3*c(38)*c(4)
  V(54)= 1D4*c(38)*c(9)

```


$$\begin{aligned} V(55) &= 1D4*c(40)*c(6)*c(3) \\ V(56) &= 1D4*c(40)*c(6)*c(3) \\ V(57) &= 2D-1*c(41) \\ V(58) &= 1D4*c(39)*c(9) \\ V(59) &= 1D4*c(44)*c(6)*c(3) \\ V(60) &= 2.5D3*c(44)*c(6)*c(3) \\ V(61) &= 2D-1*c(45) \\ V(62) &= 1D2*c(4)*c(37) \end{aligned}$$

! *** Estas reacciones se adiciona, digamos inter mecanismos ***

! Se usa el formato largo, propuesto por Ariel - Ver cuaderno.

$$\begin{aligned} V(63) &= 1D3*c(11)*c(35)-4D4*c(10)*c(36)*c(3) \\ V(64) &= 1D4*c(36)*c(11) \\ V(65) &= 1D3*c(49)*c(11)-4D4*c(50)*c(10)*c(3) \\ V(66) &= 1D4*c(50)*c(11) \\ V(67) &= 1D6*c(51)*c(23) \\ V(68) &= 1D8*c(50)*c(23) \\ V(69) &= 1D6*c(51)*c(31) \\ V(70) &= 1D7*c(50)*c(31) \end{aligned}$$

! *** NR5 Revisado en la web http://www.phy.bme.hu/deps/chem_ph/Research/BZ_Simulation/Ce4+.html

$$V(71) = 1D0*c(28)$$

! *** Se adiciona una reacci3n de consumo de la quinona, para representar la desaparici3n de esta y por tanto la desaparici3n del ciclo que origina los "burst".

$$V(72) = 1D5*c(51)$$

C

$$\begin{aligned} \text{Br-} \\ \text{YDOT}(1) &= -V(1) - V(2) - V(3) + V(12) + V(14) + V(17) + V(19) + V(24) + V(30) \\ &+ V(35) + V(40) + V(52) + V(53) + V(57) + V(62) + V(71) \end{aligned}$$

C

$$\begin{aligned} \text{HOBr} \\ \text{YDOT}(2) &= -V(1) + 2*V(2) + V(3) + V(5) - V(15) + V(17) - V(31) + V(33) - V(41) \end{aligned}$$

C

$$\begin{aligned} \text{H+} \\ \text{YDOT}(3) &= -V(1) - V(2) - 2*V(3) - V(4) + 2*V(5) - V(6) - V(8) - 2*V(9) + V(11) \\ &+ V(12) + V(14) + V(17) + V(19) + V(20) + V(21) + V(23) + V(24) + V(27) + V(30) \\ &+ V(35) + V(37) + V(40) - V(48) - V(49) - V(51) + V(52) + V(53) - V(55) - V(56) \\ &+ V(57) - V(59) - V(60) + V(61) + V(62) + V(63) + V(64) + V(65) + V(66) + V(71) \end{aligned}$$

c

$$\begin{aligned} \text{Br2} \\ \text{YDOT}(4) &= V(1) + 0.5*V(10) - V(14) - V(30) - V(40) - V(52) - V(53) - V(62) \end{aligned}$$

c

$$\begin{aligned} \text{HBrO2} \\ \text{YDOT}(5) &= -V(2) + V(3) - V(4) - V(5) - V(6) + V(8) + 2*V(9) + V(18) + V(26) + V(34) \\ &+ V(46) + V(47) + V(50) + V(54) + V(58) \end{aligned}$$

c

$$\begin{aligned} \text{BrO3-} \\ \text{YDOT}(6) &= -V(3) + V(5) - V(6) - 2*V(9) - V(47) - V(48) - V(49) - V(51) - V(55) \\ &+ -V(56) - V(59) - V(60) \end{aligned}$$

c

$$\begin{aligned} \text{H2BrO2+} \\ \text{YDOT}(7) &= V(4) - V(5) \end{aligned}$$

c

$$\begin{aligned} \text{Br2O4} \\ \text{YDOT}(8) &= V(6) - V(7) \end{aligned}$$

c

$$\begin{aligned} \text{BrO2*} \\ \text{YDOT}(9) &= 2*V(7) - V(8) - V(10) - V(16) - V(26) - V(32) - V(45) + V(48) + V(49) \\ &+ -V(50) - V(54) + V(55) + V(56) - V(58) + V(59) + V(60) \end{aligned}$$

c

$$\begin{aligned} \text{Ce+3} \\ \text{YDOT}(10) &= -V(8) + V(11) + V(20) + V(21) + V(23) + V(27) + V(37) + V(63) + V(64) \\ &+ V(65) + V(66) \end{aligned}$$

c

$$\begin{aligned} \text{Ce+4} \\ \text{YDOT}(11) &= +V(8) - V(11) - V(20) - V(21) - V(23) - V(27) - V(37) - V(63) - V(64) \\ &+ -V(65) - V(66) \end{aligned}$$

```
c      O2
YDOT(12)=V(9)+V(10)      !!!!Solo se acumula

c      BrMA
YDOT(13)=-V(11)-V(13)-V(24)+V(25)+V(30)+V(31)

c      BrMA*
YDOT(14)=V(11)-2*V(12)-V(16)-V(25)-V(35)-V(43)

c      BrEETRA
YDOT(15)=V(12)+V(43)      !!!!Solo se acumula

c      CO2
YDOT(16)=V(12)+V(17)+V(21)+V(23)+V(24)+V(25)+V(26)+V(36)+V(38)
++V(43)+V(44)+V(67)+V(68)+V(71)      !!!!Solo se acumula

c      BrMA(enol)
YDOT(17)=V(13)-V(14)-V(15)

c      Br2MA
YDOT(18)=V(14)+V(15)      !!!!Solo se acumula

c      BrMABrO2
YDOT(19)=V(16)-V(17)-V(18)

c      OA
YDOT(20)=V(17)+V(20)-V(21)+V(22)+V(71)

c      BrTA
YDOT(21)=V(18)-V(19)+V(40)+V(41)

c      MOA
YDOT(22)=V(19)-V(20)+V(33)+V(46)+V(47)+V(69)+V(70)

c      COOH*
YDOT(23)=V(20)+V(21)-2D0*V(22)-V(23)-V(24)-V(25)-V(26)-V(36)
+V(44)-V(67)-V(68)

c      MA*
YDOT(24)=V(24)+V(27)-2*V(28)-V(32)-V(35)-V(36)-V(42)-V(48)

c      MA
YDOT(25)=-V(27)-V(29)+V(36)

c      ETA
YDOT(26)=V(28)      !!!Solo se acumula

c      MA(enol)
YDOT(27)=V(29)-V(30)-V(31)

c      MABrO2
YDOT(28)=V(32)-V(33)-V(34)-V(71)

c      TA
YDOT(29)=V(34)-V(37)-V(39)+V(44)-V(47)

c      EETA
YDOT(30)=V(35)+V(42)      !!!!Solo se acumula

c      TA*
YDOT(31)=V(37)-2*V(38)-V(42)-V(43)-V(44)-V(45)-V(69)-V(70)

c      EEHTRA
YDOT(32)=V(38)      !!!!Solo se acumula

c      TA(enol)
YDOT(33)=V(39)-V(40)-V(41)
```

```

c      TAbR02
      YDOT(34)=V(45)-V(46)
! *** Desde aquí se suman las EDOs de las especies del mecanismo GVKFR
!      R      Fenol      H2BrO2+
      YDOT(35)=-V(49)-V(50)-V(52)-V(63)

!      R*      Fenol* = H-*Fenol=0      Br2O4
      YDOT(36)=V(49)+V(50)-V(51)+V(63)-V(64)

!      Rox1      HO-HFenol=0      Ce+3
      YDOT(37)=V(51)-V(62)

!      RBr      Br*      Ce+4
      YDOT(38)=V(52)-V(53)-V(54)

!      RBr2      O=Fenol*-OH = *O-Fenol-OH      O2
      YDOT(39)=V(53)-V(58)

!      RBr*      O=Fenol=0      BrMA
      YDOT(40)=V(54)-V(55)-V(56)

!      R(BrOH)      HO-Fenol-OH      BrMA*
      YDOT(41)=V(55)-V(57)

!      Rox2      HO-Fenol-Br      BrEETRA
      YDOT(42)=V(56)      !!!!Solo se acumula

!      OQN      (Fenol-O)2      CO2
      YDOT(43)=V(57)      !!!!Solo se acumula

!      RBr2*
      YDOT(44)=V(58)-V(59)-V(60)

!      RBr(BrOH)
      YDOT(45)=V(59)-V(61)

!      Rox3
      YDOT(46)=V(60)      !!!!Solo se acumula

!      BrOQN
      YDOT(47)=V(61)      !!!!Solo se acumula

!      Rox4
      YDOT(48)=V(62)      !!!!Solo se acumula
!      ROH - p-Hidroxifenol - Especie nueva
      YDOT(49)=V(64)-V(65)+V(68)+V(70)
!      p-Hidroxifenol Radical - Especie nueva
      YDOT(50)=V(65)-V(66)+V(67)-V(68)+V(69)-V(70)
!      p-Quinona - Especie nueva
      YDOT(51)=V(66)-V(67)-V(69)-V(72)
      END SUBROUTINE !F

      SUBROUTINE JAC
      END SUBROUTINE JAC
C*****
*DECK DLSODE
      SUBROUTINE DLSODE (F, NEQ, Y, T, TOUT, ITOL, RTOL, ATOL, ITASK,
1      ISTATE, IOPT, RWORK, LRW, IWORK, LIW, JAC, MF)
C***BEGIN PROLOGUE DLSODE
C***PURPOSE Livermore solver for ordinary differential equations.
C      DLSODE solves the initial-value problem for stiff or
C      nonstiff systems of first-order ODE's,
C      dy/dt = f(t,y), or, in component form,
C      dy(i)/dt = f(i) = f(i,t,y(1),y(2),...,y(N)), i=1,...,N.
C***LIBRARY MATHLIB (ODEPACK)
C***CATEGORY I1A

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C***TYPE      DOUBLE PRECISION (SLSODE-S, DLSODE-D)
C***KEYWORDS  ORDINARY DIFFERENTIAL EQUATIONS, INITIAL VALUE PROBLEM,
C              STIFF, NONSTIFF
C***AUTHOR    Hindmarsh, Alan C., (LLNL)
C              Computing and Mathematics Research Div., L-316
C              Lawrence Livermore National Laboratory
C              Livermore, CA 94550.
C***DESCRIPTION
C
C      NOTE: The DLSODE solver is not re-entrant, and so is usable on
C            the Cray multi-processor machines only if it is not used
C            in a multi-tasking environment.
C            If re-entrancy is required, use NLSODE instead.
C
C            The formats of the DLSODE and NLSODE writeups differ from
C            those of the other MATHLIB routines.
C
C            The "Usage" and "Arguments" sections treat only a subset of
C            available options, in condensed fashion. The options
C            covered and the information supplied will support most
C            standard uses of DLSODE.
C
C            For more sophisticated uses, full details on all options are
C            given in the concluding section, headed "Long Description."
C            A synopsis of the DLSODE Long Description is provided at the
C            beginning of that section; general topics covered are:
C            - Elements of the call sequence; optional input and output
C            - Optional supplemental routines in the DLSODE package
C            - internal COMMON block
C
C *Usage:
C      Communication between the user and the DLSODE package, for normal
C      situations, is summarized here. This summary describes a subset
C      of the available options. See "Long Description" for complete
C      details, including optional communication, nonstandard options,
C      and instructions for special situations.
C
C      A sample program is given in the "Examples" section.
C
C      Refer to the argument descriptions for the definitions of the
C      quantities that appear in the following sample declarations.
C
C      For MF = 10,
C          PARAMETER (LRW = 20 + 16*NEQ,          LIW = 20)
C      For MF = 21 or 22,
C          PARAMETER (LRW = 22 + 9*NEQ + NEQ**2,  LIW = 20 + NEQ)
C      For MF = 24 or 25,
C          PARAMETER (LRW = 22 + 10*NEQ + (2*ML+MU)*NEQ,
C          *          LIW = 20 + NEQ)
C
C      EXTERNAL F, JAC
C      INTEGER  NEQ, ITOL, ITASK, ISTATE, IOPT, LRW, IWORK(LIW),
C      *        LIW, MF
C      DOUBLE PRECISION Y(NEQ), T, TOUT, RTOL, ATOL(ntonol), RWORK(LRW)
C
C      CALL DLSODE (F, NEQ, Y, T, TOUT, ITOL, RTOL, ATOL, ITASK,
C      *          ISTATE, IOPT, RWORK, LRW, IWORK, LIW, JAC, MF)
C
C *Arguments:
C      F      :EXT      Name of subroutine for right-hand-side vector f.
C                  This name must be declared EXTERNAL in calling
C                  program. The form of F must be:
C
C                  SUBROUTINE F (NEQ, T, Y, YDOT)
C                  INTEGER  NEQ
C                  DOUBLE PRECISION T, Y(NEQ), YDOT(NEQ)

```

```

C           The inputs are NEQ, T, Y. F is to set
C
C           YDOT(i) = f(i,T,Y(1),Y(2),...,Y(NEQ)),
C                               i = 1, ..., NEQ .
C
C   NEQ   :IN   Number of first-order ODE's.
C
C   Y     :INOUT Array of values of the y(t) vector, of length NEQ.
C           Input: For the first call, Y should contain the
C                   values of y(t) at t = T. (Y is an input
C                   variable only if ISTATE = 1.)
C           Output: On return, Y will contain the values at the
C                   new t-value.
C
C   T     :INOUT Value of the independent variable. On return it
C                   will be the current value of t (normally TOUT).
C
C   TOUT  :IN   Next point where output is desired (.NE. T).
C
C   ITOL  :IN   1 or 2 according as ATOL (below) is a scalar or
C                   an array.
C
C   RTOL  :IN   Relative tolerance parameter (scalar).
C
C   ATOL  :IN   Absolute tolerance parameter (scalar or array).
C                   If ITOL = 1, ATOL need not be dimensioned.
C                   If ITOL = 2, ATOL must be dimensioned at least NEQ.
C
C           The estimated local error in Y(i) will be controlled
C           so as to be roughly less (in magnitude) than
C
C           EWT(i) = RTOL*ABS(Y(i)) + ATOL      if ITOL = 1, or
C           EWT(i) = RTOL*ABS(Y(i)) + ATOL(i)  if ITOL = 2.
C
C           Thus the local error test passes if, in each
C           component, either the absolute error is less than
C           ATOL (or ATOL(i)), or the relative error is less
C           than RTOL.
C
C           Use RTOL = 0.0 for pure absolute error control, and
C           use ATOL = 0.0 (or ATOL(i) = 0.0) for pure relative
C           error control. Caution: Actual (global) errors may
C           exceed these local tolerances, so choose them
C           conservatively.
C
C   ITASK :IN   Flag indicating the task DLSODE is to perform.
C           Use ITASK = 1 for normal computation of output
C           values of y at t = TOUT.
C
C   ISTATE:INOUT Index used for input and output to specify the state
C                   of the calculation.
C           Input:
C           1   This is the first call for a problem.
C           2   This is a subsequent call.
C           Output:
C           2   DLSODE was successful (otherwise, negative).
C               Note that ISTATE need not be modified after a
C               successful return.
C           -1  Excess work done on this call (perhaps wrong
C               MF).
C           -2  Excess accuracy requested (tolerances too
C               small).
C           -3  Illegal input detected (see printed message).
C           -4  Repeated error test failures (check all
C               inputs).
C           -5  Repeated convergence failures (perhaps bad
C               Jacobian supplied or wrong choice of MF or

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```

C          tolerances).
C          -6 Error weight became zero during problem
C            (solution component i vanished, and ATOL or
C            ATOL(i) = 0.).
C
C IOPT  :IN   Flag indicating whether optional inputs are used:
C            0 No.
C            1 Yes. (See "Optional inputs" under "Long
C              Description," Part 1.)
C
C RWORK :WORK Real work array of length at least:
C            20 + 16*NEQ          for MF = 10,
C            22 + 9*NEQ + NEQ**2   for MF = 21 or 22,
C            22 + 10*NEQ + (2*ML + MU)*NEQ for MF = 24 or 25.
C
C LRW   :IN   Declared length of RWORK (in user's DIMENSION
C            statement).
C
C IWORK :WORK Integer work array of length at least:
C            20          for MF = 10,
C            20 + NEQ    for MF = 21, 22, 24, or 25.
C
C
C            If MF = 24 or 25, input in IWORK(1),IWORK(2) the
C            lower and upper Jacobian half-bandwidths ML,MU.
C
C            On return, IWORK contains information that may be
C            of interest to the user:
C
C            Name  Location  Meaning
C            ----  -
C            NST   IWORK(11) Number of steps taken for the problem so
C                      far.
C            NFE   IWORK(12) Number of f evaluations for the problem
C                      so far.
C            NJE   IWORK(13) Number of Jacobian evaluations (and of
C                      matrix LU decompositions) for the problem
C                      so far.
C            NQU   IWORK(14) Method order last used (successfully).
C            LENRW IWORK(17) Length of RWORK actually required. This
C                      is defined on normal returns and on an
C                      illegal input return for insufficient
C                      storage.
C            LENIW IWORK(18) Length of IWORK actually required. This
C                      is defined on normal returns and on an
C                      illegal input return for insufficient
C                      storage.
C
C LIW   :IN   Declared length of IWORK (in user's DIMENSION
C            statement).
C
C JAC   :EXT  Name of subroutine for Jacobian matrix (MF =
C            21 or 24). If used, this name must be declared
C            EXTERNAL in calling program. If not used, pass a
C            dummy name. The form of JAC must be:
C
C            SUBROUTINE JAC (NEQ, T, Y, ML, MU, PD, NROWPD)
C            INTEGER NEQ, ML, MU, NROWPD
C            DOUBLE PRECISION T, Y(NEQ), PD(NROWPD,NEQ)
C
C            See item c, under "Description" below for more
C            information about JAC.
C
C MF    :IN   Method flag. Standard values are:
C            10 Nonstiff (Adams) method, no Jacobian used.
C            21 Stiff (BDF) method, user-supplied full Jacobian.
C            22 Stiff method, internally generated full
C                Jacobian.

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```

C          24 Stiff method, user-supplied banded Jacobian.
C          25 Stiff method, internally generated banded
C             Jacobian.
C
C *Description:
C   DLSODE solves the initial value problem for stiff or nonstiff
C   systems of first-order ODE's,
C
C       dy/dt = f(t,y) ,
C
C   or, in component form,
C
C       dy(i)/dt = f(i) = f(i,t,y(1),y(2),...,y(NEQ))
C                               (i = 1, ..., NEQ) .
C
C   DLSODE is a package based on the GEAR and GEARB packages, and on
C   the October 23, 1978, version of the tentative ODEPACK user
C   interface standard, with minor modifications.
C
C   The steps in solving such a problem are as follows.
C
C   a. First write a subroutine of the form
C
C       SUBROUTINE F (NEQ, T, Y, YDOT)
C       INTEGER NEQ
C       DOUBLE PRECISION T, Y(NEQ), YDOT(NEQ)
C
C   which supplies the vector function f by loading YDOT(i) with
C   f(i).
C
C   b. Next determine (or guess) whether or not the problem is stiff.
C   Stiffness occurs when the Jacobian matrix df/dy has an
C   eigenvalue whose real part is negative and large in magnitude
C   compared to the reciprocal of the t span of interest. If the
C   problem is nonstiff, use method flag MF = 10. If it is stiff,
C   there are four standard choices for MF, and DLSODE requires the
C   Jacobian matrix in some form. This matrix is regarded either
C   as full (MF = 21 or 22), or banded (MF = 24 or 25). In the
C   banded case, DLSODE requires two half-bandwidth parameters ML
C   and MU. These are, respectively, the widths of the lower and
C   upper parts of the band, excluding the main diagonal. Thus the
C   band consists of the locations (i,j) with
C
C       i - ML <= j <= i + MU ,
C
C   and the full bandwidth is ML + MU + 1 .
C
C   c. If the problem is stiff, you are encouraged to supply the
C   Jacobian directly (MF = 21 or 24), but if this is not feasible,
C   DLSODE will compute it internally by difference quotients (MF =
C   22 or 25). If you are supplying the Jacobian, write a
C   subroutine of the form
C
C       SUBROUTINE JAC (NEQ, T, Y, ML, MU, PD, NROWPD)
C       INTEGER NEQ, ML, MU, NROWPD
C       DOUBLE PRECISION Y, Y(NEQ), PD(NROWPD,NEQ)
C
C   which provides df/dy by loading PD as follows:
C   - For a full Jacobian (MF = 21), load PD(i,j) with df(i)/dy(j),
C     the partial derivative of f(i) with respect to y(j). (Ignore
C     the ML and MU arguments in this case.)
C   - For a banded Jacobian (MF = 24), load PD(i-j+MU+1,j) with
C     df(i)/dy(j); i.e., load the diagonal lines of df/dy into the
C     rows of PD from the top down.
C   - In either case, only nonzero elements need be loaded.
C
C   d. Write a main program that calls subroutine DLSODE once for each

```

C point at which answers are desired. This should also provide
 C for possible use of logical unit 6 for output of error messages
 C by DLSODE.

C
 C Before the first call to DLSODE, set ISTATE = 1, set Y and T to
 C the initial values, and set TOUT to the first output point. To
 C continue the integration after a successful return, simply
 C reset TOUT and call DLSODE again. No other parameters need be
 C reset.

C *Examples:

C The following is a simple example problem, with the coding needed
 C for its solution by DLSODE. The problem is from chemical kinetics,
 C and consists of the following three rate equations:

C $dy_1/dt = -.04*y_1 + 1.E4*y_2*y_3$
 C $dy_2/dt = .04*y_1 - 1.E4*y_2*y_3 - 3.E7*y_2**2$
 C $dy_3/dt = 3.E7*y_2**2$

C on the interval from $t = 0.0$ to $t = 4.E10$, with initial conditions
 C $y_1 = 1.0$, $y_2 = y_3 = 0$. The problem is stiff.

C
 C The following coding solves this problem with DLSODE, using
 C MF = 21 and printing results at $t = .4, 4., \dots, 4.E10$. It uses
 C ITOL = 2 and ATOL much smaller for y_2 than for y_1 or y_3 because y_2
 C has much smaller values. At the end of the run, statistical
 C quantities of interest are printed.

```

C      EXTERNAL  FEX, JEX
C      INTEGER  IOPT, IOUT, ISTATE, ITASK, ITOL, IWORK(23), LIW, LRW,
C      *        MF, NEQ
C      DOUBLE PRECISION  ATOL(3), RTOL, RWORK(58), T, TOUT, Y(3)
C      NEQ = 3
C      Y(1) = 1.D0
C      Y(2) = 0.D0
C      Y(3) = 0.D0
C      T = 0.D0
C      TOUT = .4D0
C      ITOL = 2
C      RTOL = 1.D-4
C      ATOL(1) = 1.D-6
C      ATOL(2) = 1.D-10
C      ATOL(3) = 1.D-6
C      ITASK = 1
C      ISTATE = 1
C      IOPT = 0
C      LRW = 58
C      LIW = 23
C      MF = 21
C      DO 40 IOUT = 1,12
C          CALL DLSODE (FEX, NEQ, Y, T, TOUT, ITOL, RTOL, ATOL, ITASK,
C      *              ISTATE, IOPT, RWORK, LRW, IWORK, LIW, JEX, MF)
C          WRITE(6,20)  T, Y(1), Y(2), Y(3)
C      20  FORMAT(' At t =',D12.4,'   y =',3D14.6)
C          IF (ISTATE .LT. 0) GO TO 80
C      40  TOUT = TOUT*10.D0
C          WRITE(6,60)  IWORK(11), IWORK(12), IWORK(13)
C      60  FORMAT('/' No. steps =',i4,',   No. f-s =',i4,',   No. J-s =',i4)
C          STOP
C      80  WRITE(6,90)  ISTATE
C      90  FORMAT('///' Error halt.. ISTATE =',I3)
C          STOP
C          END
C
C      SUBROUTINE  FEX (NEQ, T, Y, YDOT)
C      INTEGER  NEQ
C      DOUBLE PRECISION  T, Y(3), YDOT(3)

```



```

C      YDOT(1) = -.04D0*Y(1) + 1.D4*Y(2)*Y(3)
C      YDOT(3) = 3.D7*Y(2)*Y(2)
C      YDOT(2) = -YDOT(1) - YDOT(3)
C      RETURN
C      END
C
C      SUBROUTINE JEX (NEQ, T, Y, ML, MU, PD, NRPD)
C      INTEGER  NEQ, ML, MU, NRPD
C      DOUBLE PRECISION  T, Y(3), PD(NRPD,3)
C      PD(1,1) = -.04D0
C      PD(1,2) = 1.D4*Y(3)
C      PD(1,3) = 1.D4*Y(2)
C      PD(2,1) = .04D0
C      PD(2,3) = -PD(1,3)
C      PD(3,2) = 6.D7*Y(2)
C      PD(2,2) = -PD(1,2) - PD(3,2)
C      RETURN
C      END
C
C      The output from this program (on a Cray-1 in single precision)
C      is as follows.
C
C      At t = 4.0000e-01    y = 9.851726e-01  3.386406e-05  1.479357e-02
C      At t = 4.0000e+00    y = 9.055142e-01  2.240418e-05  9.446344e-02
C      At t = 4.0000e+01    y = 7.158050e-01  9.184616e-06  2.841858e-01
C      At t = 4.0000e+02    y = 4.504846e-01  3.222434e-06  5.495122e-01
C      At t = 4.0000e+03    y = 1.831701e-01  8.940379e-07  8.168290e-01
C      At t = 4.0000e+04    y = 3.897016e-02  1.621193e-07  9.610297e-01
C      At t = 4.0000e+05    y = 4.935213e-03  1.983756e-08  9.950648e-01
C      At t = 4.0000e+06    y = 5.159269e-04  2.064759e-09  9.994841e-01
C      At t = 4.0000e+07    y = 5.306413e-05  2.122677e-10  9.999469e-01
C      At t = 4.0000e+08    y = 5.494530e-06  2.197825e-11  9.999945e-01
C      At t = 4.0000e+09    y = 5.129458e-07  2.051784e-12  9.999995e-01
C      At t = 4.0000e+10    y = -7.170603e-08 -2.868241e-13  1.000000e+00
C
C      No. steps = 330,  No. f-s = 405,  No. J-s = 69
C
C *Accuracy:
C      The accuracy of the solution depends on the choice of tolerances
C      RTOL and ATOL.  Actual (global) errors may exceed these local
C      tolerances, so choose them conservatively.
C
C *Cautions:
C      The work arrays should not be altered between calls to DLSODE for
C      the same problem, except possibly for the conditional and optional
C      inputs.
C
C *Portability:
C      Since NEQ is dimensioned inside DLSODE, some compilers may object
C      to a call to DLSODE with NEQ a scalar variable.  In this event,
C      use DIMENSION NEQ(1).  Similar remarks apply to RTOL and ATOL.
C
C      Note to Cray users:
C      For maximum efficiency, use the CFT77 compiler.  Appropriate
C      compiler optimization directives have been inserted for CFT77
C      (but not CIVIC).
C
C      NOTICE:  If moving the DLSODE source code to other systems,
C      contact the author for notes on nonstandard Fortran usage,
C      COMMON block, and other installation details.
C
C *Reference:
C      Alan C. Hindmarsh, "ODEPACK, a systematized collection of ODE
C      solvers," in Scientific Computing, R. S. Stepleman, et al., Eds.
C      (North-Holland, Amsterdam, 1983), pp. 55-64.
C
C *Long Description:

```

C The following complete description of the user interface to
C DLSODE consists of four parts:

- C 1. The call sequence to subroutine DLSODE, which is a driver
C routine for the solver. This includes descriptions of both
C the call sequence arguments and user-supplied routines.
C Following these descriptions is a description of optional
C inputs available through the call sequence, and then a
C description of optional outputs in the work arrays.
- C 2. Descriptions of other routines in the DLSODE package that may
C be (optionally) called by the user. These provide the ability
C to alter error message handling, save and restore the internal
C COMMON, and obtain specified derivatives of the solution $y(t)$.
- C 3. Descriptions of COMMON block to be declared in overlay or
C similar environments, or to be saved when doing an interrupt
C of the problem and continued solution later.
- C 4. Description of two routines in the DLSODE package, either of
C which the user may replace with his own version, if desired.
C These relate to the measurement of errors.

Part 1. Call Sequence

Arguments

The call sequence parameters used for input only are

F, NEQ, TOUT, ITOL, RTOL, ATOL, ITASK, IOPT, LRW, LIW, JAC, MF,

and those used for both input and output are

Y, T, ISTATE.

The work arrays RWORK and IWORK are also used for conditional and optional inputs and optional outputs. (The term output here refers to the return from subroutine DLSODE to the user's calling program.)

The legality of input parameters will be thoroughly checked on the initial call for the problem, but not checked thereafter unless a change in input parameters is flagged by ISTATE = 3 on input.

The descriptions of the call arguments are as follows.

F The name of the user-supplied subroutine defining the ODE system. The system must be put in the first-order form $dy/dt = f(t,y)$, where f is a vector-valued function of the scalar t and the vector y . Subroutine F is to compute the function f . It is to have the form

```
SUBROUTINE F (NEQ, T, Y, YDOT)
DOUBLE PRECISION Y(NEQ), YDOT(NEQ)
```

where NEQ, T, and Y are input, and the array YDOT = $f(T,Y)$ is output. Y and YDOT are arrays of length NEQ. Subroutine F should not alter $Y(1), \dots, Y(NEQ)$. F must be declared EXTERNAL in the calling program.

Subroutine F may access user-defined quantities in $NEQ(2), \dots$ and/or in $Y(NEQ(1)+1), \dots$, if NEQ is an array (dimensioned in F) and/or Y has length exceeding NEQ(1). See the descriptions of NEQ and Y below.

C If quantities computed in the F routine are needed
C externally to DLSODE, an extra call to F should be made
C for this purpose, for consistent and accurate results.
C If only the derivative dy/dt is needed, use DINTDY
C instead.
C

C NEQ The size of the ODE system (number of first-order
C ordinary differential equations). Used only for input.
C NEQ may be decreased, but not increased, during the
C problem. If NEQ is decreased (with ISTATE = 3 on input),
C the remaining components of Y should be left undisturbed,
C if these are to be accessed in F and/or JAC.
C

C Normally, NEQ is a scalar, and it is generally referred
C to as a scalar in this user interface description.
C However, NEQ may be an array, with NEQ(1) set to the
C system size. (The DLSODE package accesses only NEQ(1).)
C In either case, this parameter is passed as the NEQ
C argument in all calls to F and JAC. Hence, if it is an
C array, locations NEQ(2),... may be used to store other
C integer data and pass it to F and/or JAC. Subroutines
C F and/or JAC must include NEQ in a DIMENSION statement
C in that case.
C

C Y A real array for the vector of dependent variables, of
C length NEQ or more. Used for both input and output on
C the first call (ISTATE = 1), and only for output on
C other calls. On the first call, Y must contain the
C vector of initial values. On output, Y contains the
C computed solution vector, evaluated at T. If desired,
C the Y array may be used for other purposes between
C calls to the solver.
C

C This array is passed as the Y argument in all calls to F
C and JAC. Hence its length may exceed NEQ, and locations
C Y(NEQ+1),... may be used to store other real data and
C pass it to F and/or JAC. (The DLSODE package accesses
C only Y(1),...,Y(NEQ).)
C

C T The independent variable. On input, T is used only on
C the first call, as the initial point of the integration.
C On output, after each call, T is the value at which a
C computed solution Y is evaluated (usually the same as
C TOUT). On an error return, T is the farthest point
C reached.
C

C TOUT The next value of T at which a computed solution is
C desired. Used only for input.
C

C When starting the problem (ISTATE = 1), TOUT may be equal
C to T for one call, then should not equal T for the next
C call. For the initial T, an input value of TOUT .NE. T
C is used in order to determine the direction of the
C integration (i.e., the algebraic sign of the step sizes)
C and the rough scale of the problem. Integration in
C either direction (forward or backward in T) is permitted.
C

C If ITASK = 2 or 5 (one-step modes), TOUT is ignored
C after the first call (i.e., the first call with
C TOUT .NE. T). Otherwise, TOUT is required on every call.
C

C If ITASK = 1, 3, or 4, the values of TOUT need not be
C monotone, but a value of TOUT which backs up is limited
C to the current internal T interval, whose endpoints are
C TCUR - HU and TCUR. (See "Optional Outputs" below for
C TCUR and HU.)
C

C
C ITOL An indicator for the type of error control. See
C description below under ATOL. Used only for input.
C
C RTOL A relative error tolerance parameter, either a scalar or
C an array of length NEQ. See description below under
C ATOL. Input only.
C
C ATOL An absolute error tolerance parameter, either a scalar or
C an array of length NEQ. Input only.
C
C The input parameters ITOL, RTOL, and ATOL determine the
C error control performed by the solver. The solver will
C control the vector $e = (e(i))$ of estimated local errors
C in Y, according to an inequality of the form
C
C
$$\text{rms-norm of } (e(i)/EWT(i)) \leq 1,$$

C
C where
C
C
$$EWT(i) = RTOL(i)*ABS(Y(i)) + ATOL(i),$$

C
C and the rms-norm (root-mean-square norm) here is
C
C
$$\text{rms-norm}(v) = \text{SQRT}(\text{sum } v(i)**2 / \text{NEQ}).$$

C
C Here EWT = (EWT(i)) is a vector of weights which must
C always be positive, and the values of RTOL and ATOL
C should all be nonnegative. The following table gives the
C types (scalar/array) of RTOL and ATOL, and the
C corresponding form of EWT(i).
C
C

ITOL	RTOL	ATOL	EWT(i)
1	scalar	scalar	$RTOL*ABS(Y(i)) + ATOL$
2	scalar	array	$RTOL*ABS(Y(i)) + ATOL(i)$
3	array	scalar	$RTOL(i)*ABS(Y(i)) + ATOL$
4	array	array	$RTOL(i)*ABS(Y(i)) + ATOL(i)$

C
C When either of these parameters is a scalar, it need not
C be dimensioned in the user's calling program.
C
C If none of the above choices (with ITOL, RTOL, and ATOL
C fixed throughout the problem) is suitable, more general
C error controls can be obtained by substituting
C user-supplied routines for the setting of EWT and/or for
C the norm calculation. See Part 4 below.
C
C If global errors are to be estimated by making a repeated
C run on the same problem with smaller tolerances, then all
C components of RTOL and ATOL (i.e., of EWT) should be
C scaled down uniformly.
C
C ITASK An index specifying the task to be performed. Input
C only. ITASK has the following values and meanings:
C 1 Normal computation of output values of $y(t)$ at
C $t = \text{TOUT}$ (by overshooting and interpolating).
C 2 Take one step only and return.
C 3 Stop at the first internal mesh point at or beyond
C $t = \text{TOUT}$ and return.
C 4 Normal computation of output values of $y(t)$ at
C $t = \text{TOUT}$ but without overshooting $t = \text{TCRIT}$. TCRIT
C must be input as $\text{RWORK}(1)$. TCRIT may be equal to or
C beyond TOUT , but not behind it in the direction of
C integration. This option is useful if the problem
C has a singularity at or beyond $t = \text{TCRIT}$.
C 5 Take one step, without passing TCRIT, and return.

C TCRIT must be input as RWORK(1).
C
C Note: If ITASK = 4 or 5 and the solver reaches TCRIT
C (within roundoff), it will return T = TCRIT (exactly) to
C indicate this (unless ITASK = 4 and TOUT comes before
C TCRIT, in which case answers at T = TOUT are returned
C first).
C
C ISTATE An index used for input and output to specify the state
C of the calculation.
C
C On input, the values of ISTATE are as follows:
C 1 This is the first call for the problem
C (initializations will be done). See "Note" below.
C 2 This is not the first call, and the calculation is to
C continue normally, with no change in any input
C parameters except possibly TOUT and ITASK. (If ITOL,
C RTOL, and/or ATOL are changed between calls with
C ISTATE = 2, the new values will be used but not
C tested for legality.)
C 3 This is not the first call, and the calculation is to
C continue normally, but with a change in input
C parameters other than TOUT and ITASK. Changes are
C allowed in NEQ, ITOL, RTOL, ATOL, IOPT, LRW, LIW, MF,
C ML, MU, and any of the optional inputs except H0.
C (See IWORK description for ML and MU.)
C
C Note: A preliminary call with TOUT = T is not counted as
C a first call here, as no initialization or checking of
C input is done. (Such a call is sometimes useful for the
C purpose of outputting the initial conditions.) Thus the
C first call for which TOUT .NE. T requires ISTATE = 1 on
C input.
C
C On output, ISTATE has the following values and meanings:
C 1 Nothing was done, as TOUT was equal to T with
C ISTATE = 1 on input.
C 2 The integration was performed successfully.
C -1 An excessive amount of work (more than MXSTEP steps)
C was done on this call, before completing the
C requested task, but the integration was otherwise
C successful as far as T. (MXSTEP is an optional input
C and is normally 500.) To continue, the user may
C simply reset ISTATE to a value >1 and call again (the
C excess work step counter will be reset to 0). In
C addition, the user may increase MXSTEP to avoid this
C error return; see "Optional Inputs" below.
C -2 Too much accuracy was requested for the precision of
C the machine being used. This was detected before
C completing the requested task, but the integration
C was successful as far as T. To continue, the
C tolerance parameters must be reset, and ISTATE must
C be set to 3. The optional output TOLSF may be used
C for this purpose. (Note: If this condition is
C detected before taking any steps, then an illegal
C input return (ISTATE = -3) occurs instead.)
C -3 Illegal input was detected, before taking any
C integration steps. See written message for details.
C (Note: If the solver detects an infinite loop of
C calls to the solver with illegal input, it will cause
C the run to stop.)
C -4 There were repeated error-test failures on one
C attempted step, before completing the requested task,
C but the integration was successful as far as T. The
C problem may have a singularity, or the input may be
C inappropriate.
C -5 There were repeated convergence-test failures on one

C attempted step, before completing the requested task,
 C but the integration was successful as far as T. This
 C may be caused by an inaccurate Jacobian matrix, if
 C one is being used.

C -6 EWT(i) became zero for some i during the integration.
 C Pure relative error control (ATOL(i)=0.0) was
 C requested on a variable which has now vanished. The
 C integration was successful as far as T.

C Note: Since the normal output value of ISTATE is 2, it
 C does not need to be reset for normal continuation. Also,
 C since a negative input value of ISTATE will be regarded
 C as illegal, a negative output value requires the user to
 C change it, and possibly other inputs, before calling the
 C solver again.

C IOPT An integer flag to specify whether any optional inputs
 C are being used on this call. Input only. The optional
 C inputs are listed under a separate heading below.
 C 0 No optional inputs are being used. Default values
 C will be used in all cases.
 C 1 One or more optional inputs are being used.

C RWORK A real working array (double precision). The length of
 C RWORK must be at least

$$20 + NYH*(MAXORD + 1) + 3*NEQ + LWM$$

C where

C NYH = the initial value of NEQ,
 C MAXORD = 12 (if METH = 1) or 5 (if METH = 2) (unless a
 C smaller value is given as an optional input),
 C LWM = 0 if MITER = 0,
 C LWM = NEQ**2 + 2 if MITER = 1 or 2,
 C LWM = NEQ + 2 if MITER = 3, and
 C LWM = (2*ML + MU + 1)*NEQ + 2
 C if MITER = 4 or 5.

C (See the MF description below for METH and MITER.)

C Thus if MAXORD has its default value and NEQ is constant,
 C this length is:

C 20 + 16*NEQ for MF = 10,
 C 22 + 16*NEQ + NEQ**2 for MF = 11 or 12,
 C 22 + 17*NEQ for MF = 13,
 C 22 + 17*NEQ + (2*ML + MU)*NEQ for MF = 14 or 15,
 C 20 + 9*NEQ for MF = 20,
 C 22 + 9*NEQ + NEQ**2 for MF = 21 or 22,
 C 22 + 10*NEQ for MF = 23,
 C 22 + 10*NEQ + (2*ML + MU)*NEQ for MF = 24 or 25.

C The first 20 words of RWORK are reserved for conditional
 C and optional inputs and optional outputs.

C The following word in RWORK is a conditional input:
 C RWORK(1) = TCRIT, the critical value of t which the
 C solver is not to overshoot. Required if ITASK
 C is 4 or 5, and ignored otherwise. See ITASK.

C LRW The length of the array RWORK, as declared by the user.
 C (This will be checked by the solver.)

C IWORK An integer work array. Its length must be at least
 C 20 if MITER = 0 or 3 (MF = 10, 13, 20, 23), or
 C 20 + NEQ otherwise (MF = 11, 12, 14, 15, 21, 22, 24, 25).
 C (See the MF description below for MITER.) The first few
 C words of IWORK are used for conditional and optional
 C inputs and optional outputs.

C
C The following two words in IWORK are conditional inputs:
C IWORK(1) = ML These are the lower and upper half-
C IWORK(2) = MU bandwidths, respectively, of the banded
C Jacobian, excluding the main diagonal.
C The band is defined by the matrix locations
C (i,j) with $i - ML \leq j \leq i + MU$. ML and MU
C must satisfy $0 \leq ML, MU \leq NEQ - 1$. These are
C required if MITER is 4 or 5, and ignored
C otherwise. ML and MU may in fact be the band
C parameters for a matrix to which df/dy is only
C approximately equal.
C
C LIW The length of the array IWORK, as declared by the user.
C (This will be checked by the solver.)
C
C Note: The work arrays must not be altered between calls to DLSODE
C for the same problem, except possibly for the conditional and
C optional inputs, and except for the last $3*NEQ$ words of RWORK.
C The latter space is used for internal scratch space, and so is
C available for use by the user outside DLSODE between calls, if
C desired (but not for use by F or JAC).
C
C JAC The name of the user-supplied routine (MITER = 1 or 4) to
C compute the Jacobian matrix, df/dy , as a function of the
C scalar t and the vector y . (See the MF description below
C for MITER.) It is to have the form
C
C SUBROUTINE JAC (NEQ, T, Y, ML, MU, PD, NROWPD)
C DOUBLE PRECISION Y(NEQ), PD(NROWPD,NEQ)
C
C where NEQ, T, Y, ML, MU, and NROWPD are input and the
C array PD is to be loaded with partial derivatives
C (elements of the Jacobian matrix) on output. PD must be
C given a first dimension of NROWPD. T and Y have the same
C meaning as in subroutine F.
C
C In the full matrix case (MITER = 1), ML and MU are
C ignored, and the Jacobian is to be loaded into PD in
C columnwise manner, with $df(i)/dy(j)$ loaded into PD(i,j).
C
C In the band matrix case (MITER = 4), the elements within
C the band are to be loaded into PD in columnwise manner,
C with diagonal lines of df/dy loaded into the rows of PD.
C Thus $df(i)/dy(j)$ is to be loaded into PD(i-j+MU+1,j). ML
C and MU are the half-bandwidth parameters (see IWORK).
C The locations in PD in the two triangular areas which
C correspond to nonexistent matrix elements can be ignored
C or loaded arbitrarily, as they are overwritten by DLSODE.
C
C JAC need not provide df/dy exactly. A crude approximation
C (possibly with a smaller bandwidth) will do.
C
C In either case, PD is preset to zero by the solver, so
C that only the nonzero elements need be loaded by JAC.
C Each call to JAC is preceded by a call to F with the same
C arguments NEQ, T, and Y. Thus to gain some efficiency,
C intermediate quantities shared by both calculations may
C be saved in a user COMMON block by F and not recomputed
C by JAC, if desired. Also, JAC may alter the Y array, if
C desired. JAC must be declared EXTERNAL in the calling
C program.
C
C Subroutine JAC may access user-defined quantities in
C NEQ(2),... and/or in Y(NEQ(1)+1),... if NEQ is an array
C (dimensioned in JAC) and/or Y has length exceeding
C NEQ(1). See the descriptions of NEQ and Y above.

C
 C MF The method flag. Used only for input. The legal values
 C of MF are 10, 11, 12, 13, 14, 15, 20, 21, 22, 23, 24,
 C and 25. MF has decimal digits METH and MITER:
 C $MF = 10 * METH + MITER$.
 C
 C METH indicates the basic linear multistep method:
 C 1 Implicit Adams method.
 C 2 Method based on backward differentiation formulas
 C (BDF's).
 C
 C MITER indicates the corrector iteration method:
 C 0 Functional iteration (no Jacobian matrix is
 C involved).
 C 1 Chord iteration with a user-supplied full (NEQ by
 C NEQ) Jacobian.
 C 2 Chord iteration with an internally generated
 C (difference quotient) full Jacobian (using NEQ
 C extra calls to F per df/dy value).
 C 3 Chord iteration with an internally generated
 C diagonal Jacobian approximation (using one extra call
 C to F per df/dy evaluation).
 C 4 Chord iteration with a user-supplied banded Jacobian.
 C 5 Chord iteration with an internally generated banded
 C Jacobian (using $ML + MU + 1$ extra calls to F per
 C df/dy evaluation).
 C
 C If MITER = 1 or 4, the user must supply a subroutine JAC
 C (the name is arbitrary) as described above under JAC.
 C For other values of MITER, a dummy argument can be used.

Optional Inputs

 C The following is a list of the optional inputs provided for in the
 C call sequence. (See also Part 2.) For each such input variable,
 C this table lists its name as used in this documentation, its
 C location in the call sequence, its meaning, and the default value.
 C The use of any of these inputs requires IOPT = 1, and in that case
 C all of these inputs are examined. A value of zero for any of
 C these optional inputs will cause the default value to be used.
 C Thus to use a subset of the optional inputs, simply preload
 C locations 5 to 10 in RWORK and IWORK to 0.0 and 0 respectively,
 C and then set those of interest to nonzero values.

Name	Location	Meaning and default value
H0	RWORK(5)	Step size to be attempted on the first step. The default value is determined by the solver.
HMAX	RWORK(6)	Maximum absolute step size allowed. The default value is infinite.
HMIN	RWORK(7)	Minimum absolute step size allowed. The default value is 0. (This lower bound is not enforced on the final step before reaching TCRIT when ITASK = 4 or 5.)
MAXORD	IWORK(5)	Maximum order to be allowed. The default value is 12 if METH = 1, and 5 if METH = 2. (See the MF description above for METH.) If MAXORD exceeds the default value, it will be reduced to the default value. If MAXORD is changed during the problem, it may cause the current order to be reduced.
MXSTEP	IWORK(6)	Maximum number of (internally defined) steps allowed during one call to the solver. The default value is 500.
MXHNIL	IWORK(7)	Maximum number of messages printed (per problem) warning that $T + H = T$ on a step ($H =$ step size). This must be positive to

C result in a nondefault value. The default
 C value is 10.
 C
 C Optional Outputs
 C -----
 C As optional additional output from DLSODE, the variables listed
 C below are quantities related to the performance of DLSODE which
 C are available to the user. These are communicated by way of the
 C work arrays, but also have internal mnemonic names as shown.
 C Except where stated otherwise, all of these outputs are defined on
 C any successful return from DLSODE, and on any return with ISTATE =
 C -1, -2, -4, -5, or -6. On an illegal input return (ISTATE = -3),
 C they will be unchanged from their existing values (if any), except
 C possibly for TOLSF, LENRW, and LENIW. On any error return,
 C outputs relevant to the error will be defined, as noted below.
 C
 C Name Location Meaning
 C -----
 C HU RWORK(11) Step size in t last used (successfully).
 C HCUR RWORK(12) Step size to be attempted on the next step.
 C TCUR RWORK(13) Current value of the independent variable which
 C the solver has actually reached, i.e., the
 C current internal mesh point in t. On output,
 C TCUR will always be at least as far as the
 C argument T, but may be farther (if interpolation
 C was done).
 C TOLSF RWORK(14) Tolerance scale factor, greater than 1.0,
 C computed when a request for too much accuracy
 C was detected (ISTATE = -3 if detected at the
 C start of the problem, ISTATE = -2 otherwise).
 C If ITOL is left unaltered but RTOL and ATOL are
 C uniformly scaled up by a factor of TOLSF for the
 C next call, then the solver is deemed likely to
 C succeed. (The user may also ignore TOLSF and
 C alter the tolerance parameters in any other way
 C appropriate.)
 C NST IWORK(11) Number of steps taken for the problem so far.
 C NFE IWORK(12) Number of F evaluations for the problem so far.
 C NJE IWORK(13) Number of Jacobian evaluations (and of matrix LU
 C decompositions) for the problem so far.
 C NQU IWORK(14) Method order last used (successfully).
 C NQCUR IWORK(15) Order to be attempted on the next step.
 C IMXER IWORK(16) Index of the component of largest magnitude in
 C the weighted local error vector ($e(i)/EWT(i)$),
 C on an error return with ISTATE = -4 or -5.
 C LENRW IWORK(17) Length of RWORK actually required. This is
 C defined on normal returns and on an illegal
 C input return for insufficient storage.
 C LENIW IWORK(18) Length of IWORK actually required. This is
 C defined on normal returns and on an illegal
 C input return for insufficient storage.
 C
 C The following two arrays are segments of the RWORK array which may
 C also be of interest to the user as optional outputs. For each
 C array, the table below gives its internal name, its base address
 C in RWORK, and its description.
 C
 C Name Base address Description
 C -----
 C YH 21 The Nordsieck history array, of size NYH by
 C (NQCUR + 1), where NYH is the initial value of
 C NEQ. For $j = 0, 1, \dots, NQCUR$, column $j + 1$ of
 C YH contains $HCUR^{*j}/factorial(j)$ times the j th
 C derivative of the interpolating polynomial
 C currently representing the solution, evaluated
 C at $t = TCUR$.
 C ACOR LENRW-NEQ+1 Array of size NEQ used for the accumulated

C corrections on each step, scaled on output to
 C represent the estimated local error in Y on
 C the last step. This is the vector e in the
 C description of the error control. It is
 C defined only on successful return from DLSODE.
 C
 C

C Part 2. Other Callable Routines
 C -----
 C

C The following are optional calls which the user may make to gain
 C additional capabilities in conjunction with DLSODE.
 C

Form of call	Function

CALL XSETUN(LUN)	Set the logical unit number, LUN, for output of messages from DLSODE, if the default is not desired. The default value of LUN is 6. This call may be made at any time and will take effect immediately.
CALL XSETF(MFLAG)	Set a flag to control the printing of messages by DLSODE. MFLAG = 0 means do not print. (Danger: this risks losing valuable information.) MFLAG = 1 means print (the default). This call may be made at any time and will take effect immediately.
CALL DSRCOM(RSAV, ISAV, JOB)	Saves and restores the contents of the internal COMMON blocks used by DLSODE (see Part 3 below). RSAV must be a real array of length 218 or more, and ISAV must be an integer array of length 37 or more. JOB = 1 means save COMMON into RSAV/ISAV. JOB = 2 means restore COMMON from same. DSRCOM is useful if one is interrupting a run and restarting later, or alternating between two or more problems solved with DLSODE.
CALL DINTDY(,,,,,) (see below)	Provide derivatives of y, of various orders, at a specified point t, if desired. It may be called only after a successful return from DLSODE. Detailed instructions follow.

C Detailed instructions for using DINTDY
 C -----
 C

C The form of the CALL is:

C CALL DINTDY (T, K, RWORK(21), NYH, DKY, IFLAG)

C The input parameters are:

C T Value of independent variable where answers are
 C desired (normally the same as the T last returned by
 C DLSODE). For valid results, T must lie between
 C TCUR - HU and TCUR. (See "Optional Outputs" above
 C for TCUR and HU.)
 C K Integer order of the derivative desired. K must
 C satisfy $0 \leq K \leq \text{NQCUR}$, where NQCUR is the current
 C order (see "Optional Outputs"). The capability
 C corresponding to $K = 0$, i.e., computing $y(t)$, is
 C already provided by DLSODE directly. Since
 C NQCUR ≥ 1 , the first derivative dy/dt is always
 C available with DINTDY.
 C RWORK(21) The base address of the history array YH.
 C NYH Column length of YH, equal to the initial value of NEQ.

C
C The output parameters are:
C
C DKY Real array of length NEQ containing the computed value
C of the Kth derivative of $y(t)$.
C IFLAG Integer flag, returned as 0 if K and T were legal,
C -1 if K was illegal, and -2 if T was illegal.
C On an error return, a message is also written.
C
C
C Part 3. Common Blocks
C -----
C
C If DLSODE is to be used in an overlay situation, the user must
C declare, in the primary overlay, the variables in:
C (1) the call sequence to DLSODE,
C (2) the internal COMMON block /DLS001/, of length 255
C (218 double precision words followed by 37 integer words).
C
C If DLSODE is used on a system in which the contents of internal
C COMMON blocks are not preserved between calls, the user should
C declare the above COMMON block in his main program to insure that
C its contents are preserved.
C
C If the solution of a given problem by DLSODE is to be interrupted
C and then later continued, as when restarting an interrupted run or
C alternating between two or more problems, the user should save,
C following the return from the last DLSODE call prior to the
C interruption, the contents of the call sequence variables and the
C internal COMMON block, and later restore these values before the
C next DLSODE call for that problem. In addition, if XSETUN and/or
C XSETF was called for non-default handling of error messages, then
C these calls must be repeated. To save and restore the COMMON
C block, use subroutine DSRCOM (see Part 2 above).
C
C
C Part 4. Optionally Replaceable Solver Routines
C -----
C
C Below are descriptions of two routines in the DLSODE package which
C relate to the measurement of errors. Either routine can be
C replaced by a user-supplied version, if desired. However, since
C such a replacement may have a major impact on performance, it
C should be done only when absolutely necessary, and only with great
C caution. (Note: The means by which the package version of a
C routine is superseded by the user's version may be system-
C dependent.)
C
C DEWSET
C -----
C The following subroutine is called just before each internal
C integration step, and sets the array of error weights, EWT, as
C described under ITOL/RTOL/ATOL above:
C
C SUBROUTINE DEWSET (NEQ, ITOL, RTOL, ATOL, YCUR, EWT)
C
C where NEQ, ITOL, RTOL, and ATOL are as in the DLSODE call
C sequence, YCUR contains the current dependent variable vector,
C and EWT is the array of weights set by DEWSET.
C
C If the user supplies this subroutine, it must return in EWT(i)
C ($i = 1, \dots, \text{NEQ}$) a positive quantity suitable for comparing errors
C in $Y(i)$ to. The EWT array returned by DEWSET is passed to the
C DVNORM routine (see below), and also used by DLSODE in the
C computation of the optional output IMXER, the diagonal Jacobian
C approximation, and the increments for difference quotient
C Jacobians.

C
 C In the user-supplied version of DEWSET, it may be desirable to use
 C the current values of derivatives of y. Derivatives up to order NQ
 C are available from the history array YH, described above under
 C optional outputs. In DEWSET, YH is identical to the YCUR array,
 C extended to NQ + 1 columns with a column length of NYH and scale
 C factors of $H^{**j}/\text{factorial}(j)$. On the first call for the problem,
 C given by NST = 0, NQ is 1 and H is temporarily set to 1.0. The
 C quantities NQ, NYH, H, and NST can be obtained by including in
 C DEWSET the statements:

```
C
C      DOUBLE PRECISION  RLS
C      COMMON /DLS001/ RLS(218),ILS(37)
C      NQ = ILS(33)
C      NYH = ILS(12)
C      NST = ILS(34)
C      H = RLS(212)
C
```

C Thus, for example, the current value of dy/dt can be obtained as
 C YCUR(NYH+i)/H (i=1,...,NEQ) (and the division by H is unnecessary
 C when NST = 0).

```
C
C DVNORM
C -----
```

C DVNORM is a real function routine which computes the weighted
 C root-mean-square norm of a vector v:

```
C      d = DVNORM (n, v, w)
C
```

C where:

```
C n = the length of the vector,
C v = real array of length n containing the vector,
C w = real array of length n containing weights,
C d = SQRT( (1/n) * sum(v(i)*w(i))**2 ).
```

C DVNORM is called with n = NEQ and with $w(i) = 1.0/\text{EWT}(i)$, where
 C EWT is as set by subroutine DEWSET.

C If the user supplies this function, it should return a nonnegative
 C value of DVNORM suitable for use in the error control in DLSODE.
 C None of the arguments should be altered by DVNORM. For example, a
 C user-supplied DVNORM routine might:

```
C - Substitute a max-norm of (v(i)*w(i)) for the rms-norm, or
C - Ignore some components of v in the norm, with the effect of
C   suppressing the error control on those components of Y.
```

```
C -----
C***REFERENCES Alan C. Hindmarsh, "ODEPACK, a systematized collection
C               of ODE solvers", in Scientific Computing, R. S.
C               Stepleman, et al. (Eds.), (North-Holland, Amsterdam,
C               1983), pp. 55-64.
```

```
C***ROUTINES CALLED DEWSET, DINTDY, DUMACH, DSTODE, DVNORM, XERRWD
```

```
C***COMMON BLOCKS DLS001
```

```
C***REVISION HISTORY (YYMMDD)
```

```
C 791129 DATE WRITTEN
C 870330 Major update by ACH.
C 890426 Modified prologue to SLATEC/LDOC format. (FNF)
C 890501 Many improvements to prologue. (FNF)
C 890503 A few final corrections to prologue. (FNF)
C 890504 Minor cosmetic changes. (FNF)
C 890510 Corrected description of Y in Arguments section. (FNF)
C 890517 Minor corrections to prologue. (FNF)
C 920514 Updated with prologue edited 891025 by G. Shaw for manual.
C 920515 Converted source lines to upper case. (FNF)
C 920603 Revised XERRWD calls using mixed upper-lower case. (ACH)
C 920616 Revised prologue comment regarding CFT. (ACH)
C 921116 Revised prologue comments regarding Common. (ACH).
C 930326 Added comment about non-reentrancy. (FNF)
```

```

C 930723 Changed R1MACH to RUMACH. (FNF)
C 930801 Removed Common variables ILLIN and NTREP (affects driver
C logic and Common references); minor changes to prologue and
C internal comments; changed Hollerith strings to quoted
C strings; changed internal comments to mixed case; changed
C dummy dimensions from 1 to *. (ACH)
C 930809 Changed to generic intrinsic names; changed names of
C subprograms and Common blocks to SLSODE etc. (ACH)
C 930929 Eliminated use of REAL intrinsic; other minor changes. (ACH)
C 931005 Generated double precision version. (ACH)
C***END PROLOGUE DLSODE
C
C*Internal Notes:
C
C Other Routines in the DLSODE Package.
C
C In addition to Subroutine DLSODE, the DLSODE package includes the
C following subroutines and function routines:
C DINTDY computes an interpolated value of the y vector at t = TOUT.
C DSTODE is the core integrator, which does one step of the
C integration and the associated error control.
C DCFODE sets all method coefficients and test constants.
C DPREPJ computes and preprocesses the Jacobian matrix J = df/dy
C and the Newton iteration matrix P = I - h*10*J.
C DSOLSY manages solution of linear system in chord iteration.
C DEWSET sets the error weight vector EWT before each step.
C DVNORM computes the weighted R.M.S. norm of a vector.
C DSRCOM is a user-callable routine to save and restore
C the contents of the internal Common block.
C DGEFA and DGESL are routines from LINPACK for solving full
C systems of linear algebraic equations.
C DGBFA and DGBSL are routines from LINPACK for solving banded
C linear systems.
C DUMACH computes the unit roundoff in a machine-independent manner.
C XERRWD, XSETUN, and XSETF handle the printing of all error
C messages and warnings. XERRWD is machine-dependent.
C Note.. DVNORM and DUMACH are function routines. All the others
C are subroutines.
C
C The intrinsic routines used by DLSODE are..
C ABS, MAX, MIN, MOD, SIGN, and SQRT.
C
C**End
C
C Declare arguments.
C
EXTERNAL F, JAC
INTEGER NEQ, ITOL, ITASK, ISTATE, IOPT, LRW, IWORK, LIW, MF
DOUBLE PRECISION Y, T, TOUT, RTOL, ATOL, RWORK
DIMENSION NEQ(*), Y(*), RTOL(*), ATOL(*), RWORK(LRW), IWORK(LIW)
C
C Declare externals.
C
EXTERNAL DPREPJ, DSOLSY
DOUBLE PRECISION DUMACH, DVNORM
C
C Declare all other variables.
C
INTEGER INIT, LYH, LEWT, LACOR, LSAVF, LWM, LIWM,
1 MXSTEP, MXHNIL, NHNIL, NSLAST, NYH, IOWNS
INTEGER ICF, IERPJ, IERSL, JCUR, JSTART, KFLAG, L, METH, MITER,
1 MAXORD, MAXCOR, MSBP, MXNCF, N, NQ, NST, NFE, NJE, NQU
INTEGER I, I1, I2, IFLAG, IMXER, KGO, LFO,
1 LENIW, LENRW, LENWM, ML, MORD, MU, MXHNL0, MXSTP0
DOUBLE PRECISION ROWNS,
1 CCMAX, EL0, H, HMIN, HMXI, HU, RC, TN, UROUND
DOUBLE PRECISION ATOLI, AYI, BIG, EWTI, H0, HMAX, HMX, RH, RTOLI,

```

```

1  TCRIT, TDIST, TNEXT, TOL, TOLSF, TP, SIZE, SUM, W0
   DIMENSION MORD(2)
   LOGICAL IHIT
   CHARACTER*80 MSG
C-----
C The following internal common block contains
C (a) variables which are local to any subroutine but whose values must
C   be preserved between calls to the routine (own variables), and
C (b) variables which are communicated between subroutines.
C The structure of the block is as follows.. All real variables are
C listed first, followed by all integers. Within each type, the
C variables are grouped with those local to Subroutine DLSODE first,
C then those local to Subroutine DSTODE, and finally those used
C for communication. The block is declared in subroutines
C DLSODE, DINTDY, DSTODE, DPREPJ, and DSOLSY. Groups of variables are
C replaced by dummy arrays in the common declarations in routines
C where those variables are not used.
C-----
COMMON /DLS001/ ROWNS(209),
1  CCMAX, EL0, H, HMIN, HMXI, HU, RC, TN, UROUND,
2  INIT, LYH, LEWT, LACOR, LSAVF, LWM, LIWM,
3  MXSTEP, MXHNIL, NHNIL, NSLAST, NYH, IOWNS(6),
4  ICF, IERPJ, IERSL, JCUR, JSTART, KFLAG, L, METH, MITER,
5  MAXORD, MAXCOR, MSBP, MXNCF, N, NQ, NST, NFE, NJE, NQU
C
DATA MORD(1),MORD(2)/12,5/, MXSTP0/500/, MXHNLO/10/
C-----
C Block A.
C This code block is executed on every call.
C It tests ISTATE and ITASK for legality and branches appropriately.
C If ISTATE .GT. 1 but the flag INIT shows that initialization has
C not yet been done, an error return occurs.
C If ISTATE = 1 and TOUT = T, return immediately.
C-----
C
C***FIRST EXECUTABLE STATEMENT DLSODE
   IF (ISTATE .LT. 1 .OR. ISTATE .GT. 3) GO TO 601
   IF (ITASK .LT. 1 .OR. ITASK .GT. 5) GO TO 602
   IF (ISTATE .EQ. 1) GO TO 10
   IF (INIT .EQ. 0) GO TO 603
   IF (ISTATE .EQ. 2) GO TO 200
   GO TO 20
10  INIT = 0
   IF (TOUT .EQ. T) RETURN
C-----
C Block B.
C The next code block is executed for the initial call (ISTATE = 1),
C or for a continuation call with parameter changes (ISTATE = 3).
C It contains checking of all inputs and various initializations.
C
C First check legality of the non-optional inputs NEQ, ITOL, IOPT,
C MF, ML, and MU.
C-----
20  IF (NEQ(1) .LE. 0) GO TO 604
   IF (ISTATE .EQ. 1) GO TO 25
   IF (NEQ(1) .GT. N) GO TO 605
25  N = NEQ(1)
   IF (ITOL .LT. 1 .OR. ITOL .GT. 4) GO TO 606
   IF (IOPT .LT. 0 .OR. IOPT .GT. 1) GO TO 607
   METH = MF/10
   MITER = MF - 10*METH
   IF (METH .LT. 1 .OR. METH .GT. 2) GO TO 608
   IF (MITER .LT. 0 .OR. MITER .GT. 5) GO TO 608
   IF (MITER .LE. 3) GO TO 30
   ML = IWORK(1)
   MU = IWORK(2)
   IF (ML .LT. 0 .OR. ML .GE. N) GO TO 609

```

```

      IF (MU .LT. 0 .OR. MU .GE. N) GO TO 610
30   CONTINUE
C Next process and check the optional inputs. -----
      IF (IOPT .EQ. 1) GO TO 40
      MAXORD = MORD(METH)
      MXSTEP = MXSTP0
      MXHNIL = MXHNL0
      IF (ISTATE .EQ. 1) H0 = 0.0D0
      HMXI = 0.0D0
      HMIN = 0.0D0
      GO TO 60
40   MAXORD = IWORK(5)
      IF (MAXORD .LT. 0) GO TO 611
      IF (MAXORD .EQ. 0) MAXORD = 100
      MAXORD = MIN(MAXORD,MORD(METH))
      MXSTEP = IWORK(6)
      IF (MXSTEP .LT. 0) GO TO 612
      IF (MXSTEP .EQ. 0) MXSTEP = MXSTP0
      MXHNIL = IWORK(7)
      IF (MXHNIL .LT. 0) GO TO 613
      IF (MXHNIL .EQ. 0) MXHNIL = MXHNL0
      IF (ISTATE .NE. 1) GO TO 50
      H0 = RWORK(5)
      IF ((TOUT - T)*H0 .LT. 0.0D0) GO TO 614
50   HMAX = RWORK(6)
      IF (HMAX .LT. 0.0D0) GO TO 615
      HMXI = 0.0D0
      IF (HMAX .GT. 0.0D0) HMXI = 1.0D0/HMAX
      HMIN = RWORK(7)
      IF (HMIN .LT. 0.0D0) GO TO 616
C-----
C Set work array pointers and check lengths LRW and LIW.
C Pointers to segments of RWORK and IWORK are named by prefixing L to
C the name of the segment.  E.g., the segment YH starts at RWORK(LYH).
C Segments of RWORK (in order) are denoted YH, WM, EWT, SAVF, ACOR.
C-----
60   LYH = 21
      IF (ISTATE .EQ. 1) NYH = N
      LWM = LYH + (MAXORD + 1)*NYH
      IF (MITER .EQ. 0) LENWM = 0
      IF (MITER .EQ. 1 .OR. MITER .EQ. 2) LENWM = N*N + 2
      IF (MITER .EQ. 3) LENWM = N + 2
      IF (MITER .GE. 4) LENWM = (2*ML + MU + 1)*N + 2
      LEWT = LWM + LENWM
      LSAVF = LEWT + N
      LACOR = LSAVF + N
      LENRW = LACOR + N - 1
      IWORK(17) = LENRW
      LIWM = 1
      LENIW = 20 + N
      IF (MITER .EQ. 0 .OR. MITER .EQ. 3) LENIW = 20
      IWORK(18) = LENIW
      IF (LENRW .GT. LRW) GO TO 617
      IF (LENIW .GT. LIW) GO TO 618
C Check RTOL and ATOL for legality. -----
      RTOLI = RTOL(1)
      ATOLI = ATOL(1)
      DO 70 I = 1,N
          IF (ITOL .GE. 3) RTOLI = RTOL(I)
          IF (ITOL .EQ. 2 .OR. ITOL .EQ. 4) ATOLI = ATOL(I)
          IF (RTOLI .LT. 0.0D0) GO TO 619
          IF (ATOLI .LT. 0.0D0) GO TO 620
70   CONTINUE
      IF (ISTATE .EQ. 1) GO TO 100
C If ISTATE = 3, set flag to signal parameter changes to DSTODE. -----
      JSTART = -1
      IF (NQ .LE. MAXORD) GO TO 90

```

```

C MAXORD was reduced below NQ. Copy YH(*,MAXORD+2) into SAVF. -----
  DO 80 I = 1,N
  80   RWORK(I+LSAVF-1) = RWORK(I+LWM-1)
C Reload WM(1) = RWORK(LWM), since LWM may have changed. -----
  90   IF (MITER .GT. 0) RWORK(LWM) = SQRT(UROUND)
      IF (N .EQ. NYH) GO TO 200
C NEQ was reduced. Zero part of YH to avoid undefined references. -----
  I1 = LYH + L*NYH
  I2 = LYH + (MAXORD + 1)*NYH - 1
  IF (I1 .GT. I2) GO TO 200
  DO 95 I = I1,I2
  95   RWORK(I) = 0.0D0
      GO TO 200
-----
C Block C.
C The next block is for the initial call only (ISTATE = 1).
C It contains all remaining initializations, the initial call to F,
C and the calculation of the initial step size.
C The error weights in EWT are inverted after being loaded.
-----
  100  UROUND = DUMACH()
      TN = T
      IF (ITASK .NE. 4 .AND. ITASK .NE. 5) GO TO 110
      TCRIT = RWORK(1)
      IF ((TCRIT - TOUT)*(TOUT - T) .LT. 0.0D0) GO TO 625
      IF (H0 .NE. 0.0D0 .AND. (T + H0 - TCRIT)*H0 .GT. 0.0D0)
1      H0 = TCRIT - T
  110  JSTART = 0
      IF (MITER .GT. 0) RWORK(LWM) = SQRT(UROUND)
      NHNIL = 0
      NST = 0
      NJE = 0
      NSLAST = 0
      HU = 0.0D0
      NQU = 0
      CCMAX = 0.3D0
      MAXCOR = 3
      MSBP = 20
      MXNCF = 10
C Initial call to F. (LF0 points to YH(*,2).) -----
  LF0 = LYH + NYH
  CALL F (NEQ, T, Y, RWORK(LF0))
  NFE = 1
C Load the initial value vector in YH. -----
  DO 115 I = 1,N
  115  RWORK(I+LYH-1) = Y(I)
C Load and invert the EWT array. (H is temporarily set to 1.0.) -----
  NQ = 1
  H = 1.0D0
  CALL DEWSET (N, ITOL, RTOL, ATOL, RWORK(LYH), RWORK(LEWT))
  DO 120 I = 1,N
      IF (RWORK(I+LEWT-1) .LE. 0.0D0) GO TO 621
  120  RWORK(I+LEWT-1) = 1.0D0/RWORK(I+LEWT-1)
-----
C The coding below computes the step size, H0, to be attempted on the
C first step, unless the user has supplied a value for this.
C First check that TOUT - T differs significantly from zero.
C A scalar tolerance quantity TOL is computed, as MAX(RTOL(I))
C if this is positive, or MAX(ATOL(I)/ABS(Y(I))) otherwise, adjusted
C so as to be between 100*UROUND and 1.0E-3.
C Then the computed value H0 is given by..
C
C      NEQ
C      H0**2 = TOL / ( w0**2 + (1/NEQ) * SUM ( f(i)/ywt(i) )**2 )
C
C where  w0      = MAX ( ABS(T), ABS(TOUT) ),
C         f(i)   = i-th component of initial value of f,
C         ywt(i) = EWT(i)/TOL (a weight for y(i)).

```


C The sign of H0 is inferred from the initial values of TOUT and T.

```

C-----
      IF (H0 .NE. 0.0D0) GO TO 180
      TDIST = ABS(TOUT - T)
      W0 = MAX(ABS(T),ABS(TOUT))
      IF (TDIST .LT. 2.0D0*UROUND*W0) GO TO 622
      TOL = RTOL(1)
      IF (ITOL .LE. 2) GO TO 140
      DO 130 I = 1,N
130    TOL = MAX(TOL,RTOL(I))
140    IF (TOL .GT. 0.0D0) GO TO 160
      ATOLI = ATOL(1)
      DO 150 I = 1,N
          IF (ITOL .EQ. 2 .OR. ITOL .EQ. 4) ATOLI = ATOL(I)
          AYI = ABS(Y(I))
          IF (AYI .NE. 0.0D0) TOL = MAX(TOL,ATOLI/AYI)
150    CONTINUE
160    TOL = MAX(TOL,100.0D0*UROUND)
      TOL = MIN(TOL,0.001D0)
      SUM = DVNORM (N, RWORK(LF0), RWORK(LEWT))
      SUM = 1.0D0/(TOL*W0*W0) + TOL*SUM**2
      H0 = 1.0D0/SQRT(SUM)
      H0 = MIN(H0,TDIST)
      H0 = SIGN(H0,TOUT-T)

```

C Adjust H0 if necessary to meet HMAX bound. -----

```

180    RH = ABS(H0)*HMXI
      IF (RH .GT. 1.0D0) H0 = H0/RH
C Load H with H0 and scale YH(*,2) by H0. -----
      H = H0
      DO 190 I = 1,N
190    RWORK(I+LF0-1) = H0*RWORK(I+LF0-1)
      GO TO 270

```

C-----

C Block D.

C The next code block is for continuation calls only (ISTATE = 2 or 3)
C and is to check stop conditions before taking a step.

```

C-----
200    NSLAST = NST
      GO TO (210, 250, 220, 230, 240), ITASK
210    IF ((TN - TOUT)*H .LT. 0.0D0) GO TO 250
      CALL DINTDY (TOUT, 0, RWORK(LYH), NYH, Y, IFLAG)
      IF (IFLAG .NE. 0) GO TO 627
      T = TOUT
      GO TO 420
220    TP = TN - HU*(1.0D0 + 100.0D0*UROUND)
      IF ((TP - TOUT)*H .GT. 0.0D0) GO TO 623
      IF ((TN - TOUT)*H .LT. 0.0D0) GO TO 250
      GO TO 400
230    TCRIT = RWORK(1)
      IF ((TN - TCRIT)*H .GT. 0.0D0) GO TO 624
      IF ((TCRIT - TOUT)*H .LT. 0.0D0) GO TO 625
      IF ((TN - TOUT)*H .LT. 0.0D0) GO TO 245
      CALL DINTDY (TOUT, 0, RWORK(LYH), NYH, Y, IFLAG)
      IF (IFLAG .NE. 0) GO TO 627
      T = TOUT
      GO TO 420
240    TCRIT = RWORK(1)
      IF ((TN - TCRIT)*H .GT. 0.0D0) GO TO 624
245    HMX = ABS(TN) + ABS(H)
      IHIT = ABS(TN - TCRIT) .LE. 100.0D0*UROUND*HMX
      IF (IHIT) GO TO 400
      TNEXT = TN + H*(1.0D0 + 4.0D0*UROUND)
      IF ((TNEXT - TCRIT)*H .LE. 0.0D0) GO TO 250
      H = (TCRIT - TN)*(1.0D0 - 4.0D0*UROUND)
      IF (ISTATE .EQ. 2) JSTART = -2

```

C-----

C Block E.

```

C The next block is normally executed for all calls and contains
C the call to the one-step core integrator DSTODE.
C
C This is a looping point for the integration steps.
C
C First check for too many steps being taken, update EWT (if not at
C start of problem), check for too much accuracy being requested, and
C check for H below the roundoff level in T.
C-----
250 CONTINUE
   IF ((NST-NSLAST) .GE. MXSTEP) GO TO 500
   CALL DEWSET (N, ITOL, RTOL, ATOL, RWORK(LYH), RWORK(LEWT))
   DO 260 I = 1,N
     IF (RWORK(I+LEWT-1) .LE. 0.0D0) GO TO 510
260   RWORK(I+LEWT-1) = 1.0D0/RWORK(I+LEWT-1)
270   TOLSF = UROUND*DVNORM (N, RWORK(LYH), RWORK(LEWT))
   IF (TOLSF .LE. 1.0D0) GO TO 280
   TOLSF = TOLSF*2.0D0
   IF (NST .EQ. 0) GO TO 626
   GO TO 520
280   IF ((TN + H) .NE. TN) GO TO 290
   NHNIL = NHNIL + 1
   IF (NHNIL .GT. MXHNIL) GO TO 290
   MSG = 'DLSODE- Warning..internal T (=R1) and H (=R2) are'
   CALL XERRWD (MSG, 50, 101, 0, 0, 0, 0, 0, 0.0D0, 0.0D0)
   MSG='      such that in the machine, T + H = T on the next step `
   CALL XERRWD (MSG, 60, 101, 0, 0, 0, 0, 0, 0.0D0, 0.0D0)
   MSG = `      (H = step size). Solver will continue anyway'
   CALL XERRWD (MSG, 50, 101, 0, 0, 0, 0, 2, TN, H)
   IF (NHNIL .LT. MXHNIL) GO TO 290
   MSG = 'DLSODE- Above warning has been issued I1 times. `
   CALL XERRWD (MSG, 50, 102, 0, 0, 0, 0, 0, 0.0D0, 0.0D0)
   MSG = `      It will not be issued again for this problem'
   CALL XERRWD (MSG, 50, 102, 0, 1, MXHNIL, 0, 0, 0.0D0, 0.0D0)
290 CONTINUE
C-----
C CALL DSTODE (NEQ, Y, YH, NYH, YH, EWT, SAVF, ACOR, WM, IWM, F, JAC, DPREPJ, DSOLSY)
C-----
   CALL DSTODE (NEQ, Y, RWORK(LYH), NYH, RWORK(LYH), RWORK(LEWT),
1    RWORK(LSAVF), RWORK(LACOR), RWORK(LWM), IWORK(LIWM),
2    F, JAC, DPREPJ, DSOLSY)
   KGO = 1 - KFLAG
   GO TO (300, 530, 540), KGO
C-----
C Block F.
C The following block handles the case of a successful return from the
C core integrator (KFLAG = 0). Test for stop conditions.
C-----
300 INIT = 1
   GO TO (310, 400, 330, 340, 350), ITASK
C ITASK = 1. If TOUT has been reached, interpolate. -----
310 IF ((TN - TOUT)*H .LT. 0.0D0) GO TO 250
   CALL DINTDY (TOUT, 0, RWORK(LYH), NYH, Y, IFLAG)
   T = TOUT
   GO TO 420
C ITASK = 3. Jump to exit if TOUT was reached. -----
330 IF ((TN - TOUT)*H .GE. 0.0D0) GO TO 400
   GO TO 250
C ITASK = 4. See if TOUT or TCRIT was reached. Adjust H if necessary.
340 IF ((TN - TOUT)*H .LT. 0.0D0) GO TO 345
   CALL DINTDY (TOUT, 0, RWORK(LYH), NYH, Y, IFLAG)
   T = TOUT
   GO TO 420
345 HMX = ABS(TN) + ABS(H)
   IHIT = ABS(TN - TCRIT) .LE. 100.0D0*UROUND*HMX
   IF (IHIT) GO TO 400
   TNEXT = TN + H*(1.0D0 + 4.0D0*UROUND)

```

```

      IF ((TNEXT - TCRIT)*H .LE. 0.0D0) GO TO 250
      H = (TCRIT - TN)*(1.0D0 - 4.0D0*UROUND)
      JSTART = -2
      GO TO 250
C ITASK = 5. See if TCRIT was reached and jump to exit. -----
350 HMX = ABS(TN) + ABS(H)
      IHIT = ABS(TN - TCRIT) .LE. 100.0D0*UROUND*HMX
C-----
C Block G.
C The following block handles all successful returns from DLSODE.
C If ITASK .NE. 1, Y is loaded from YH and T is set accordingly.
C ISTATE is set to 2, the illegal input counter is zeroed, and the
C optional outputs are loaded into the work arrays before returning.
C If ISTATE = 1 and TOUT = T, there is a return with no action taken.
C-----
400 DO 410 I = 1,N
410   Y(I) = RWORK(I+LYH-1)
      T = TN
      IF (ITASK .NE. 4 .AND. ITASK .NE. 5) GO TO 420
      IF (IHIT) T = TCRIT
420 ISTATE = 2
      RWORK(11) = HU
      RWORK(12) = H
      RWORK(13) = TN
      IWORK(11) = NST
      IWORK(12) = NFE
      IWORK(13) = NJE
      IWORK(14) = NQU
      IWORK(15) = NQ
      RETURN
C-----
C Block H.
C The following block handles all unsuccessful returns other than
C those for illegal input. First the error message routine is called.
C If there was an error test or convergence test failure, IMXER is set.
C Then Y is loaded from YH and T is set to TN. The optional outputs
C are loaded into the work arrays before returning.
C-----
C The maximum number of steps was taken before reaching TOUT. -----
500 MSG = 'DLSODE- At current T (=R1), MXSTEP (=I1) steps  \'
      CALL XERRWD (MSG, 50, 201, 0, 0, 0, 0, 0, 0.0D0, 0.0D0)
      MSG = '      taken on this call before reaching TOUT  \'
      CALL XERRWD (MSG, 50, 201, 0, 1, MXSTEP, 0, 1, TN, 0.0D0)
      ISTATE = -1
      GO TO 580
C EWT(I) .LE. 0.0 for some I (not at start of problem). -----
510 EWTI = RWORK(LEWT+I-1)
      MSG = 'DLSODE- At T (=R1), EWT(I1) has become R2 .LE. 0.'
      CALL XERRWD (MSG, 50, 202, 0, 1, I, 0, 2, TN, EWTI)
      ISTATE = -6
      GO TO 580
C Too much accuracy requested for machine precision. -----
520 MSG = 'DLSODE- At T (=R1), too much accuracy requested  \'
      CALL XERRWD (MSG, 50, 203, 0, 0, 0, 0, 0, 0.0D0, 0.0D0)
      MSG = '      for precision of machine.. see TOLSF (=R2)  \'
      CALL XERRWD (MSG, 50, 203, 0, 0, 0, 0, 2, TN, TOLSF)
      RWORK(14) = TOLSF
      ISTATE = -2
      GO TO 580
C KFLAG = -1. Error test failed repeatedly or with ABS(H) = HMIN. -----
530 MSG = 'DLSODE- At T(=R1) and step size H(=R2), the error\'
      CALL XERRWD (MSG, 50, 204, 0, 0, 0, 0, 0, 0.0D0, 0.0D0)
      MSG = '      test failed repeatedly or with ABS(H) = HMIN\'
      CALL XERRWD (MSG, 50, 204, 0, 0, 0, 0, 2, TN, H)
      ISTATE = -4
      GO TO 560
C KFLAG = -2. Convergence failed repeatedly or with ABS(H) = HMIN. -----

```

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540 MSG = 'DLSODE- At T (=R1) and step size H (=R2), the      `
CALL XERRWD (MSG, 50, 205, 0, 0, 0, 0, 0, 0.0D0, 0.0D0)
MSG = `          corrector convergence failed repeatedly    `
CALL XERRWD (MSG, 50, 205, 0, 0, 0, 0, 0, 0.0D0, 0.0D0)
MSG = `          or with ABS(H) = HMIN                       `
CALL XERRWD (MSG, 30, 205, 0, 0, 0, 0, 2, TN, H)
ISTATE = -5
C Compute IMXER if relevant. -----
560 BIG = 0.0D0
    IMXER = 1
    DO 570 I = 1,N
        SIZE = ABS(RWORK(I+LACOR-1)*RWORK(I+LEWT-1))
        IF (BIG .GE. SIZE) GO TO 570
        BIG = SIZE
        IMXER = I
570    CONTINUE
    IWORK(16) = IMXER
C Set Y vector, T, and optional outputs. -----
580 DO 590 I = 1,N
590    Y(I) = RWORK(I+LYH-1)
    T = TN
    RWORK(11) = HU
    RWORK(12) = H
    RWORK(13) = TN
    IWORK(11) = NST
    IWORK(12) = NFE
    IWORK(13) = NJE
    IWORK(14) = NQU
    IWORK(15) = NQ
    RETURN
C-----
C Block I.
C The following block handles all error returns due to illegal input
C (ISTATE = -3), as detected before calling the core integrator.
C First the error message routine is called. If the illegal input
C is a negative ISTATE, the run is aborted (apparent infinite loop).
C-----
601 MSG = 'DLSODE- ISTATE (=I1) illegal `
CALL XERRWD (MSG, 30, 1, 0, 1, ISTATE, 0, 0, 0.0D0, 0.0D0)
IF (ISTATE .LT. 0) GO TO 800
GO TO 700
602 MSG = 'DLSODE- ITASK (=I1) illegal `
CALL XERRWD (MSG, 30, 2, 0, 1, ITASK, 0, 0, 0.0D0, 0.0D0)
GO TO 700
603 MSG = 'DLSODE- ISTATE .GT. 1 but DLSODE not initialized `
CALL XERRWD (MSG, 50, 3, 0, 0, 0, 0, 0, 0.0D0, 0.0D0)
GO TO 700
604 MSG = 'DLSODE- NEQ (=I1) .LT. 1 `
CALL XERRWD (MSG, 30, 4, 0, 1, NEQ(1), 0, 0, 0.0D0, 0.0D0)
GO TO 700
605 MSG = 'DLSODE- ISTATE = 3 and NEQ increased (I1 to I2) `
CALL XERRWD (MSG, 50, 5, 0, 2, N, NEQ(1), 0, 0.0D0, 0.0D0)
GO TO 700
606 MSG = 'DLSODE- ITOL (=I1) illegal `
CALL XERRWD (MSG, 30, 6, 0, 1, ITOL, 0, 0, 0.0D0, 0.0D0)
GO TO 700
607 MSG = 'DLSODE- IOPT (=I1) illegal `
CALL XERRWD (MSG, 30, 7, 0, 1, IOPT, 0, 0, 0.0D0, 0.0D0)
GO TO 700
608 MSG = 'DLSODE- MF (=I1) illegal `
CALL XERRWD (MSG, 30, 8, 0, 1, MF, 0, 0, 0.0D0, 0.0D0)
GO TO 700
609 MSG = 'DLSODE- ML (=I1) illegal.. .LT.0 or .GE.NEQ (=I2)'
CALL XERRWD (MSG, 50, 9, 0, 2, ML, NEQ(1), 0, 0.0D0, 0.0D0)
GO TO 700
610 MSG = 'DLSODE- MU (=I1) illegal.. .LT.0 or .GE.NEQ (=I2)'
CALL XERRWD (MSG, 50, 10, 0, 2, MU, NEQ(1), 0, 0.0D0, 0.0D0)

```

```

GO TO 700
611 MSG = 'DLSODE- MAXORD (=I1) .LT. 0 `
CALL XERRWD (MSG, 30, 11, 0, 1, MAXORD, 0, 0, 0.0D0, 0.0D0)
GO TO 700
612 MSG = 'DLSODE- MXSTEP (=I1) .LT. 0 `
CALL XERRWD (MSG, 30, 12, 0, 1, MXSTEP, 0, 0, 0.0D0, 0.0D0)
GO TO 700
613 MSG = 'DLSODE- MXHNIL (=I1) .LT. 0 `
CALL XERRWD (MSG, 30, 13, 0, 1, MXHNIL, 0, 0, 0.0D0, 0.0D0)
GO TO 700
614 MSG = 'DLSODE- TOUT (=R1) behind T (=R2) `
CALL XERRWD (MSG, 40, 14, 0, 0, 0, 0, 2, TOUT, T)
MSG = ` Integration direction is given by H0 (=R1) `
CALL XERRWD (MSG, 50, 14, 0, 0, 0, 0, 1, H0, 0.0D0)
GO TO 700
615 MSG = 'DLSODE- HMAX (=R1) .LT. 0.0 `
CALL XERRWD (MSG, 30, 15, 0, 0, 0, 0, 1, HMAX, 0.0D0)
GO TO 700
616 MSG = 'DLSODE- HMIN (=R1) .LT. 0.0 `
CALL XERRWD (MSG, 30, 16, 0, 0, 0, 0, 1, HMIN, 0.0D0)
GO TO 700
617 CONTINUE
MSG='DLSODE- RWORK length needed, LENRW (=I1), exceeds LRW (=I2)'
CALL XERRWD (MSG, 60, 17, 0, 2, LENRW, LRW, 0, 0.0D0, 0.0D0)
GO TO 700
618 CONTINUE
MSG='DLSODE- IWORK length needed, LENIW (=I1), exceeds LIW (=I2)'
CALL XERRWD (MSG, 60, 18, 0, 2, LENIW, LIW, 0, 0.0D0, 0.0D0)
GO TO 700
619 MSG = 'DLSODE- RTOL(I1) is R1 .LT. 0.0 `
CALL XERRWD (MSG, 40, 19, 0, 1, I, 0, 1, RTOLI, 0.0D0)
GO TO 700
620 MSG = 'DLSODE- ATOL(I1) is R1 .LT. 0.0 `
CALL XERRWD (MSG, 40, 20, 0, 1, I, 0, 1, ATOLI, 0.0D0)
GO TO 700
621 EWTI = RWORK(LEWT+I-1)
MSG = 'DLSODE- EWT(I1) is R1 .LE. 0.0 `
CALL XERRWD (MSG, 40, 21, 0, 1, I, 0, 1, EWTI, 0.0D0)
GO TO 700
622 CONTINUE
MSG='DLSODE- TOUT (=R1) too close to T(=R2) to start integration'
CALL XERRWD (MSG, 60, 22, 0, 0, 0, 0, 2, TOUT, T)
GO TO 700
623 CONTINUE
MSG='DLSODE- ITASK = I1 and TOUT (=R1) behind TCUR - HU (= R2) `
CALL XERRWD (MSG, 60, 23, 0, 1, ITASK, 0, 2, TOUT, TP)
GO TO 700
624 CONTINUE
MSG='DLSODE- ITASK = 4 OR 5 and TCRIT (=R1) behind TCUR (=R2) `
CALL XERRWD (MSG, 60, 24, 0, 0, 0, 0, 2, TCRIT, TN)
GO TO 700
625 CONTINUE
MSG='DLSODE- ITASK = 4 or 5 and TCRIT (=R1) behind TOUT (=R2) `
CALL XERRWD (MSG, 60, 25, 0, 0, 0, 0, 2, TCRIT, TOUT)
GO TO 700
626 MSG = 'DLSODE- At start of problem, too much accuracy `
CALL XERRWD (MSG, 50, 26, 0, 0, 0, 0, 0, 0.0D0, 0.0D0)
MSG=' requested for precision of machine.. See TOLSF (=R1) `
CALL XERRWD (MSG, 60, 26, 0, 0, 0, 0, 1, TOLSF, 0.0D0)
RWORK(14) = TOLSF
GO TO 700
627 MSG = 'DLSODE- Trouble in DINTDY. ITASK = I1, TOUT = R1'
CALL XERRWD (MSG, 50, 27, 0, 1, ITASK, 0, 1, TOUT, 0.0D0)
C
700 ISTATE = -3
RETURN
C

```

```

800 MSG = 'DLSODE- Run aborted.. apparent infinite loop   '
      CALL XERRWD (MSG, 50, 303, 2, 0, 0, 0, 0, 0.0D0, 0.0D0)
      RETURN
C----- END OF SUBROUTINE DLSODE -----
      END
*DECK DCFODE
      SUBROUTINE DCFODE (METH, ELCO, TESCO)
C***BEGIN PROLOGUE  DCFODE
C***SUBSIDIARY
C***PURPOSE  Set ODE integrator coefficients.
C***LIBRARY  MATHLIB (ODEPACK)
C***TYPE     DOUBLE PRECISION (SCFODE-S, DCFODE-D)
C***AUTHOR  Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C
C  DCFODE is called by the integrator routine to set coefficients
C  needed there.  The coefficients for the current method, as
C  given by the value of METH, are set for all orders and saved.
C  The maximum order assumed here is 12 if METH = 1 and 5 if METH = 2.
C  (A smaller value of the maximum order is also allowed.)
C  DCFODE is called once at the beginning of the problem,
C  and is not called again unless and until METH is changed.
C
C  The ELCO array contains the basic method coefficients.
C  The coefficients el(i), 1 .le. i .le. nq+1, for the method of
C  order nq are stored in ELCO(i,nq).  They are given by a generating
C  polynomial, i.e.,
C      l(x) = el(1) + el(2)*x + ... + el(nq+1)*x**nq.
C  For the implicit Adams methods, l(x) is given by
C      dl/dx = (x+1)*(x+2)*...*(x+nq-1)/factorial(nq-1),    l(-1) = 0.
C  For the BDF methods, l(x) is given by
C      l(x) = (x+1)*(x+2)* ... *(x+nq)/K,
C  where      K = factorial(nq)*(1 + 1/2 + ... + 1/nq).
C
C  The TESCO array contains test constants used for the
C  local error test and the selection of step size and/or order.
C  At order nq, TESCO(k,nq) is used for the selection of step
C  size at order nq - 1 if k = 1, at order nq if k = 2, and at order
C  nq + 1 if k = 3.
C
C***SEE ALSO  DLSODE
C***ROUTINES CALLED  (NONE)
C***REVISION HISTORY  (YMMDD)
C   791129  DATE WRITTEN
C   890501  Modified prologue to SLATEC/LDOC format.  (FNF)
C   890503  Minor cosmetic changes.  (FNF)
C   930809  Renamed to allow single/double precision versions.  (ACH)
C***END PROLOGUE  DCFODE
C**End
      INTEGER METH
      INTEGER I, IB, NQ, NQM1, NQP1
      DOUBLE PRECISION ELCO, TESCO
      DOUBLE PRECISION AGAMQ, FNQ, FNQM1, PC, PINT, RAGQ,
1    RQFAC, RQ1FAC, TSIGN, XPIN
      DIMENSION ELCO(13,12), TESCO(3,12)
      DIMENSION PC(12)
C
C***FIRST EXECUTABLE STATEMENT  DCFODE
      GO TO (100, 200), METH
C
100  ELCO(1,1) = 1.0D0
      ELCO(2,1) = 1.0D0
      TESCO(1,1) = 0.0D0
      TESCO(2,1) = 2.0D0
      TESCO(1,2) = 1.0D0
      TESCO(3,12) = 0.0D0
      PC(1) = 1.0D0

```

```

      RQFAC = 1.0D0
      DO 140 NQ = 2,12
C-----
C The PC array will contain the coefficients of the polynomial
C   p(x) = (x+1)*(x+2)*...*(x+nq-1).
C Initially, p(x) = 1.
C-----
      RQ1FAC = RQFAC
      RQFAC = RQFAC/NQ
      NQM1 = NQ - 1
      FNQM1 = NQM1
      NQP1 = NQ + 1
C Form coefficients of p(x)*(x+nq-1). -----
      PC(NQ) = 0.0D0
      DO 110 IB = 1,NQM1
        I = NQP1 - IB
110      PC(I) = PC(I-1) + FNQM1*PC(I)
      PC(1) = FNQM1*PC(1)
C Compute integral, -1 to 0, of p(x) and x*p(x). -----
      PINT = PC(1)
      XPIN = PC(1)/2.0D0
      TSIGN = 1.0D0
      DO 120 I = 2,NQ
        TSIGN = -TSIGN
        PINT = PINT + TSIGN*PC(I)/I
120      XPIN = XPIN + TSIGN*PC(I)/(I+1)
C Store coefficients in ELCO and TESCO. -----
      ELCO(1,NQ) = PINT*RQ1FAC
      ELCO(2,NQ) = 1.0D0
      DO 130 I = 2,NQ
130      ELCO(I+1,NQ) = RQ1FAC*PC(I)/I
      AGAMQ = RQFAC*XPIN
      RAGQ = 1.0D0/AGAMQ
      TESCO(2,NQ) = RAGQ
      IF (NQ .LT. 12) TESCO(1,NQP1) = RAGQ*RQFAC/NQP1
      TESCO(3,NQM1) = RAGQ
140      CONTINUE
      RETURN
C
200 PC(1) = 1.0D0
      RQ1FAC = 1.0D0
      DO 230 NQ = 1,5
C-----
C The PC array will contain the coefficients of the polynomial
C   p(x) = (x+1)*(x+2)*...*(x+nq).
C Initially, p(x) = 1.
C-----
      FNQ = NQ
      NQP1 = NQ + 1
C form coefficients of p(x)*(x+nq). -----
      PC(NQP1) = 0.0D0
      DO 210 IB = 1,NQ
        I = NQ + 2 - IB
210      PC(I) = PC(I-1) + FNQ*PC(I)
      PC(1) = FNQ*PC(1)
C Store coefficients in ELCO and TESCO. -----
      DO 220 I = 1,NQP1
220      ELCO(I,NQ) = PC(I)/PC(2)
      ELCO(2,NQ) = 1.0D0
      TESCO(1,NQ) = RQ1FAC
      TESCO(2,NQ) = NQP1/ELCO(1,NQ)
      TESCO(3,NQ) = (NQ+2)/ELCO(1,NQ)
      RQ1FAC = RQ1FAC/FNQ
230      CONTINUE
      RETURN
C----- END OF SUBROUTINE DCFODE -----
      END

```

```

*DECK DINTDY
      SUBROUTINE DINTDY (T, K, YH, NYH, DKY, IFLAG)
C***BEGIN PROLOGUE  DINTDY
C***SUBSIDIARY
C***PURPOSE  Interpolate solution derivatives.
C***LIBRARY  MATHLIB (ODEPACK)
C***TYPE     DOUBLE PRECISION (SINTDY-S, DINTDY-D)
C***AUTHOR  Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C
C  DINTDY computes interpolated values of the K-th derivative of the
C  dependent variable vector y, and stores it in DKY.  This routine
C  is called within the package with K = 0 and T = TOUT, but may
C  also be called by the user for any K up to the current order.
C  (See detailed instructions in the usage documentation.)
C
C  The computed values in DKY are gotten by interpolation using the
C  Nordsieck history array YH.  This array corresponds uniquely to a
C  vector-valued polynomial of degree NQCUR or less, and DKY is set
C  to the K-th derivative of this polynomial at T.
C  The formula for DKY is:
C
C      q
C  DKY(i) = sum c(j,K) * (T - tn)**(j-K) * h**(-j) * YH(i,j+1)
C      j=K
C  where c(j,K) = j*(j-1)*...*(j-K+1), q = NQCUR, tn = TCUR, h = HCUR.
C  The quantities nq = NQCUR, l = nq+1, N = NEQ, tn, and h are
C  communicated by COMMON.  The above sum is done in reverse order.
C  IFLAG is returned negative if either K or T is out of bounds.
C
C***SEE ALSO  DLSODE
C***ROUTINES CALLED  XERRWD
C***COMMON BLOCKS  DLS001
C***REVISION HISTORY  (YMMDD)
C   791129  DATE WRITTEN
C   890501  Modified prologue to SLATEC/LDOC format.  (FNF)
C   890503  Minor cosmetic changes.  (FNF)
C   930809  Renamed to allow single/double precision versions.  (ACH)
C***END PROLOGUE  DINTDY
C**End
      INTEGER K, NYH, IFLAG
      INTEGER IOWND, IOWNS,
1     ICF, IERPJ, IERSL, JCUR, JSTART, KFLAG, L, METH, MITER,
2     MAXORD, MAXCOR, MSBP, MXNCF, N, NQ, NST, NFE, NJE, NQU
      INTEGER I, IC, J, JB, JB2, JJ, JJ1, JP1
      DOUBLE PRECISION T, YH, DKY
      DOUBLE PRECISION ROWNS,
1     CCMAX, EL0, H, HMIN, HMXI, HU, RC, TN, UROUND
      DOUBLE PRECISION C, R, S, TP
      CHARACTER*80 MSG
      DIMENSION YH(NYH,*), DKY(*)
      COMMON /DLS001/ ROWNS(209),
2     CCMAX, EL0, H, HMIN, HMXI, HU, RC, TN, UROUND,
3     IOWND(12), IOWNS(6),
4     ICF, IERPJ, IERSL, JCUR, JSTART, KFLAG, L, METH, MITER,
5     MAXORD, MAXCOR, MSBP, MXNCF, N, NQ, NST, NFE, NJE, NQU
C
C***FIRST EXECUTABLE STATEMENT  DINTDY
      IFLAG = 0
      IF (K .LT. 0 .OR. K .GT. NQ) GO TO 80
      TP = TN - HU - 100.0D0*UROUND*(TN + HU)
      IF ((T-TP)*(T-TN) .GT. 0.0D0) GO TO 90
C
      S = (T - TN)/H
      IC = 1
      IF (K .EQ. 0) GO TO 15
      JJ1 = L - K
      DO 10 JJ = JJ1,NQ

```



```

10     IC = IC*JJ
15     C = IC
      DO 20 I = 1,N
20     DKY(I) = C*YH(I,L)
      IF (K .EQ. NQ) GO TO 55
      JB2 = NQ - K
      DO 50 JB = 1,JB2
        J = NQ - JB
        JP1 = J + 1
        IC = 1
        IF (K .EQ. 0) GO TO 35
        JJ1 = JP1 - K
        DO 30 JJ = JJ1,J
30     IC = IC*JJ
35     C = IC
      DO 40 I = 1,N
40     DKY(I) = C*YH(I,JP1) + S*DKY(I)
50     CONTINUE
      IF (K .EQ. 0) RETURN
55     R = H*(-K)
      DO 60 I = 1,N
60     DKY(I) = R*DKY(I)
      RETURN
C
80     MSG = 'DINTDY- K (=I1) illegal      '
      CALL XERRWD (MSG, 30, 51, 0, 1, K, 0, 0, 0.0D0, 0.0D0)
      IFLAG = -1
      RETURN
90     MSG = 'DINTDY- T (=R1) illegal      '
      CALL XERRWD (MSG, 30, 52, 0, 0, 0, 0, 1, T, 0.0D0)
      MSG='      T not in interval TCUR - HU (= R1) to TCUR (=R2)      '
      CALL XERRWD (MSG, 60, 52, 0, 0, 0, 0, 2, TP, TN)
      IFLAG = -2
      RETURN
C----- END OF SUBROUTINE DINTDY -----
      END
*DECK DPREPJ
      SUBROUTINE DPREPJ (NEQ, Y, YH, NYH, EWT, FTEM, SAVF, WM, IWM,
1     F, JAC)
C***BEGIN PROLOGUE  DPREPJ
C***SUBSIDIARY
C***PURPOSE  Compute and process Newton iteration matrix.
C***LIBRARY  MATHLIB (ODEPACK)
C***TYPE     DOUBLE PRECISION (SPREPJ-S, DPREPJ-D)
C***AUTHOR  Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C
C  DPREPJ is called by DSTODE to compute and process the matrix
C   $P = I - h*el(1)*J$ , where J is an approximation to the Jacobian.
C  Here J is computed by the user-supplied routine JAC if
C  MITER = 1 or 4, or by finite differencing if MITER = 2, 3, or 5.
C  If MITER = 3, a diagonal approximation to J is used.
C  J is stored in WM and replaced by P.  If MITER .ne. 3, P is then
C  subjected to LU decomposition in preparation for later solution
C  of linear systems with P as coefficient matrix.  This is done
C  by DGEFA if MITER = 1 or 2, and by DGBFA if MITER = 4 or 5.
C
C  In addition to variables described in DSTODE and DLSODE prologues,
C  communication with DPREPJ uses the following:
C  Y      = array containing predicted values on entry.
C  FTEM   = work array of length N (ACOR in DSTODE).
C  SAVF   = array containing f evaluated at predicted y.
C  WM     = real work space for matrices.  On output it contains the
C          inverse diagonal matrix if MITER = 3 and the LU decomposition
C          of P if MITER is 1, 2, 4, or 5.
C          Storage of matrix elements starts at WM(3).
C          WM also contains the following matrix-related data:

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C      WM(1) = SQRT(UROUND), used in numerical Jacobian increments.
C      WM(2) = H*EL0, saved for later use if MITER = 3.
C      IWM  = integer work space containing pivot information, starting at
C      IWM(21), if MITER is 1, 2, 4, or 5. IWM also contains band
C      parameters ML = IWM(1) and MU = IWM(2) if MITER is 4 or 5.
C      ELO  = EL(1) (input).
C      IERPJ = output error flag, = 0 if no trouble, .gt. 0 if
C      P matrix found to be singular.
C      JCUR  = output flag = 1 to indicate that the Jacobian matrix
C      (or approximation) is now current.
C      This routine also uses the COMMON variables EL0, H, TN, UROUND,
C      MITER, N, NFE, and NJE.
C
C***SEE ALSO  DLSODE
C***ROUTINES CALLED  DGBFA, DGEFA, DVNORM
C***COMMON BLOCKS  DLS001
C***REVISION HISTORY  (YYMMDD)
C  791129  DATE WRITTEN
C  890501  Modified prologue to SLATEC/LDOC format.  (FNF)
C  890504  Minor cosmetic changes.  (FNF)
C  930809  Renamed to allow single/double precision versions.  (ACH)
C***END PROLOGUE  DPREPJ
C**End
      EXTERNAL F, JAC
      INTEGER NEQ, NYH, IWM
      INTEGER IOWND, IOWNS,
1     ICF, IERPJ, IERSL, JCUR, JSTART, KFLAG, L, METH, MITER,
2     MAXORD, MAXCOR, MSBP, MXNCF, N, NQ, NST, NFE, NJE, NQU
      INTEGER I, I1, I2, IER, II, J, J1, JJ, LENP,
1     MBA, MBAND, MEB1, MEBAND, ML, ML3, MU, NP1
      DOUBLE PRECISION Y, YH, EWT, FTEM, SAVF, WM
      DOUBLE PRECISION ROWNS,
1     CCMAX, EL0, H, HMIN, HMXI, HU, RC, TN, UROUND
      DOUBLE PRECISION CON, DI, FAC, HL0, R, R0, SRUR, YI, YJ, YJJ,
1     DVNORM
      DIMENSION NEQ(*), Y(*), YH(NYH,*), EWT(*), FTEM(*), SAVF(*),
1     WM(*), IWM(*)
      COMMON /DLS001/ ROWNS(209),
2     CCMAX, EL0, H, HMIN, HMXI, HU, RC, TN, UROUND,
3     IOWND(12), IOWNS(6),
4     ICF, IERPJ, IERSL, JCUR, JSTART, KFLAG, L, METH, MITER,
5     MAXORD, MAXCOR, MSBP, MXNCF, N, NQ, NST, NFE, NJE, NQU
C
C***FIRST EXECUTABLE STATEMENT  DPREPJ
      NJE = NJE + 1
      IERPJ = 0
      JCUR = 1
      HL0 = H*ELO
      GO TO (100, 200, 300, 400, 500), MITER
C If MITER = 1, call JAC and multiply by scalar. -----
100  LENP = N*N
      DO 110 I = 1,LENP
110   WM(I+2) = 0.0D0
      CALL JAC (NEQ, TN, Y, 0, 0, WM(3), N)
      CON = -HL0
      DO 120 I = 1,LENP
120   WM(I+2) = WM(I+2)*CON
      GO TO 240
C If MITER = 2, make N calls to F to approximate J. -----
200  FAC = DVNORM (N, SAVF, EWT)
      R0 = 1000.0D0*ABS(H)*UROUND*N*FAC
      IF (R0 .EQ. 0.0D0) R0 = 1.0D0
      SRUR = WM(1)
      J1 = 2
      DO 230 J = 1,N
          YJ = Y(J)
          R = MAX(SRUR*ABS(YJ),R0/EWT(J))

```

```

        Y(J) = Y(J) + R
        FAC = -HL0/R
        CALL F (NEQ, TN, Y, FTEM)
        DO 220 I = 1,N
220     WM(I+J1) = (FTEM(I) - SAVF(I))*FAC
        Y(J) = YJ
        J1 = J1 + N
230     CONTINUE
        NFE = NFE + N
C Add identity matrix. -----
240     J = 3
        NP1 = N + 1
        DO 250 I = 1,N
            WM(J) = WM(J) + 1.0D0
250     J = J + NP1
C Do LU decomposition on P. -----
        CALL DGEFA (WM(3), N, N, IWM(21), IER)
        IF (IER .NE. 0) IERPJ = 1
        RETURN
C If MITER = 3, construct a diagonal approximation to J and P. -----
300     WM(2) = HL0
        R = EL0*0.1D0
        DO 310 I = 1,N
310     Y(I) = Y(I) + R*(H*SAVF(I) - YH(I,2))
        CALL F (NEQ, TN, Y, WM(3))
        NFE = NFE + 1
        DO 320 I = 1,N
            R0 = H*SAVF(I) - YH(I,2)
            DI = 0.1D0*R0 - H*(WM(I+2) - SAVF(I))
            WM(I+2) = 1.0D0
            IF (ABS(R0) .LT. UROUND/EWT(I)) GO TO 320
            IF (ABS(DI) .EQ. 0.0D0) GO TO 330
            WM(I+2) = 0.1D0*R0/DI
320     CONTINUE
        RETURN
330     IERPJ = 1
        RETURN
C If MITER = 4, call JAC and multiply by scalar. -----
400     ML = IWM(1)
        MU = IWM(2)
        ML3 = ML + 3
        MBAND = ML + MU + 1
        MEBAND = MBAND + ML
        LENP = MEBAND*N
        DO 410 I = 1,LENP
410     WM(I+2) = 0.0D0
        CALL JAC (NEQ, TN, Y, ML, MU, WM(ML3), MEBAND)
        CON = -HL0
        DO 420 I = 1,LENP
420     WM(I+2) = WM(I+2)*CON
        GO TO 570
C If MITER = 5, make MBAND calls to F to approximate J. -----
500     ML = IWM(1)
        MU = IWM(2)
        MBAND = ML + MU + 1
        MBA = MIN(MBAND,N)
        MEBAND = MBAND + ML
        MEB1 = MEBAND - 1
        SRUR = WM(1)
        FAC = DVNORM (N, SAVF, EWT)
        R0 = 1000.0D0*ABS(H)*UROUND*N*FAC
        IF (R0 .EQ. 0.0D0) R0 = 1.0D0
        DO 560 J = 1,MBA
            DO 530 I = J,N,MBAND
                YI = Y(I)
                R = MAX(SRUR*ABS(YI),R0/EWT(I))
530     Y(I) = Y(I) + R

```

```

CALL F (NEQ, TN, Y, FTEM)
DO 550 JJ = J,N,MBAND
  Y(JJ) = YH(JJ,1)
  YJJ = Y(JJ)
  R = MAX(SRUR*ABS(YJJ),R0/EWT(JJ))
  FAC = -HL0/R
  I1 = MAX(JJ-MU,1)
  I2 = MIN(JJ+ML,N)
  II = JJ*MEB1 - ML + 2
  DO 540 I = I1,I2
540   WM(II+I) = (FTEM(I) - SAVF(I))*FAC
550   CONTINUE
560   CONTINUE
      NFE = NFE + MBA
C Add identity matrix. -----
570   II = MBAND + 2
      DO 580 I = 1,N
          WM(II) = WM(II) + 1.0D0
580   II = II + MEBAND
C Do LU decomposition of P. -----
      CALL DGBFA (WM(3), MEBAND, N, ML, MU, IWM(21), IER)
      IF (IER .NE. 0) IERPJ = 1
      RETURN
C----- END OF SUBROUTINE DPREPJ -----
      END
*DECK DSOLSY
      SUBROUTINE DSOLSY (WM, IWM, X, TEM)
C***BEGIN PROLOGUE  DSOLSY
C***SUBSIDIARY
C***PURPOSE  ODEPACK linear system solver.
C***LIBRARY  MATHLIB (ODEPACK)
C***TYPE     DOUBLE PRECISION (SSOLSY-S, DSOLSY-D)
C***AUTHOR  Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C
C This routine manages the solution of the linear system arising from
C a chord iteration. It is called if MITER .ne. 0.
C If MITER is 1 or 2, it calls DGESL to accomplish this.
C If MITER = 3 it updates the coefficient h*EL0 in the diagonal
C matrix, and then computes the solution.
C If MITER is 4 or 5, it calls DGBSL.
C Communication with DSOLSY uses the following variables:
C WM = real work space containing the inverse diagonal matrix if
C MITER = 3 and the LU decomposition of the matrix otherwise.
C Storage of matrix elements starts at WM(3).
C WM also contains the following matrix-related data:
C WM(1) = SQRT(UROUND) (not used here),
C WM(2) = HL0, the previous value of h*EL0, used if MITER = 3.
C IWM = integer work space containing pivot information, starting at
C IWM(21), if MITER is 1, 2, 4, or 5. IWM also contains band
C parameters ML = IWM(1) and MU = IWM(2) if MITER is 4 or 5.
C X = the right-hand side vector on input, and the solution vector
C on output, of length N.
C TEM = vector of work space of length N, not used in this version.
C IERSL = output flag (in COMMON). IERSL = 0 if no trouble occurred.
C IERSL = 1 if a singular matrix arose with MITER = 3.
C This routine also uses the COMMON variables EL0, H, MITER, and N.
C
C***SEE ALSO  DLSODE
C***ROUTINES CALLED  DGBSL, DGESL
C***COMMON BLOCKS  DLS001
C***REVISION HISTORY  (YYMMDD)
C 791129 DATE WRITTEN
C 890501 Modified prologue to SLATEC/LDOC format. (FNF)
C 890503 Minor cosmetic changes. (FNF)
C 930809 Renamed to allow single/double precision versions. (ACH)
C***END PROLOGUE  DSOLSY

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C**End
      INTEGER IWM
      INTEGER IOWND, IOWNS,
1     ICF, IERPJ, IERSL, JCUR, JSTART, KFLAG, L, METH, MITER,
2     MAXORD, MAXCOR, MSBP, MXNCF, N, NQ, NST, NFE, NJE, NQU
      INTEGER I, MEBAND, ML, MU
      DOUBLE PRECISION WM, X, TEM
      DOUBLE PRECISION ROWNS,
1     CCMAX, EL0, H, HMIN, HMXI, HU, RC, TN, UROUND
      DOUBLE PRECISION DI, HL0, PHL0, R
      DIMENSION WM(*), IWM(*), X(*), TEM(*)
      COMMON /DLS001/ ROWNS(209),
2     CCMAX, EL0, H, HMIN, HMXI, HU, RC, TN, UROUND,
3     IOWND(12), IOWNS(6),
4     ICF, IERPJ, IERSL, JCUR, JSTART, KFLAG, L, METH, MITER,
5     MAXORD, MAXCOR, MSBP, MXNCF, N, NQ, NST, NFE, NJE, NQU
C
C***FIRST EXECUTABLE STATEMENT  DSOLSY
      IERSL = 0
      GO TO (100, 100, 300, 400, 400), MITER
100  CALL DGESL (WM(3), N, N, IWM(21), X, 0)
      RETURN
C
300  PHL0 = WM(2)
      HL0 = H*EL0
      WM(2) = HL0
      IF (HL0 .EQ. PHL0) GO TO 330
      R = HL0/PHL0
      DO 320 I = 1,N
          DI = 1.0D0 - R*(1.0D0 - 1.0D0/WM(I+2))
          IF (ABS(DI) .EQ. 0.0D0) GO TO 390
320  WM(I+2) = 1.0D0/DI
330  DO 340 I = 1,N
340  X(I) = WM(I+2)*X(I)
      RETURN
390  IERSL = 1
      RETURN
C
400  ML = IWM(1)
      MU = IWM(2)
      MEBAND = 2*ML + MU + 1
      CALL DGBSL (WM(3), MEBAND, N, ML, MU, IWM(21), X, 0)
      RETURN
C----- END OF SUBROUTINE DSOLSY -----
      END
*DECK DSRCOM
      SUBROUTINE DSRCOM (RSAV, ISAV, JOB)
C***BEGIN PROLOGUE  DSRCOM
C***SUBSIDIARY
C***PURPOSE  Save/restore ODEPACK COMMON blocks.
C***LIBRARY  MATHLIB (ODEPACK)
C***TYPE     DOUBLE PRECISION (SSRCOM-S, DSRCOM-D)
C***AUTHOR  Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C
C  This routine saves or restores (depending on JOB) the contents of
C  the COMMON block DLS001, which is used internally
C  by one or more ODEPACK solvers.
C
C  RSAV = real array of length 218 or more.
C  ISAV = integer array of length 37 or more.
C  JOB = flag indicating to save or restore the COMMON blocks:
C        JOB = 1 if COMMON is to be saved (written to RSAV/ISAV)
C        JOB = 2 if COMMON is to be restored (read from RSAV/ISAV)
C        A call with JOB = 2 presumes a prior call with JOB = 1.
C
C***SEE ALSO  DLSODE

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C***ROUTINES CALLED (NONE)
C***COMMON BLOCKS DLS001
C***REVISION HISTORY (YYMMDD)
C 791129 DATE WRITTEN
C 890501 Modified prologue to SLATEC/LDOC format. (FNF)
C 890503 Minor cosmetic changes. (FNF)
C 921116 Deleted treatment of block /EH0001/. (ACH)
C 930801 Reduced Common block length by 2. (ACH)
C 930809 Renamed to allow single/double precision versions. (ACH)
C***END PROLOGUE DSRCOM
C**End
      INTEGER ISAV, JOB
      INTEGER ILS
      INTEGER I, LENILS, LENRLS
      DOUBLE PRECISION RSAV, RLS
      DIMENSION RSAV(*), ISAV(*)
      COMMON /DLS001/ RLS(218), ILS(37)
      DATA LENRLS/218/, LENILS/37/

C
C***FIRST EXECUTABLE STATEMENT DSRCOM
      IF (JOB .EQ. 2) GO TO 100

C
      DO 10 I = 1,LENRLS
10      RSAV(I) = RLS(I)
      DO 20 I = 1,LENILS
20      ISAV(I) = ILS(I)
      RETURN

C
100 CONTINUE
      DO 110 I = 1,LENRLS
110      RLS(I) = RSAV(I)
      DO 120 I = 1,LENILS
120      ILS(I) = ISAV(I)
      RETURN

C----- END OF SUBROUTINE DSRCOM -----
      END
*DECK DSTODE
      SUBROUTINE DSTODE (NEQ, Y, YH, NYH, YH1, EWT, SAVF, ACOR,
1 WM, IWM, F, JAC, PJAC, SLVS)
C***BEGIN PROLOGUE DSTODE
C***SUBSIDIARY
C***PURPOSE Performs one step of an ODEPACK integration.
C***LIBRARY MATHLIB (ODEPACK)
C***TYPE DOUBLE PRECISION (SSTODE-S, DSTODE-D)
C***AUTHOR Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C
C DSTODE performs one step of the integration of an initial value
C problem for a system of ordinary differential equations.
C Note: DSTODE is independent of the value of the iteration method
C indicator MITER, when this is .ne. 0, and hence is independent
C of the type of chord method used, or the Jacobian structure.
C Communication with DSTODE is done with the following variables:
C
C NEQ = integer array containing problem size in NEQ(1), and
C passed as the NEQ argument in all calls to F and JAC.
C Y = an array of length .ge. N used as the Y argument in
C all calls to F and JAC.
C YH = an NYH by LMAX array containing the dependent variables
C and their approximate scaled derivatives, where
C LMAX = MAXORD + 1. YH(i,j+1) contains the approximate
C j-th derivative of y(i), scaled by h**j/factorial(j)
C (j = 0,1,...,NQ). on entry for the first step, the first
C two columns of YH must be set from the initial values.
C NYH = a constant integer .ge. N, the first dimension of YH.
C YH1 = a one-dimensional array occupying the same space as YH.
C EWT = an array of length N containing multiplicative weights

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C          for local error measurements. Local errors in Y(i) are
C          compared to 1.0/EWT(i) in various error tests.
C  SAVF    = an array of working storage, of length N.
C          Also used for input of YH(*,MAXORD+2) when JSTART = -1
C          and MAXORD .lt. the current order NQ.
C  ACOR    = a work array of length N, used for the accumulated
C          corrections. On a successful return, ACOR(i) contains
C          the estimated one-step local error in Y(i).
C  WM,IWM  = real and integer work arrays associated with matrix
C          operations in chord iteration (MITER .ne. 0).
C  PJAC    = name of routine to evaluate and preprocess Jacobian matrix
C          and  $P = I - h \cdot e_{10} \cdot JAC$ , if a chord method is being used.
C  SLVS    = name of routine to solve linear system in chord iteration.
C  CCMAX   = maximum relative change in  $h \cdot e_{10}$  before PJAC is called.
C  H       = the step size to be attempted on the next step.
C          H is altered by the error control algorithm during the
C          problem. H can be either positive or negative, but its
C          sign must remain constant throughout the problem.
C  HMIN    = the minimum absolute value of the step size h to be used.
C  HMXI    = inverse of the maximum absolute value of h to be used.
C          HMXI = 0.0 is allowed and corresponds to an infinite hmax.
C          HMIN and HMXI may be changed at any time, but will not
C          take effect until the next change of h is considered.
C  TN      = the independent variable. TN is updated on each step taken.
C  JSTART  = an integer used for input only, with the following
C          values and meanings:
C          0 perform the first step.
C          .gt.0 take a new step continuing from the last.
C          -1 take the next step with a new value of H, MAXORD,
C             N, METH, MITER, and/or matrix parameters.
C          -2 take the next step with a new value of H,
C             but with other inputs unchanged.
C          On return, JSTART is set to 1 to facilitate continuation.
C  KFLAG   = a completion code with the following meanings:
C          0 the step was succesful.
C          -1 the requested error could not be achieved.
C          -2 corrector convergence could not be achieved.
C          -3 fatal error in PJAC or SLVS.
C          A return with KFLAG = -1 or -2 means either
C          abs(H) = HMIN or 10 consecutive failures occurred.
C          On a return with KFLAG negative, the values of TN and
C          the YH array are as of the beginning of the last
C          step, and H is the last step size attempted.
C  MAXORD  = the maximum order of integration method to be allowed.
C  MAXCOR  = the maximum number of corrector iterations allowed.
C  MSBP    = maximum number of steps between PJAC calls (MITER .gt. 0).
C  MXNCF   = maximum number of convergence failures allowed.
C  METH/MITER = the method flags. See description in driver.
C  N       = the number of first-order differential equations.
C  The values of CCMAX, H, HMIN, HMXI, TN, JSTART, KFLAG, MAXORD,
C  MAXCOR, MSBP, MXNCF, METH, MITER, and N are communicated via COMMON.
C
C***SEE ALSO  DLSODE
C***ROUTINES CALLED  DCFODE, DVNORM
C***COMMON BLOCKS  DLS001
C***REVISION HISTORY  (YYMMDD)
C  791129  DATE WRITTEN
C  890501  Modified prologue to SLATEC/LDOC format.  (FNF)
C  890503  Minor cosmetic changes.  (FNF)
C  930809  Renamed to allow single/double precision versions.  (ACH)
C***END PROLOGUE  DSTODE
C**End
EXTERNAL F, JAC, PJAC, SLVS
INTEGER NEQ, NYH, IWM
INTEGER IOWND, IALTH, IPUP, LMAX, MEO, NQNYH, NSLP,
1  ICF, IERPJ, IERSL, JCUR, JSTART, KFLAG, L, METH, MITER,
2  MAXORD, MAXCOR, MSBP, MXNCF, N, NQ, NST, NFE, NJE, NQU

```

```

INTEGER I, I1, IREDO, IRET, J, JB, M, NCF, NEWQ
DOUBLE PRECISION Y, YH, YH1, EWT, SAVF, ACOR, WM
DOUBLE PRECISION CONIT, CRATE, EL, ELCO, HOLD, RMAX, TESCO,
2  CCMAX, EL0, H, HMIN, HMXI, HU, RC, TN, UROUND
DOUBLE PRECISION DCON, DDN, DEL, DELP, DSM, DUP, EXDN, EXSM, EXUP,
1  R, RH, RHDN, RHSM, RHUP, TOLD, DVNORM
DIMENSION NEQ(*), Y(*), YH(NYH,*), YH1(*), EWT(*), SAVF(*),
1  ACOR(*), WM(*), IWM(*)
COMMON /DLS001/ CONIT, CRATE, EL(13), ELCO(13,12),
1  HOLD, RMAX, TESCO(3,12),
2  CCMAX, EL0, H, HMIN, HMXI, HU, RC, TN, UROUND, IOWND(12),
3  IALTH, IPUP, LMAX, MEO, NQNYH, NSLP,
4  ICF, IERPJ, IERSL, JCUR, JSTART, KFLAG, L, METH, MITER,
5  MAXORD, MAXCOR, MSBP, MXNCF, N, NQ, NST, NFE, NJE, NQU

```

C

C***FIRST EXECUTABLE STATEMENT DSTODE

```

KFLAG = 0
TOLD = TN
NCF = 0
IERPJ = 0
IERSL = 0
JCUR = 0
ICF = 0
DELP = 0.0D0
IF (JSTART .GT. 0) GO TO 200
IF (JSTART .EQ. -1) GO TO 100
IF (JSTART .EQ. -2) GO TO 160

```

C-----

C On the first call, the order is set to 1, and other variables are
C initialized. RMAX is the maximum ratio by which H can be increased
C in a single step. It is initially 1.E4 to compensate for the small
C initial H, but then is normally equal to 10. If a failure
C occurs (in corrector convergence or error test), RMAX is set to 2
C for the next increase.

C-----

```

LMAX = MAXORD + 1
NQ = 1
L = 2
IALTH = 2
RMAX = 10000.0D0
RC = 0.0D0
EL0 = 1.0D0
CRATE = 0.7D0
HOLD = H
MEO = METH
NSLP = 0
IPUP = MITER
IRET = 3
GO TO 140

```

C-----

C The following block handles preliminaries needed when JSTART = -1.
C IPUP is set to MITER to force a matrix update.
C If an order increase is about to be considered (IALTH = 1),
C IALTH is reset to 2 to postpone consideration one more step.
C If the caller has changed METH, DCFODE is called to reset
C the coefficients of the method.
C If the caller has changed MAXORD to a value less than the current
C order NQ, NQ is reduced to MAXORD, and a new H chosen accordingly.
C If H is to be changed, YH must be rescaled.
C If H or METH is being changed, IALTH is reset to L = NQ + 1
C to prevent further changes in H for that many steps.

C-----

```

100 IPUP = MITER
LMAX = MAXORD + 1
IF (IALTH .EQ. 1) IALTH = 2
IF (METH .EQ. MEO) GO TO 110
CALL DCFODE (METH, ELCO, TESCO)

```



```

MEO = METH
IF (NQ .GT. MAXORD) GO TO 120
IALTH = L
IRET = 1
GO TO 150
110 IF (NQ .LE. MAXORD) GO TO 160
120 NQ = MAXORD
L = LMAX
DO 125 I = 1,L
125  EL(I) = ELCO(I,NQ)
NQNYH = NQ*NYH
RC = RC*EL(1)/EL0
EL0 = EL(1)
CONIT = 0.5D0/(NQ+2)
DDN = DVNORM(N, SAVF, EWT)/TESCO(1,L)
EXDN = 1.0D0/L
RHDN = 1.0D0/(1.3D0*DDN**EXDN + 0.0000013D0)
RH = MIN(RHDN,1.0D0)
IREDO = 3
IF (H .EQ. HOLD) GO TO 170
RH = MIN(RH,ABS(H/HOLD))
H = HOLD
GO TO 175
C-----
C DCFODE is called to get all the integration coefficients for the
C current METH. Then the EL vector and related constants are reset
C whenever the order NQ is changed, or at the start of the problem.
C-----
140 CALL DCFODE (METH, ELCO, TESCO)
150 DO 155 I = 1,L
155  EL(I) = ELCO(I,NQ)
NQNYH = NQ*NYH
RC = RC*EL(1)/EL0
EL0 = EL(1)
CONIT = 0.5D0/(NQ+2)
GO TO (160, 170, 200), IRET
C-----
C If H is being changed, the H ratio RH is checked against
C RMAX, HMIN, and HMXI, and the YH array rescaled. IALTH is set to
C L = NQ + 1 to prevent a change of H for that many steps, unless
C forced by a convergence or error test failure.
C-----
160 IF (H .EQ. HOLD) GO TO 200
RH = H/HOLD
H = HOLD
IREDO = 3
GO TO 175
170 RH = MAX(RH,HMIN/ABS(H))
175 RH = MIN(RH,RMAX)
RH = RH/MAX(1.0D0,ABS(H)*HMXI*RH)
R = 1.0D0
DO 180 J = 2,L
R = R*RH
DO 180 I = 1,N
180  YH(I,J) = YH(I,J)*R
H = H*RH
RC = RC*RH
IALTH = L
IF (IREDO .EQ. 0) GO TO 690
C-----
C This section computes the predicted values by effectively
C multiplying the YH array by the Pascal Triangle matrix.
C RC is the ratio of new to old values of the coefficient H*EL(1).
C When RC differs from 1 by more than CCMAX, IPUP is set to MITER
C to force PJAC to be called, if a Jacobian is involved.
C In any case, PJAC is called at least every MSBP steps.
C-----

```

```

200 IF (ABS(RC-1.0D0) .GT. CCMAX) IPUP = MITER
    IF (NST .GE. NSLP+MSBP) IPUP = MITER
    TN = TN + H
    I1 = NQNYH + 1
    DO 215 JB = 1,NQ
        I1 = I1 - NYH
Cdir$ ivdep
        DO 210 I = I1,NQNYH
210     YH1(I) = YH1(I) + YH1(I+NYH)
215     CONTINUE
C-----
C Up to MAXCOR corrector iterations are taken. A convergence test is
C made on the R.M.S. norm of each correction, weighted by the error
C weight vector EWT. The sum of the corrections is accumulated in the
C vector ACOR(i). The YH array is not altered in the corrector loop.
C-----
220 M = 0
    DO 230 I = 1,N
230     Y(I) = YH(I,1)
        CALL F (NEQ, TN, Y, SAVF)
        NFE = NFE + 1
        IF (IPUP .LE. 0) GO TO 250
C-----
C If indicated, the matrix P = I - h*el(1)*J is reevaluated and
C preprocessed before starting the corrector iteration. IPUP is set
C to 0 as an indicator that this has been done.
C-----
        CALL PJAC (NEQ, Y, YH, NYH, EWT, ACOR, SAVF, WM, IWM, F, JAC)
        IPUP = 0
        RC = 1.0D0
        NSLP = NST
        CRATE = 0.7D0
        IF (IERPJ .NE. 0) GO TO 430
250 DO 260 I = 1,N
260     ACOR(I) = 0.0D0
270 IF (MITER .NE. 0) GO TO 350
C-----
C In the case of functional iteration, update Y directly from
C the result of the last function evaluation.
C-----
        DO 290 I = 1,N
            SAVF(I) = H*SAVF(I) - YH(I,2)
290     Y(I) = SAVF(I) - ACOR(I)
        DEL = DVNORM (N, Y, EWT)
        DO 300 I = 1,N
            Y(I) = YH(I,1) + EL(1)*SAVF(I)
300     ACOR(I) = SAVF(I)
        GO TO 400
C-----
C In the case of the chord method, compute the corrector error,
C and solve the linear system with that as right-hand side and
C P as coefficient matrix.
C-----
350 DO 360 I = 1,N
360     Y(I) = H*SAVF(I) - (YH(I,2) + ACOR(I))
        CALL SLVS (WM, IWM, Y, SAVF)
        IF (IERSL .LT. 0) GO TO 430
        IF (IERSL .GT. 0) GO TO 410
        DEL = DVNORM (N, Y, EWT)
        DO 380 I = 1,N
            ACOR(I) = ACOR(I) + Y(I)
380     Y(I) = YH(I,1) + EL(1)*ACOR(I)
C-----
C Test for convergence. If M.gt.0, an estimate of the convergence
C rate constant is stored in CRATE, and this is used in the test.
C-----
400 IF (M .NE. 0) CRATE = MAX(0.2D0*CRATE,DEL/DELP)

```

```

DCON = DEL*MIN(1.0D0,1.5D0*CRATE)/(TESCO(2,NQ)*CONIT)
IF (DCON .LE. 1.0D0) GO TO 450
M = M + 1
IF (M .EQ. MAXCOR) GO TO 410
IF (M .GE. 2 .AND. DEL .GT. 2.0D0*DELP) GO TO 410
DELP = DEL
CALL F (NEQ, TN, Y, SAVF)
NFE = NFE + 1
GO TO 270
C-----
C The corrector iteration failed to converge.
C If MITER .ne. 0 and the Jacobian is out of date, PJAC is called for
C the next try. Otherwise the YH array is retracted to its values
C before prediction, and H is reduced, if possible. If H cannot be
C reduced or MXNCF failures have occurred, exit with KFLAG = -2.
C-----
410 IF (MITER .EQ. 0 .OR. JCUR .EQ. 1) GO TO 430
    ICF = 1
    IPUP = MITER
    GO TO 220
430 ICF = 2
    NCF = NCF + 1
    RMAX = 2.0D0
    TN = TOLD
    I1 = NQNYH + 1
    DO 445 JB = 1,NQ
        I1 = I1 - NYH
Cdir$ ivdep
    DO 440 I = I1,NQNYH
440     YH1(I) = YH1(I) - YH1(I+NYH)
445     CONTINUE
    IF (IERPJ .LT. 0 .OR. IERSL .LT. 0) GO TO 680
    IF (ABS(H) .LE. HMIN*1.00001D0) GO TO 670
    IF (NCF .EQ. MXNCF) GO TO 670
    RH = 0.25D0
    IPUP = MITER
    IREDO = 1
    GO TO 170
C-----
C The corrector has converged. JCUR is set to 0
C to signal that the Jacobian involved may need updating later.
C The local error test is made and control passes to statement 500
C if it fails.
C-----
450 JCUR = 0
    IF (M .EQ. 0) DSM = DEL/TESCO(2,NQ)
    IF (M .GT. 0) DSM = DVNORM (N, ACOR, EWT)/TESCO(2,NQ)
    IF (DSM .GT. 1.0D0) GO TO 500
C-----
C After a successful step, update the YH array.
C Consider changing H if IALTH = 1. Otherwise decrease IALTH by 1.
C If IALTH is then 1 and NQ .lt. MAXORD, then ACOR is saved for
C use in a possible order increase on the next step.
C If a change in H is considered, an increase or decrease in order
C by one is considered also. A change in H is made only if it is by a
C factor of at least 1.1. If not, IALTH is set to 3 to prevent
C testing for that many steps.
C-----
    KFLAG = 0
    IREDO = 0
    NST = NST + 1
    HU = H
    NQU = NQ
    DO 470 J = 1,L
        DO 470 I = 1,N
470     YH(I,J) = YH(I,J) + EL(J)*ACOR(I)
    IALTH = IALTH - 1

```

```

      IF (IALTH .EQ. 0) GO TO 520
      IF (IALTH .GT. 1) GO TO 700
      IF (L .EQ. LMAX) GO TO 700
      DO 490 I = 1,N
490    YH(I,LMAX) = ACOR(I)
      GO TO 700
C-----
C The error test failed.  KFLAG keeps track of multiple failures.
C Restore TN and the YH array to their previous values, and prepare
C to try the step again.  Compute the optimum step size for this or
C one lower order.  After 2 or more failures, H is forced to decrease
C by a factor of 0.2 or less.
C-----
500  KFLAG = KFLAG - 1
      TN = TOLD
      I1 = NQNYH + 1
      DO 515 JB = 1,NQ
          I1 = I1 - NYH
Cdir$ ivdep
      DO 510 I = I1,NQNYH
510    YH1(I) = YH1(I) - YH1(I+NYH)
515    CONTINUE
      RMAX = 2.0D0
      IF (ABS(H) .LE. HMIN*1.00001D0) GO TO 660
      IF (KFLAG .LE. -3) GO TO 640
      IREDO = 2
      RHUP = 0.0D0
      GO TO 540
C-----
C Regardless of the success or failure of the step, factors
C RHDN, RHSM, and RHUP are computed, by which H could be multiplied
C at order NQ - 1, order NQ, or order NQ + 1, respectively.
C In the case of failure, RHUP = 0.0 to avoid an order increase.
C The largest of these is determined and the new order chosen
C accordingly.  If the order is to be increased, we compute one
C additional scaled derivative.
C-----
520  RHUP = 0.0D0
      IF (L .EQ. LMAX) GO TO 540
      DO 530 I = 1,N
530    SAVF(I) = ACOR(I) - YH(I,LMAX)
      DUP = DVNORM (N, SAVF, EWT)/TESCO(3,NQ)
      EXUP = 1.0D0/(L+1)
      RHUP = 1.0D0/(1.4D0*DUP**EXUP + 0.0000014D0)
540  EXSM = 1.0D0/L
      RHSM = 1.0D0/(1.2D0*DSM**EXSM + 0.0000012D0)
      RHDN = 0.0D0
      IF (NQ .EQ. 1) GO TO 560
      DDN = DVNORM (N, YH(1,L), EWT)/TESCO(1,NQ)
      EXDN = 1.0D0/NQ
      RHDN = 1.0D0/(1.3D0*DDN**EXDN + 0.0000013D0)
560  IF (RHSM .GE. RHUP) GO TO 570
      IF (RHUP .GT. RHDN) GO TO 590
      GO TO 580
570  IF (RHSM .LT. RHDN) GO TO 580
      NEWQ = NQ
      RH = RHSM
      GO TO 620
580  NEWQ = NQ - 1
      RH = RHDN
      IF (KFLAG .LT. 0 .AND. RH .GT. 1.0D0) RH = 1.0D0
      GO TO 620
590  NEWQ = L
      RH = RHUP
      IF (RH .LT. 1.1D0) GO TO 610
      R = EL(L)/L
      DO 600 I = 1,N

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600   YH(I,NEWQ+1) = ACOR(I)*R
      GO TO 630
610   IALTH = 3
      GO TO 700
620   IF ((KFLAG .EQ. 0) .AND. (RH .LT. 1.1D0)) GO TO 610
      IF (KFLAG .LE. -2) RH = MIN(RH,0.2D0)
C-----
C If there is a change of order, reset NQ, l, and the coefficients.
C In any case H is reset according to RH and the YH array is rescaled.
C Then exit from 690 if the step was OK, or redo the step otherwise.
C-----
      IF (NEWQ .EQ. NQ) GO TO 170
630   NQ = NEWQ
      L = NQ + 1
      IRET = 2
      GO TO 150
C-----
C Control reaches this section if 3 or more failures have occurred.
C If 10 failures have occurred, exit with KFLAG = -1.
C It is assumed that the derivatives that have accumulated in the
C YH array have errors of the wrong order. Hence the first
C derivative is recomputed, and the order is set to 1. Then
C H is reduced by a factor of 10, and the step is retried,
C until it succeeds or H reaches HMIN.
C-----
640   IF (KFLAG .EQ. -10) GO TO 660
      RH = 0.1D0
      RH = MAX(HMIN/ABS(H),RH)
      H = H*RH
      DO 645 I = 1,N
645   Y(I) = YH(I,1)
      CALL F (NEQ, TN, Y, SAVF)
      NFE = NFE + 1
      DO 650 I = 1,N
650   YH(I,2) = H*SAVF(I)
      IPUP = MITER
      IALTH = 5
      IF (NQ .EQ. 1) GO TO 200
      NQ = 1
      L = 2
      IRET = 3
      GO TO 150
C-----
C All returns are made through this section. H is saved in HOLD
C to allow the caller to change H on the next step.
C-----
660   KFLAG = -1
      GO TO 720
670   KFLAG = -2
      GO TO 720
680   KFLAG = -3
      GO TO 720
690   RMAX = 10.0D0
700   R = 1.0D0/TESCO(2,NQU)
      DO 710 I = 1,N
710   ACOR(I) = ACOR(I)*R
720   HOLD = H
      JSTART = 1
      RETURN
C----- END OF SUBROUTINE DSTODE -----
      END
*DECK DEWSET
      SUBROUTINE DEWSET (N, ITOL, RTOL, ATOL, YCUR, EWT)
C***BEGIN PROLOGUE DEWSET
C***SUBSIDIARY
C***PURPOSE Set error weight vector.
C***LIBRARY MATHLIB (ODEPACK)

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C***TYPE      DOUBLE PRECISION (SEWSET-S, DEWSET-D)
C***AUTHOR   Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C
C   This subroutine sets the error weight vector EWT according to
C    $EWT(i) = RTOL(i)*ABS(YCUR(i)) + ATOL(i)$ ,  $i = 1, \dots, N$ ,
C   with the subscript on RTOL and/or ATOL possibly replaced by 1 above,
C   depending on the value of ITOL.
C
C***SEE ALSO  DLSODE
C***ROUTINES CALLED  (NONE)
C***REVISION HISTORY  (YMMDD)
C   791129  DATE WRITTEN
C   890501  Modified prologue to SLATEC/LDOC format.  (FNF)
C   890503  Minor cosmetic changes.  (FNF)
C   930809  Renamed to allow single/double precision versions.  (ACH)
C***END PROLOGUE  DEWSET
C**End
      INTEGER N, ITOL
      INTEGER I
      DOUBLE PRECISION RTOL, ATOL, YCUR, EWT
      DIMENSION RTOL(*), ATOL(*), YCUR(N), EWT(N)
C
C***FIRST EXECUTABLE STATEMENT  DEWSET
      GO TO (10, 20, 30, 40), ITOL
10    CONTINUE
      DO 15 I = 1,N
15      EWT(I) = RTOL(1)*ABS(YCUR(I)) + ATOL(1)
      RETURN
20    CONTINUE
      DO 25 I = 1,N
25      EWT(I) = RTOL(1)*ABS(YCUR(I)) + ATOL(I)
      RETURN
30    CONTINUE
      DO 35 I = 1,N
35      EWT(I) = RTOL(I)*ABS(YCUR(I)) + ATOL(1)
      RETURN
40    CONTINUE
      DO 45 I = 1,N
45      EWT(I) = RTOL(I)*ABS(YCUR(I)) + ATOL(I)
      RETURN
C----- END OF SUBROUTINE DEWSET -----
      END
*DECK DVNORM
      DOUBLE PRECISION FUNCTION DVNORM (N, V, W)
C***BEGIN PROLOGUE  DVNORM
C***SUBSIDIARY
C***PURPOSE  Weighted root-mean-square vector norm.
C***LIBRARY  MATHLIB (ODEPACK)
C***TYPE      DOUBLE PRECISION (SVNORM-S, DVNORM-D)
C***AUTHOR   Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C
C   This function routine computes the weighted root-mean-square norm
C   of the vector of length N contained in the array V, with weights
C   contained in the array W of length N:
C    $DVNORM = \sqrt{(1/N) * \sum (V(i)*W(i))**2}$ 
C
C***SEE ALSO  DLSODE
C***ROUTINES CALLED  (NONE)
C***REVISION HISTORY  (YMMDD)
C   791129  DATE WRITTEN
C   890501  Modified prologue to SLATEC/LDOC format.  (FNF)
C   890503  Minor cosmetic changes.  (FNF)
C   930809  Renamed to allow single/double precision versions.  (ACH)
C***END PROLOGUE  DVNORM
C**End

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```

      INTEGER N, I
      DOUBLE PRECISION V, W, SUM
      DIMENSION V(N), W(N)
C
C***FIRST EXECUTABLE STATEMENT DVNORM
      SUM = 0.0D0
      DO 10 I = 1,N
10      SUM = SUM + (V(I)*W(I))**2
      DVNORM = SQRT(SUM/N)
      RETURN
C----- END OF FUNCTION DVNORM -----
      END
*DECK DUMACH
      DOUBLE PRECISION FUNCTION DUMACH ()
C***BEGIN PROLOGUE DUMACH
C***PURPOSE Compute the unit roundoff of the machine.
C***LIBRARY MATHLIB
C***CATEGORY R1
C***TYPE DOUBLE PRECISION (RUMACH-S, DUMACH-D)
C***KEYWORDS MACHINE CONSTANTS
C***AUTHOR Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C *Usage:
C      DOUBLE PRECISION A, DUMACH
C      A = DUMACH()
C
C *Function Return Values:
C      A : the unit roundoff of the machine.
C
C *Description:
C      The unit roundoff is defined as the smallest positive machine
C      number u such that 1.0 + u .ne. 1.0. This is computed by DUMACH
C      in a machine-independent manner.
C
C***REFERENCES (NONE)
C***ROUTINES CALLED (NONE)
C***REVISION HISTORY (YMMDD)
C      930216 DATE WRITTEN
C      930818 Added SLATEC-format prologue. (FNF)
C***END PROLOGUE DUMACH
C
C*Internal Notes:
C-----
C Subroutines/functions called by DUMACH.. None
C-----
C**End
C
      DOUBLE PRECISION U, COMP
C***FIRST EXECUTABLE STATEMENT DUMACH
      U = 1.0D0
10      U = U*0.5D0
      COMP = 1.0D0 + U
      IF (COMP .NE. 1.0D0) GO TO 10
      DUMACH = U*2.0D0
      RETURN
C----- End of Function DUMACH -----
      END
*DECK XERRWD
      SUBROUTINE XERRWD (MSG, NMES, NERR, LEVEL, NI, I1, I2, NR, R1, R2)
C***BEGIN PROLOGUE XERRWD
C***SUBSIDIARY
C***PURPOSE Write error message with values.
C***LIBRARY MATHLIB
C***CATEGORY R3C
C***TYPE DOUBLE PRECISION (XERRWV-S, XERRWD-D)
C***AUTHOR Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION

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```
C
C Subroutines XERRWD, XSETF, XSETUN, and the function routine IXSAV,
C as given here, constitute a simplified version of the SLATEC error
C handling package.
C
C All arguments are input arguments.
C
C MSG      = The message (character array).
C NMES     = The length of MSG (number of characters).
C NERR     = The error number (not used).
C LEVEL    = The error level..
C           0 or 1 means recoverable (control returns to caller).
C           2 means fatal (run is aborted--see note below).
C NI       = Number of integers (0, 1, or 2) to be printed with message.
C I1,I2    = Integers to be printed, depending on NI.
C NR       = Number of reals (0, 1, or 2) to be printed with message.
C R1,R2    = Reals to be printed, depending on NR.
C
C Note.. this routine is machine-dependent and specialized for use
C in limited context, in the following ways..
C 1. The argument MSG is assumed to be of type CHARACTER, and
C    the message is printed with a format of (1X,A).
C 2. The message is assumed to take only one line.
C    Multi-line messages are generated by repeated calls.
C 3. If LEVEL = 2, control passes to the statement STOP
C    to abort the run. This statement may be machine-dependent.
C 4. R1 and R2 are assumed to be in double precision and are printed
C    in D21.13 format.
C
C***ROUTINES CALLED IXSAV
C***REVISION HISTORY (YYMMDD)
C 920831 DATE WRITTEN
C 921118 Replaced MFLGSV/LUNSAV by IXSAV. (ACH)
C 930329 Modified prologue to SLATEC format. (FNF)
C 930407 Changed MSG from CHARACTER*1 array to variable. (FNF)
C 930922 Minor cosmetic change. (FNF)
C***END PROLOGUE XERRWD
C
C*Internal Notes:
C
C For a different default logical unit number, IXSAV (or a subsidiary
C routine that it calls) will need to be modified.
C For a different run-abort command, change the statement following
C statement 100 at the end.
C-----
C Subroutines called by XERRWD.. None
C Function routine called by XERRWD.. IXSAV
C-----
C**End
C
C Declare arguments.
C
C     DOUBLE PRECISION R1, R2
C     INTEGER NMES, NERR, LEVEL, NI, I1, I2, NR
C     CHARACTER*(*) MSG
C
C Declare local variables.
C
C     INTEGER LUNIT, IXSAV, MESFLG
C
C Get logical unit number and message print flag.
C
C***FIRST EXECUTABLE STATEMENT XERRWD
C     LUNIT = IXSAV (1, 0, .FALSE.)
C     MESFLG = IXSAV (2, 0, .FALSE.)
C     IF (MESFLG .EQ. 0) GO TO 100
C
```



```

C Write the message.
C
  WRITE (LUNIT,10) MSG
10  FORMAT(1X,A)
   IF (NI .EQ. 1) WRITE (LUNIT, 20) I1
20  FORMAT(6X,'In above message, I1 =',I10)
   IF (NI .EQ. 2) WRITE (LUNIT, 30) I1,I2
30  FORMAT(6X,'In above message, I1 =',I10,3X,'I2 =',I10)
   IF (NR .EQ. 1) WRITE (LUNIT, 40) R1
40  FORMAT(6X,'In above message, R1 =',D21.13)
   IF (NR .EQ. 2) WRITE (LUNIT, 50) R1,R2
50  FORMAT(6X,'In above, R1 =',D21.13,3X,'R2 =',D21.13)
C
C Abort the run if LEVEL = 2.
C
100 IF (LEVEL .NE. 2) RETURN
    STOP
C----- End of Subroutine XERRWD -----
      END
*DECK XSETF
      SUBROUTINE XSETF (MFLAG)
C***BEGIN PROLOGUE XSETF
C***PURPOSE Reset the error print control flag.
C***LIBRARY MATHLIB
C***CATEGORY R3A
C***TYPE ALL (XSETF-A)
C***KEYWORDS ERROR CONTROL
C***AUTHOR Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C
C XSETF sets the error print control flag to MFLAG:
C MFLAG=1 means print all messages (the default).
C MFLAG=0 means no printing.
C
C***SEE ALSO XERMSG, XERRWD, XERRWV
C***REFERENCES (NONE)
C***ROUTINES CALLED IXSAV
C***REVISION HISTORY (YMMDD)
C 921118 DATE WRITEN
C 930329 Added SLATEC format prologue. (FNF)
C 930407 Corrected SEE ALSO section. (FNF)
C 930922 Made user-callable, and other cosmetic changes. (FNF)
C***END PROLOGUE XSETF
C
C Subroutines called by XSETF.. None
C Function routine called by XSETF.. IXSAV
C-----
C**End
      INTEGER MFLAG, JUNK, IXSAV
C
C***FIRST EXECUTABLE STATEMENT XSETF
      IF (MFLAG .EQ. 0 .OR. MFLAG .EQ. 1) JUNK = IXSAV (2,MFLAG,.TRUE.)
      RETURN
C----- End of Subroutine XSETF -----
      END
*DECK XSETUN
      SUBROUTINE XSETUN (LUN)
C***BEGIN PROLOGUE XSETUN
C***PURPOSE Reset the logical unit number for error messages.
C***LIBRARY MATHLIB
C***CATEGORY R3B
C***TYPE ALL (XSETUN-A)
C***KEYWORDS ERROR CONTROL
C***DESCRIPTION
C
C XSETUN sets the logical unit number for error messages to LUN.
C

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C***AUTHOR Hindmarsh, Alan C., (LLNL)
C***SEE ALSO XERMSG, XERRWD, XERRWV
C***REFERENCES (NONE)
C***ROUTINES CALLED IXSAV
C***REVISION HISTORY (YMMDD)
C 921118 DATE WRITTEN
C 930329 Added SLATEC format prologue. (FNF)
C 930407 Corrected SEE ALSO section. (FNF)
C 930922 Made user-callable, and other cosmetic changes. (FNF)
C***END PROLOGUE XSETUN
C
C Subroutines called by XSETUN.. None
C Function routine called by XSETUN.. IXSAV
C-----
C**End
      INTEGER LUN, JUNK, IXSAV
C
C***FIRST EXECUTABLE STATEMENT XSETUN
      IF (LUN .GT. 0) JUNK = IXSAV (1,LUN,.TRUE.)
      RETURN
C----- End of Subroutine XSETUN -----
      END
*DECK IXSAV
      INTEGER FUNCTION IXSAV (IPAR, IVALUE, ISET)
C***BEGIN PROLOGUE IXSAV
C***SUBSIDIARY
C***PURPOSE Save and recall error message control parameters.
C***LIBRARY MATHLIB
C***CATEGORY R3C
C***TYPE ALL (IXSAV-A)
C***AUTHOR Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C
C IXSAV saves and recalls one of two error message parameters:
C LUNIT, the logical unit number to which messages are printed, and
C MESFLG, the message print flag.
C This is a modification of the SLATEC library routine J4SAVE.
C
C Saved local variables..
C LUNIT = Logical unit number for messages. The default is obtained
C by a call to IUMACH (may be machine-dependent).
C MESFLG = Print control flag..
C 1 means print all messages (the default).
C 0 means no printing.
C
C On input..
C IPAR = Parameter indicator (1 for LUNIT, 2 for MESFLG).
C IVALUE = The value to be set for the parameter, if ISET = .TRUE.
C ISET = Logical flag to indicate whether to read or write.
C If ISET = .TRUE., the parameter will be given
C the value IVALUE. If ISET = .FALSE., the parameter
C will be unchanged, and IVALUE is a dummy argument.
C
C On return..
C IXSAV = The (old) value of the parameter.
C
C***SEE ALSO XERMSG, XERRWD, XERRWV
C***ROUTINES CALLED IUMACH
C***REVISION HISTORY (YMMDD)
C 921118 DATE WRITTEN
C 930329 Modified prologue to SLATEC format. (FNF)
C 930915 Added IUMACH call to get default output unit. (ACH)
C 930922 Minor cosmetic changes. (FNF)
C***END PROLOGUE IXSAV
C
C Subroutines called by IXSAV.. None
C Function routine called by IXSAV.. IUMACH

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C-----
C**End
      LOGICAL ISET
      INTEGER IPAR, IVALUE
C-----
      INTEGER LUNIT, MESFLG
C-----
C The following Fortran-77 declaration is to cause the values of the
C listed (local) variables to be saved between calls to this routine.
C-----
      SAVE LUNIT, MESFLG
      DATA LUNIT/-1/, MESFLG/1/
C
C***FIRST EXECUTABLE STATEMENT  IXSAV
      IF (IPAR .EQ. 1) THEN
          IF (LUNIT .EQ. -1) LUNIT = IUMACH()
          IXSAV = LUNIT
          IF (ISET) LUNIT = IVALUE
          ENDIF
C
      IF (IPAR .EQ. 2) THEN
          IXSAV = MESFLG
          IF (ISET) MESFLG = IVALUE
          ENDIF
C
      RETURN
C----- End of Function IXSAV -----
      END
*DECK IUMACH
      INTEGER FUNCTION IUMACH()
C***BEGIN PROLOGUE  IUMACH
C***PURPOSE  Provide standard output unit number.
C***LIBRARY  MATHLIB
C***CATEGORY  R1
C***TYPE     INTEGER (IUMACH-I)
C***KEYWORDS  MACHINE CONSTANTS
C***AUTHOR  Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C *Usage:
C     INTEGER  LOUT, IUMACH
C     LOUT = IUMACH()
C
C *Function Return Values:
C     LOUT : the standard logical unit for Fortran output.
C
C***REFERENCES  (NONE)
C***ROUTINES CALLED  (NONE)
C***REVISION HISTORY  (YYMMDD)
C   930915  DATE WRITTEN
C   930922  Made user-callable, and other cosmetic changes. (FNF)
C***END PROLOGUE  IUMACH
C
C*Internal Notes:
C The built-in value of 6 is standard on a wide range of Fortran
C systems. This may be machine-dependent.
C**End
C***FIRST EXECUTABLE STATEMENT  IUMACH
      IUMACH = 6
C
      RETURN
C----- End of Function IUMACH -----
      END

      subroutine dgefa(a,lda,n,ipvt,info)
      integer lda,n,ipvt(1),info
      double precision a(lda,1)
c

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```
c  dgefa factors a double precision matrix by gaussian elimination.
c
c  dgefa is usually called by dgeco, but it can be called
c  directly with a saving in time if rcond is not needed.
c  (time for dgeco) = (1 + 9/n)*(time for dgefa) .
c
c  on entry
c
c    a      double precision(lda, n)
c           the matrix to be factored.
c
c    lda    integer
c           the leading dimension of the array a .
c
c    n      integer
c           the order of the matrix a .
c
c  on return
c
c    a      an upper triangular matrix and the multipliers
c           which were used to obtain it.
c           the factorization can be written a = l*u where
c           l is a product of permutation and unit lower
c           triangular matrices and u is upper triangular.
c
c    ipvt   integer(n)
c           an integer vector of pivot indices.
c
c    info   integer
c           = 0 normal value.
c           = k if u(k,k) .eq. 0.0 . this is not an error
c           condition for this subroutine, but it does
c           indicate that dgesl or dgedi will divide by zero
c           if called. use rcond in dgeco for a reliable
c           indication of singularity.
c
c  linpack. this version dated 08/14/78 .
c  cleve moler, university of new mexico, argonne national lab.
c
c  subroutines and functions
c
c  blas daxpy,dscal,idamax
c
c  internal variables
c
c  double precision t
c  integer idamax,j,k,kpl,l,nml
c
c
c  gaussian elimination with partial pivoting
c
c  info = 0
c  nml = n - 1
c  if (nml .lt. 1) go to 70
c  do 60 k = 1, nml
c    kpl = k + 1
c
c    find l = pivot index
c
c    l = idamax(n-k+1,a(k,k),1) + k - 1
c    ipvt(k) = l
c
c    zero pivot implies this column already triangularized
c
c    if (a(l,k) .eq. 0.0d0) go to 40
c
c    interchange if necessary
```

```

c
      if (l .eq. k) go to 10
      t = a(l,k)
      a(l,k) = a(k,k)
      a(k,k) = t
10    continue
c
c      compute multipliers
c
      t = -1.0d0/a(k,k)
      call dscal(n-k,t,a(k+1,k),1)
c
c      row elimination with column indexing
c
      do 30 j = kp1, n
      t = a(l,j)
      if (l .eq. k) go to 20
      a(l,j) = a(k,j)
      a(k,j) = t
20    continue
      call daxpy(n-k,t,a(k+1,k),1,a(k+1,j),1)
30    continue
      go to 50
40    continue
      info = k
50    continue
60 continue
70 continue
      ipvt(n) = n
      if (a(n,n) .eq. 0.0d0) info = n
      return
      end
      subroutine dgesl(a,lda,n,ipvt,b,job)
      integer lda,n,ipvt(1),job
      double precision a(lda,1),b(1)
c
c      dgesl solves the double precision system
c      a * x = b or trans(a) * x = b
c      using the factors computed by dgeco or dgefa.
c
c      on entry
c
c      a      double precision(lda, n)
c             the output from dgeco or dgefa.
c
c      lda    integer
c             the leading dimension of the array a .
c
c      n      integer
c             the order of the matrix a .
c
c      ipvt   integer(n)
c             the pivot vector from dgeco or dgefa.
c
c      b      double precision(n)
c             the right hand side vector.
c
c      job    integer
c             = 0      to solve a*x = b ,
c             = nonzero to solve trans(a)*x = b where
c                   trans(a) is the transpose.
c
c      on return
c
c      b      the solution vector x .
c
c      error condition

```

```

c
c   a division by zero will occur if the input factor contains a
c   zero on the diagonal.  technically this indicates singularity
c   but it is often caused by improper arguments or improper
c   setting of lda .  it will not occur if the subroutines are
c   called correctly and if dgeco has set rcond .gt. 0.0
c   or dgefa has set info .eq. 0 .
c
c   to compute inverse(a) * c where c is a matrix
c   with p columns
c       call dgeco(a,lda,n,ipvt,rcond,z)
c       if (rcond is too small) go to ...
c       do 10 j = 1, p
c           call dgesl(a,lda,n,ipvt,c(1,j),0)
c       10 continue
c
c   linpack. this version dated 08/14/78 .
c   cleve moler, university of new mexico, argonne national lab.
c
c   subroutines and functions
c
c   blas daxpy,ddot
c
c   internal variables
c
c   double precision ddot,t
c   integer k,kb,l,nm1
c
c   nm1 = n - 1
c   if (job .ne. 0) go to 50
c
c   job = 0 , solve a * x = b
c   first solve l*y = b
c
c       if (nm1 .lt. 1) go to 30
c       do 20 k = 1, nm1
c           l = ipvt(k)
c           t = b(l)
c           if (l .eq. k) go to 10
c           b(l) = b(k)
c           b(k) = t
c   10      continue
c           call daxpy(n-k,t,a(k+1,k),1,b(k+1),1)
c   20      continue
c   30      continue
c
c   now solve u*x = y
c
c       do 40 kb = 1, n
c           k = n + 1 - kb
c           b(k) = b(k)/a(k,k)
c           t = -b(k)
c           call daxpy(k-1,t,a(1,k),1,b(1),1)
c   40      continue
c       go to 100
c   50      continue
c
c   job = nonzero, solve trans(a) * x = b
c   first solve trans(u)*y = b
c
c       do 60 k = 1, n
c           t = ddot(k-1,a(1,k),1,b(1),1)
c           b(k) = (b(k) - t)/a(k,k)
c   60      continue
c
c   now solve trans(l)*x = y
c

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```

        if (nml .lt. 1) go to 90
        do 80 kb = 1, nml
            k = n - kb
            b(k) = b(k) + ddot(n-k,a(k+1,k),1,b(k+1),1)
            l = ipvt(k)
            if (l .eq. k) go to 70
                t = b(l)
                b(l) = b(k)
                b(k) = t
        70         continue
        80         continue
        90         continue
100 continue
    return
end
subroutine dgbfa(abd,lda,n,ml,mu,ipvt,info)
integer lda,n,ml,mu,ipvt(1),info
double precision abd(lda,1)

```

c
c dgbfa factors a double precision band matrix by elimination.
c
c dgbfa is usually called by dgbco, but it can be called
c directly with a saving in time if rcond is not needed.
c
c on entry
c
c abd double precision(lda, n)
c contains the matrix in band storage. the columns
c of the matrix are stored in the columns of abd and
c the diagonals of the matrix are stored in rows
c ml+1 through 2*ml+mu+1 of abd .
c see the comments below for details.
c
c lda integer
c the leading dimension of the array abd .
c lda must be .ge. 2*ml + mu + 1 .
c
c n integer
c the order of the original matrix.
c
c ml integer
c number of diagonals below the main diagonal.
c 0 .le. ml .lt. n .
c
c mu integer
c number of diagonals above the main diagonal.
c 0 .le. mu .lt. n .
c more efficient if ml .le. mu .
c on return
c
c abd an upper triangular matrix in band storage and
c the multipliers which were used to obtain it.
c the factorization can be written $a = l*u$ where
c l is a product of permutation and unit lower
c triangular matrices and u is upper triangular.
c
c ipvt integer(n)
c an integer vector of pivot indices.
c
c info integer
c = 0 normal value.
c = k if u(k,k) .eq. 0.0 . this is not an error
c condition for this subroutine, but it does
c indicate that dgbfa will divide by zero if
c called. use rcond in dgbco for a reliable
c indication of singularity.
c

```

c   band storage
c
c   if a is a band matrix, the following program segment
c   will set up the input.
c
c       ml = (band width below the diagonal)
c       mu = (band width above the diagonal)
c       m = ml + mu + 1
c       do 20 j = 1, n
c           i1 = max0(1, j-mu)
c           i2 = min0(n, j+ml)
c           do 10 i = i1, i2
c               k = i - j + m
c               abd(k,j) = a(i,j)
c           10 continue
c       20 continue
c
c   this uses rows ml+1 through 2*ml+mu+1 of abd .
c   in addition, the first ml rows in abd are used for
c   elements generated during the triangularization.
c   the total number of rows needed in abd is 2*ml+mu+1 .
c   the ml+mu by ml+mu upper left triangle and the
c   ml by ml lower right triangle are not referenced.
c
c   linpack. this version dated 08/14/78 .
c   cleve moler, university of new mexico, argonne national lab.
c
c   subroutines and functions
c
c   blas daxpy,dscal,idamax
c   fortran max0,min0
c
c   internal variables
c
c   double precision t
c   integer i,idamax,i0,j,ju,jz,j0,j1,k,kp1,l,lm,m,mm,nml
c
c
c   m = ml + mu + 1
c   info = 0
c
c   zero initial fill-in columns
c
c   j0 = mu + 2
c   j1 = min0(n,m) - 1
c   if (j1 .lt. j0) go to 30
c   do 20 jz = j0, j1
c       i0 = m + 1 - jz
c       do 10 i = i0, ml
c           abd(i,jz) = 0.0d0
c       10 continue
c   20 continue
c   30 continue
c   jz = j1
c   ju = 0
c
c   gaussian elimination with partial pivoting
c
c   nml = n - 1
c   if (nml .lt. 1) go to 130
c   do 120 k = 1, nml
c       kp1 = k + 1
c
c       zero next fill-in column
c
c       jz = jz + 1
c       if (jz .gt. n) go to 50

```



```

        if (ml .lt. 1) go to 50
        do 40 i = 1, ml
            abd(i,jz) = 0.0d0
40         continue
50         continue
c
c         find l = pivot index
c
        lm = min0(ml,n-k)
        l = idamax(lm+1,abd(m,k),1) + m - 1
        ipvt(k) = l + k - m
c
c         zero pivot implies this column already triangularized
c
        if (abd(l,k) .eq. 0.0d0) go to 100
c
c         interchange if necessary
c
        if (l .eq. m) go to 60
        t = abd(l,k)
        abd(l,k) = abd(m,k)
        abd(m,k) = t
60         continue
c
c         compute multipliers
c
        t = -1.0d0/abd(m,k)
        call dscal(lm,t,abd(m+1,k),1)
c
c         row elimination with column indexing
c
        ju = min0(max0(ju,mu+ipvt(k)),n)
        mm = m
        if (ju .lt. kp1) go to 90
        do 80 j = kp1, ju
            l = l - 1
            mm = mm - 1
            t = abd(l,j)
            if (l .eq. mm) go to 70
            abd(l,j) = abd(mm,j)
            abd(mm,j) = t
70         continue
            call daxpy(lm,t,abd(m+1,k),1,abd(mm+1,j),1)
80         continue
90         continue
        go to 110
100        continue
        info = k
110        continue
120 continue
130 continue
        ipvt(n) = n
        if (abd(m,n) .eq. 0.0d0) info = n
        return
        end
        subroutine dgbsl(abd,lda,n,ml,mu,ipvt,b,job)
        integer lda,n,ml,mu,ipvt(1),job
        double precision abd(lda,1),b(1)
c
c         dgbsl solves the double precision band system
c         a * x = b or trans(a) * x = b
c         using the factors computed by dgbc0 or dgbf0.
c
c         on entry
c
c         abd      double precision(lda, n)
c                 the output from dgbc0 or dgbf0.

```

```

c
c      lda      integer
c              the leading dimension of the array  abd .
c
c      n        integer
c              the order of the original matrix.
c
c      ml       integer
c              number of diagonals below the main diagonal.
c
c      mu       integer
c              number of diagonals above the main diagonal.
c
c      ipvt     integer(n)
c              the pivot vector from dgbco or dgbfa.
c
c      b        double precision(n)
c              the right hand side vector.
c
c      job      integer
c              = 0          to solve  a*x = b ,
c              = nonzero    to solve  trans(a)*x = b , where
c                          trans(a)  is the transpose.
c
c on return
c
c      b        the solution vector  x .
c
c error condition
c
c      a division by zero will occur if the input factor contains a
c      zero on the diagonal.  technically this indicates singularity
c      but it is often caused by improper arguments or improper
c      setting of lda .  it will not occur if the subroutines are
c      called correctly and if dgbco has set rcond .gt. 0.0
c      or dgbfa has set info .eq. 0 .
c
c to compute inverse(a) * c  where  c  is a matrix
c with  p  columns
c      call dgbco(abd,lda,n,ml,mu,ipvt,rcond,z)
c      if (rcond is too small) go to ...
c      do 10 j = 1, p
c          call dgbsl(abd,lda,n,ml,mu,ipvt,c(1,j),0)
c      10 continue
c
c linpack. this version dated 08/14/78 .
c cleve moler, university of new mexico, argonne national lab.
c
c subroutines and functions
c
c blas daxpy,ddot
c fortran min0
c
c internal variables
c
c double precision ddot,t
c integer k,kb,l,la,lb,lm,m,nml
c
c m = mu + ml + 1
c nml = n - 1
c if (job .ne. 0) go to 50
c
c      job = 0 , solve  a * x = b
c      first solve  l*y = b
c
c      if (ml .eq. 0) go to 30
c      if (nml .lt. 1) go to 30

```

```

        do 20 k = 1, nm1
            lm = min0(m1,n-k)
            l = ipvt(k)
            t = b(l)
            if (l .eq. k) go to 10
                b(l) = b(k)
                b(k) = t
10         continue
            call daxpy(lm,t,abd(m+1,k),1,b(k+1),1)
20         continue
30         continue
c
c         now solve u*x = y
c
        do 40 kb = 1, n
            k = n + 1 - kb
            b(k) = b(k)/abd(m,k)
            lm = min0(k,m) - 1
            la = m - lm
            lb = k - lm
            t = -b(k)
            call daxpy(lm,t,abd(la,k),1,b(lb),1)
40         continue
        go to 100
50         continue
c
c         job = nonzero, solve trans(a) * x = b
c         first solve trans(u)*y = b
c
        do 60 k = 1, n
            lm = min0(k,m) - 1
            la = m - lm
            lb = k - lm
            t = ddot(lm,abd(la,k),1,b(lb),1)
            b(k) = (b(k) - t)/abd(m,k)
60         continue
c
c         now solve trans(l)*x = y
c
        if (m1 .eq. 0) go to 90
        if (nm1 .lt. 1) go to 90
        do 80 kb = 1, nm1
            k = n - kb
            lm = min0(m1,n-k)
            b(k) = b(k) + ddot(lm,abd(m+1,k),1,b(k+1),1)
            l = ipvt(k)
            if (l .eq. k) go to 70
                t = b(l)
                b(l) = b(k)
                b(k) = t
70         continue
80         continue
90         continue
100        continue
        return
        end
        subroutine daxpy(n,da,dx,incx,dy,incy)
c
c         constant times a vector plus a vector.
c         uses unrolled loops for increments equal to one.
c         jack dongarra, linpack, 3/11/78.
c
        double precision dx(1),dy(1),da
        integer i,incx,incy,ix,iy,m,mp1,n
c
        if(n.le.0) return
        if (da .eq. 0.0d0) return

```

```

if(incx.eq.1.and.incy.eq.1)go to 20
c
c      code for unequal increments or equal increments
c      not equal to 1
c
ix = 1
iy = 1
if(incx.lt.0)ix = (-n+1)*incx + 1
if(incy.lt.0)iy = (-n+1)*incy + 1
do 10 i = 1,n
  dy(iy) = dy(iy) + da*dx(ix)
  ix = ix + incx
  iy = iy + incy
10 continue
return
c
c      code for both increments equal to 1
c
c      clean-up loop
c
20 m = mod(n,4)
if( m .eq. 0 ) go to 40
do 30 i = 1,m
  dy(i) = dy(i) + da*dx(i)
30 continue
if( n .lt. 4 ) return
40 mp1 = m + 1
do 50 i = mp1,n,4
  dy(i) = dy(i) + da*dx(i)
  dy(i + 1) = dy(i + 1) + da*dx(i + 1)
  dy(i + 2) = dy(i + 2) + da*dx(i + 2)
  dy(i + 3) = dy(i + 3) + da*dx(i + 3)
50 continue
return
end
subroutine dscal(n,da,dx,incx)
c
c      scales a vector by a constant.
c      uses unrolled loops for increment equal to one.
c      jack dongarra, linpack, 3/11/78.
c
double precision da,dx(1)
integer i,incx,m,mp1,n,nincx
c
if(n.le.0)return
if(incx.eq.1)go to 20
c
c      code for increment not equal to 1
c
nincx = n*incx
do 10 i = 1,nincx,incx
  dx(i) = da*dx(i)
10 continue
return
c
c      code for increment equal to 1
c
c      clean-up loop
c
20 m = mod(n,5)
if( m .eq. 0 ) go to 40
do 30 i = 1,m
  dx(i) = da*dx(i)
30 continue
if( n .lt. 5 ) return

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```

40 mp1 = m + 1
   do 50 i = mp1,n,5
       dx(i) = da*dx(i)
       dx(i + 1) = da*dx(i + 1)
       dx(i + 2) = da*dx(i + 2)
       dx(i + 3) = da*dx(i + 3)
       dx(i + 4) = da*dx(i + 4)
50 continue
return
end
double precision function ddot(n,dx,incx,dy,incy)
c
c forms the dot product of two vectors.
c uses unrolled loops for increments equal to one.
c jack dongarra, linpack, 3/11/78.
c
double precision dx(1),dy(1),dtemp
integer i,incx,incy,ix,iy,m,mp1,n
c
ddot = 0.0d0
dtemp = 0.0d0
if(n.le.0)return
if(incx.eq.1.and.incy.eq.1)go to 20
c
c code for unequal increments or equal increments
c not equal to 1
c
ix = 1
iy = 1
if(incx.lt.0)ix = (-n+1)*incx + 1
if(incy.lt.0)iy = (-n+1)*incy + 1
do 10 i = 1,n
    dtemp = dtemp + dx(ix)*dy(iy)
    ix = ix + incx
    iy = iy + incy
10 continue
ddot = dtemp
return
c
c code for both increments equal to 1
c
c clean-up loop
c
20 m = mod(n,5)
   if( m .eq. 0 ) go to 40
   do 30 i = 1,m
       dtemp = dtemp + dx(i)*dy(i)
30 continue
   if( n .lt. 5 ) go to 60
40 mp1 = m + 1
   do 50 i = mp1,n,5
       dtemp = dtemp + dx(i)*dy(i) + dx(i + 1)*dy(i + 1) +
* dx(i + 2)*dy(i + 2) + dx(i + 3)*dy(i + 3) + dx(i + 4)*dy(i + 4)
50 continue
60 ddot = dtemp
return
end
integer function idamax(n,dx,incx)
c
c finds the index of element having max. absolute value.
c jack dongarra, linpack, 3/11/78.
c
double precision dx(1),dmax
integer i,incx,ix,n
c
idamax = 0

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```

    if( n .lt. 1 ) return
    idamax = 1
    if(n.eq.1) return
    if(incx.eq.1) go to 20
c
c     code for increment not equal to 1
c
    ix = 1
    dmax = dabs(dx(1))
    ix = ix + incx
    do 10 i = 2,n
        if(dabs(dx(ix)).le.dmax) go to 5
        idamax = i
        dmax = dabs(dx(ix))
    5   ix = ix + incx
10  continue
    return
c
c     code for increment equal to 1
c
20  dmax = dabs(dx(1))
    do 30 i = 2,n
        if(dabs(dx(i)).le.dmax) go to 30
        idamax = i
        dmax = dabs(dx(i))
30  continue
    return
end
subroutine dcopy(n,sx,incx,sy,incy)
c
c  copies a vector, x, to a vector, y.
c  uses unrolled loops for increments equal to 1.
c  jack dongarra, linpack, 3/11/78.
c
    double precision sx(1),sy(1)
    integer i,incx,incy,ix,iy,m,mp1,n
c
    if(n.le.0) return
    if(incx.eq.1.and.incy.eq.1) go to 20
c
c     code for unequal increments or equal increments
c     not equal to 1
c
    ix = 1
    iy = 1
    if(incx.lt.0) ix = (-n+1)*incx + 1
    if(incy.lt.0) iy = (-n+1)*incy + 1
    do 10 i = 1,n
        sy(iy) = sx(ix)
        ix = ix + incx
        iy = iy + incy
10  continue
    return
c
c     code for both increments equal to 1
c
c
c     clean-up loop
c
20  m = mod(n,7)
    if( m .eq. 0 ) go to 40
    do 30 i = 1,m
        sy(i) = sx(i)
30  continue
    if( n .lt. 7 ) return
40  mp1 = m + 1
    do 50 i = mp1,n,7

```

```
    sy(i) = sx(i)
    sy(i + 1) = sx(i + 1)
    sy(i + 2) = sx(i + 2)
    sy(i + 3) = sx(i + 3)
    sy(i + 4) = sx(i + 4)
    sy(i + 5) = sx(i + 5)
    sy(i + 6) = sx(i + 6)
50 continue
return
end
```